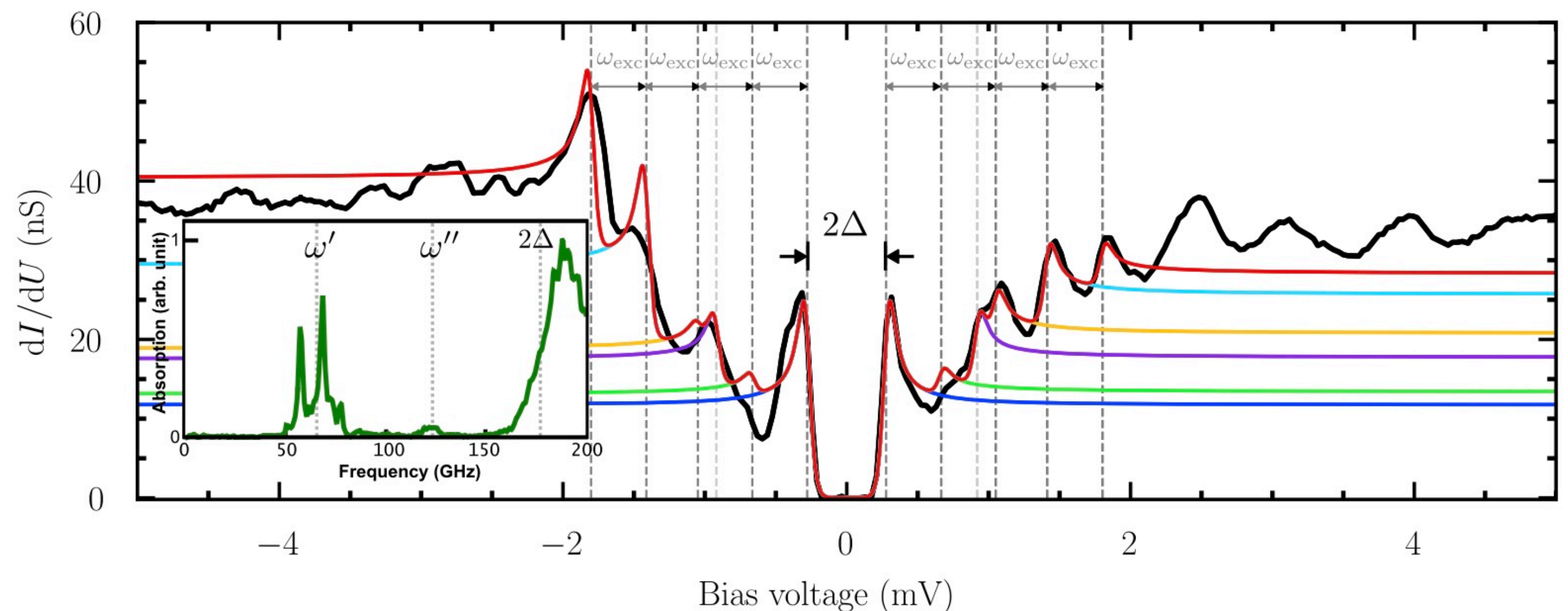
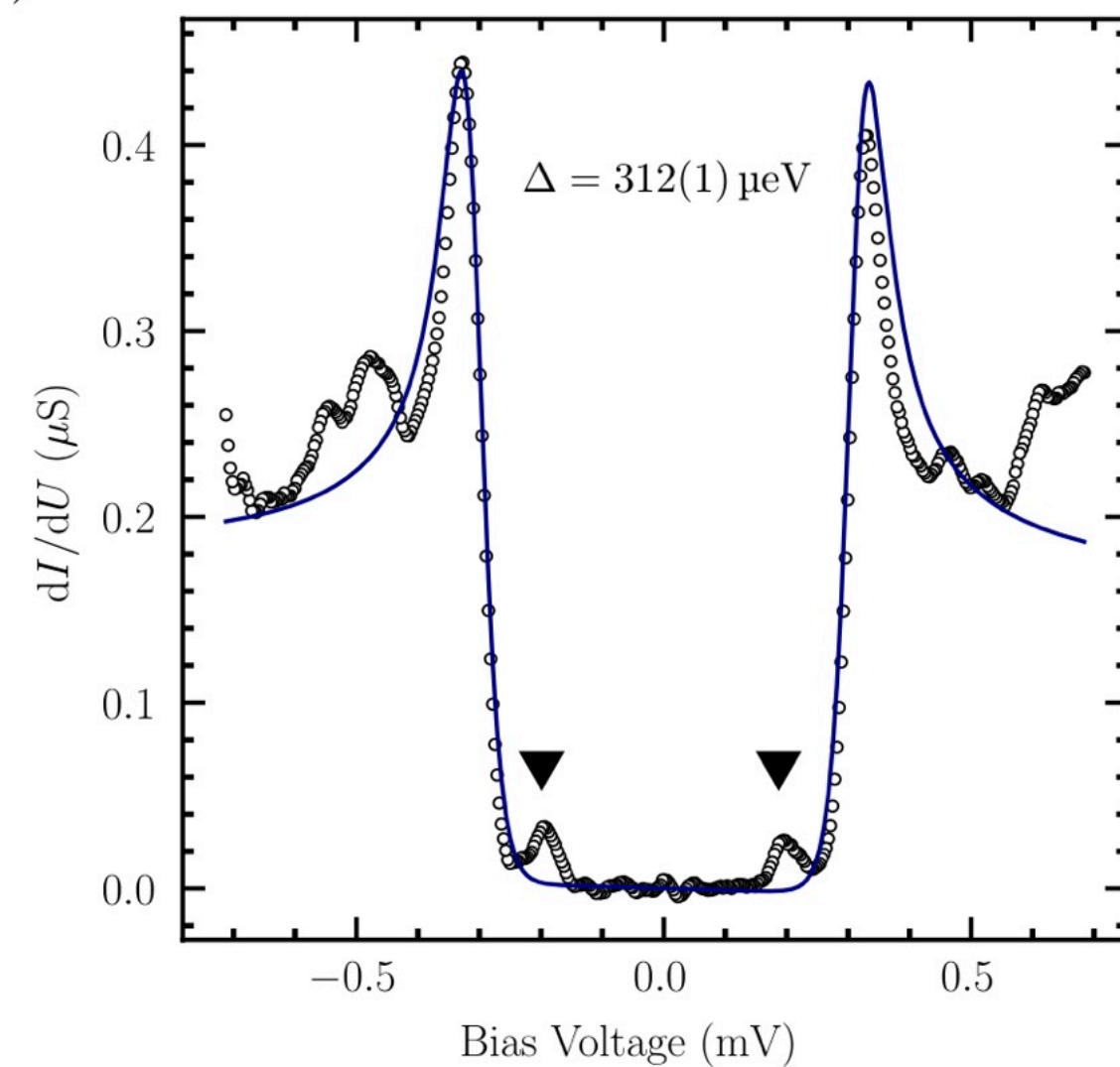


Yu-Shiba-Rusinov States and Long-lived Bosonic Excitations in Granular Aluminium

Fang Yang, Thomas Gozlini, Lukas Grünhaupt, Ioan Pop, Wulf Wulfhekel
 Karlsruhe Institute of Technology, Karlsruhe, Germany



Contributions

STM experiments & semi-classical calculations



Thomas Gozlinski



Fang Yang



Wulf Wulfhekel

grAI growth



Lukas Grünhaupt

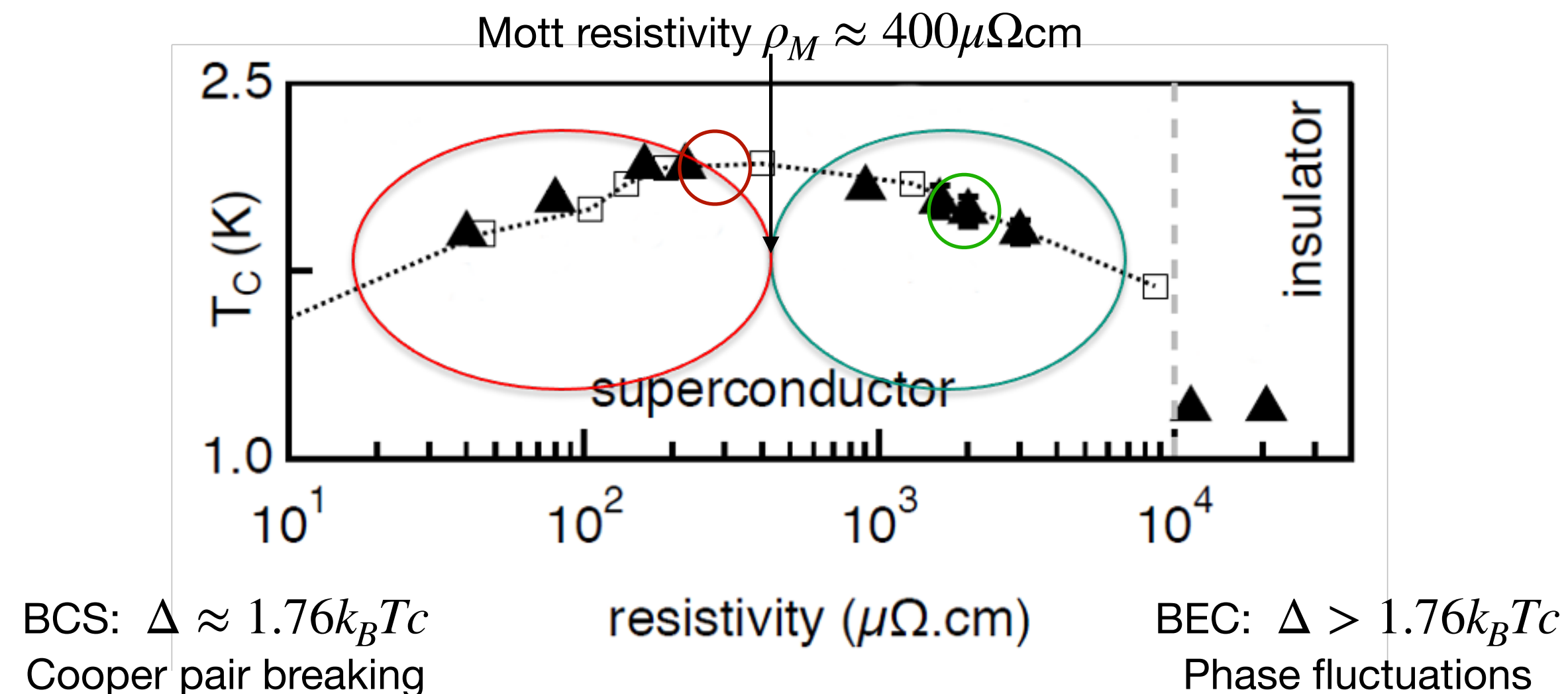


Ioan Pop

Microscopic view on grAl

- STM transport measurements with sub grain lateral resolution
- Test microscopic theory
- Superconducting gap and inhomogeneities
- Charging energies
- In gap states and decoherence
- Transfer of samples from growth chamber to UHV STM under UHV conditions

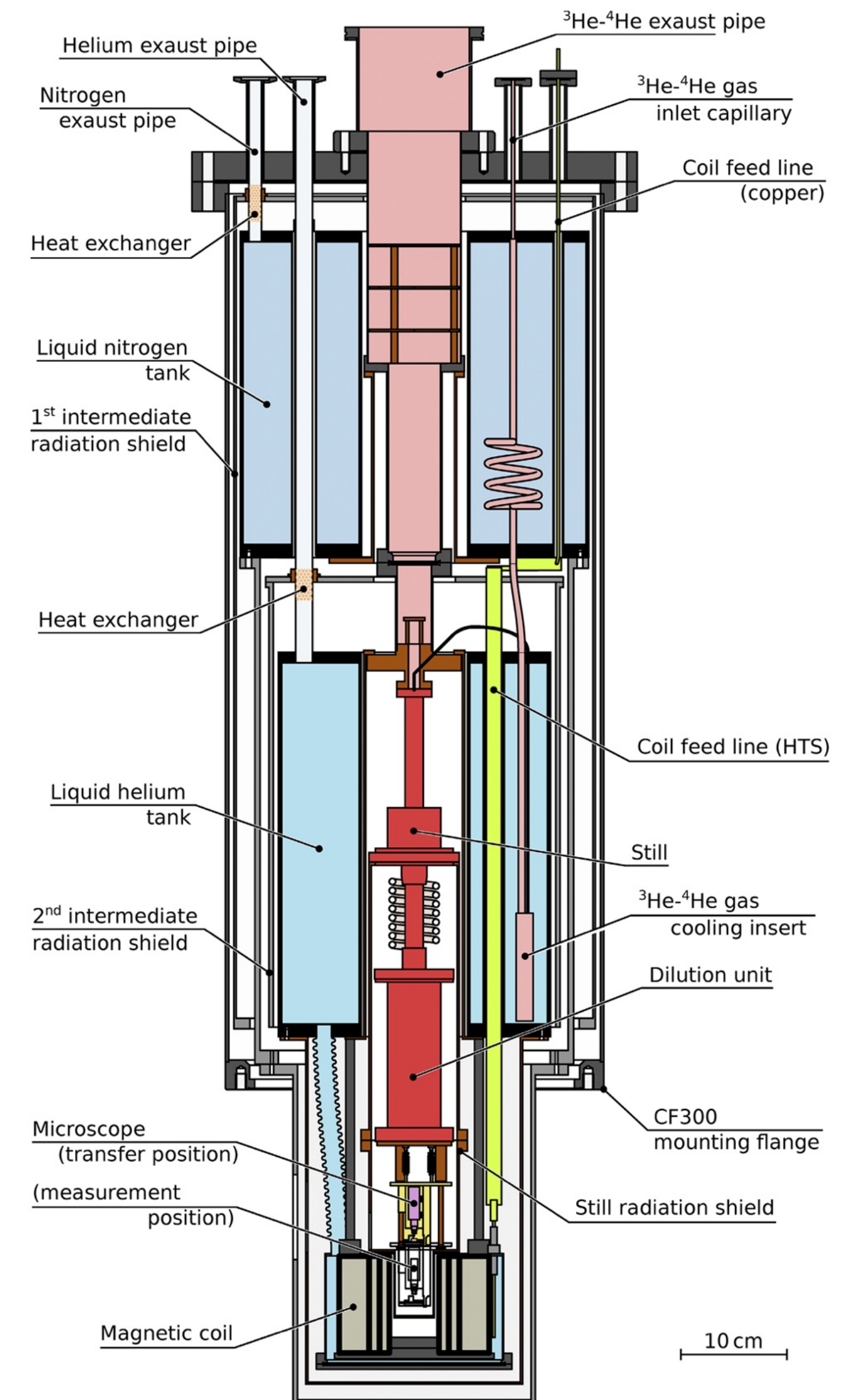
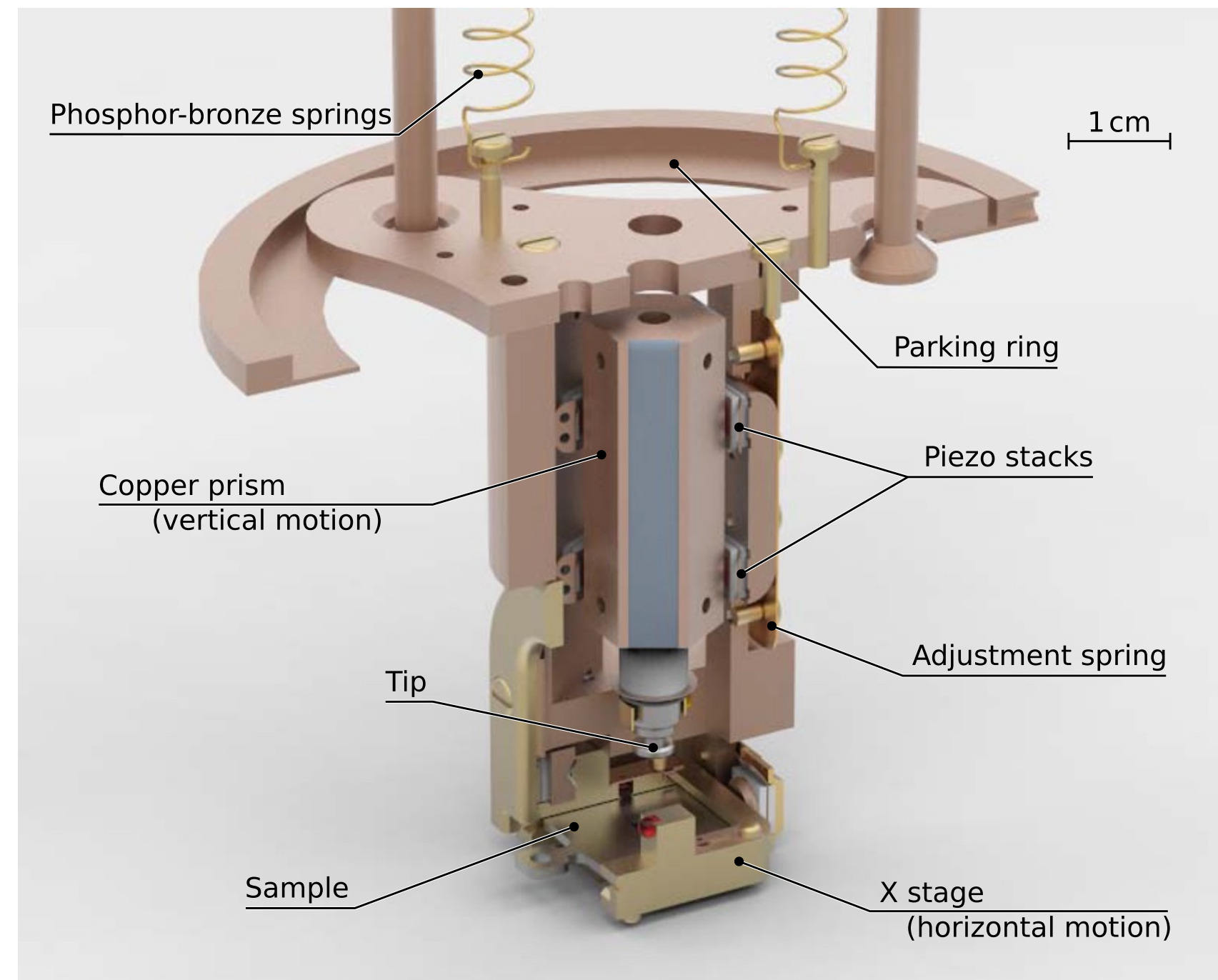
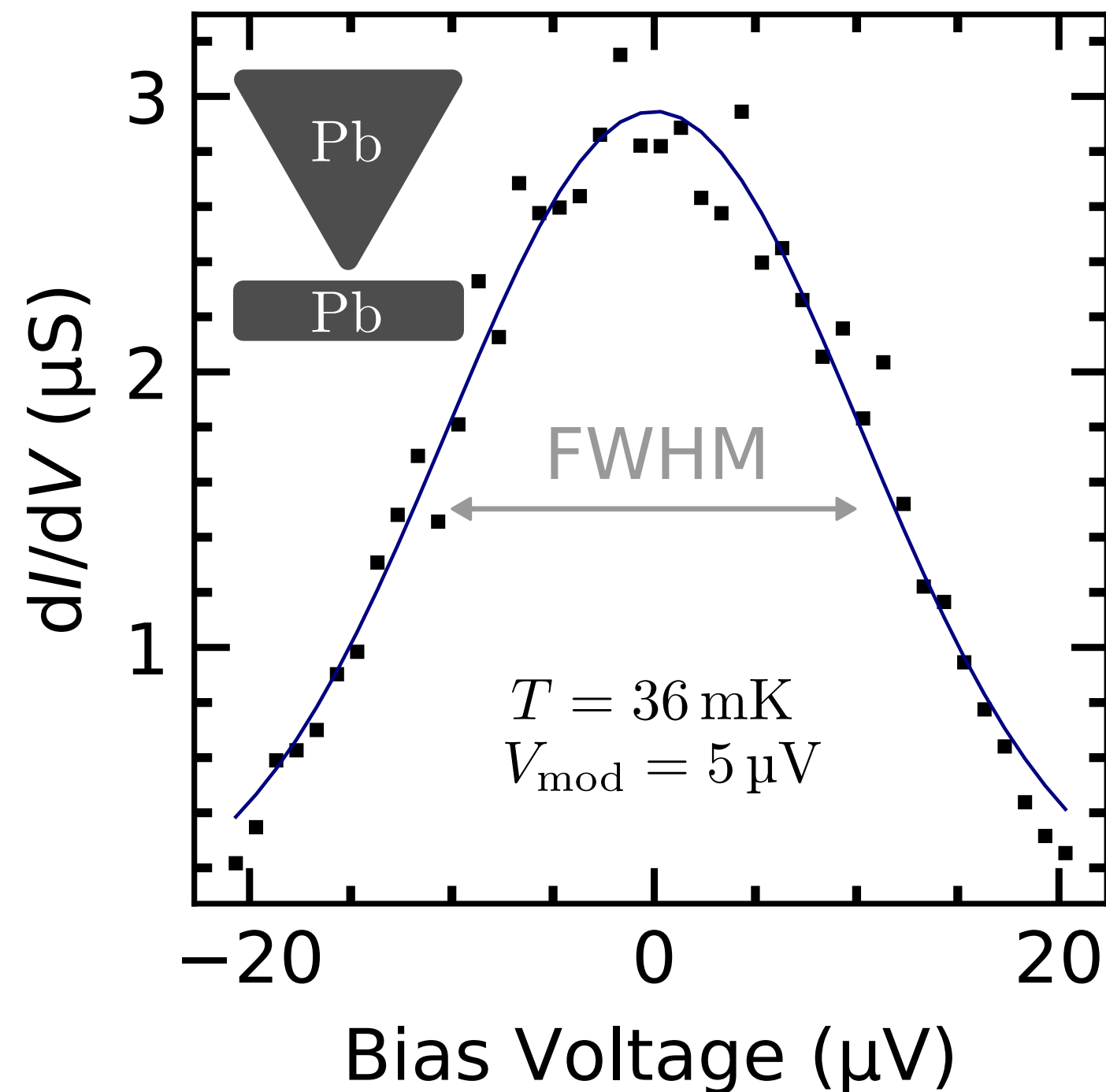
pure Al → oxygen poor (metallic) samples → oxygen rich samples



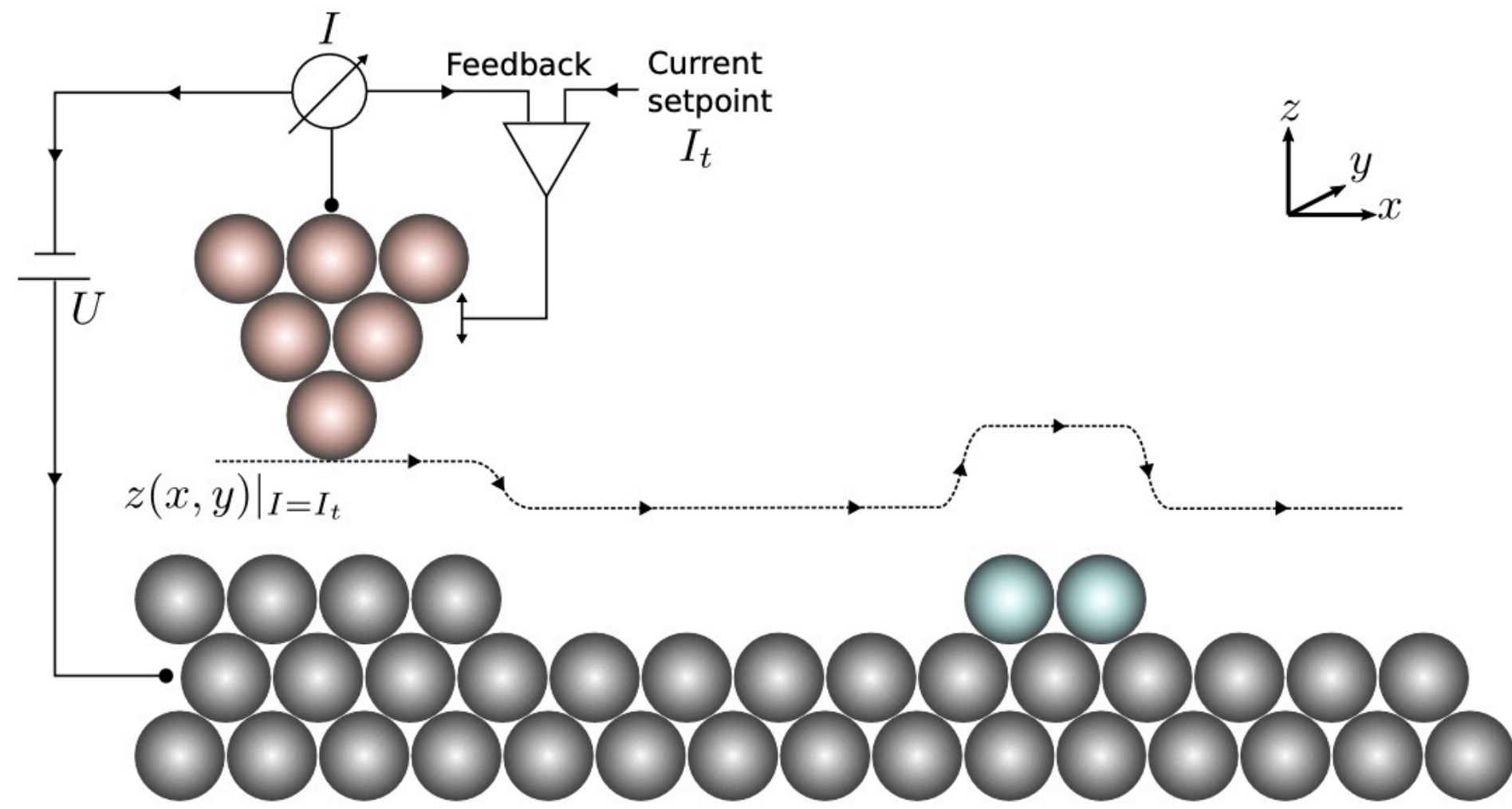
The experimental setup

- Compact and low cost 25 mK STM in UHV
- Magnetic field up to 6.5 T
- 69 mK electronic temperature
- 23 μeV resolution
- <2h sample turn-around

T. Balashov et al. Rev. Sci. Instr. 89, 113703 (2018)



What information do we get from the tunneling current?

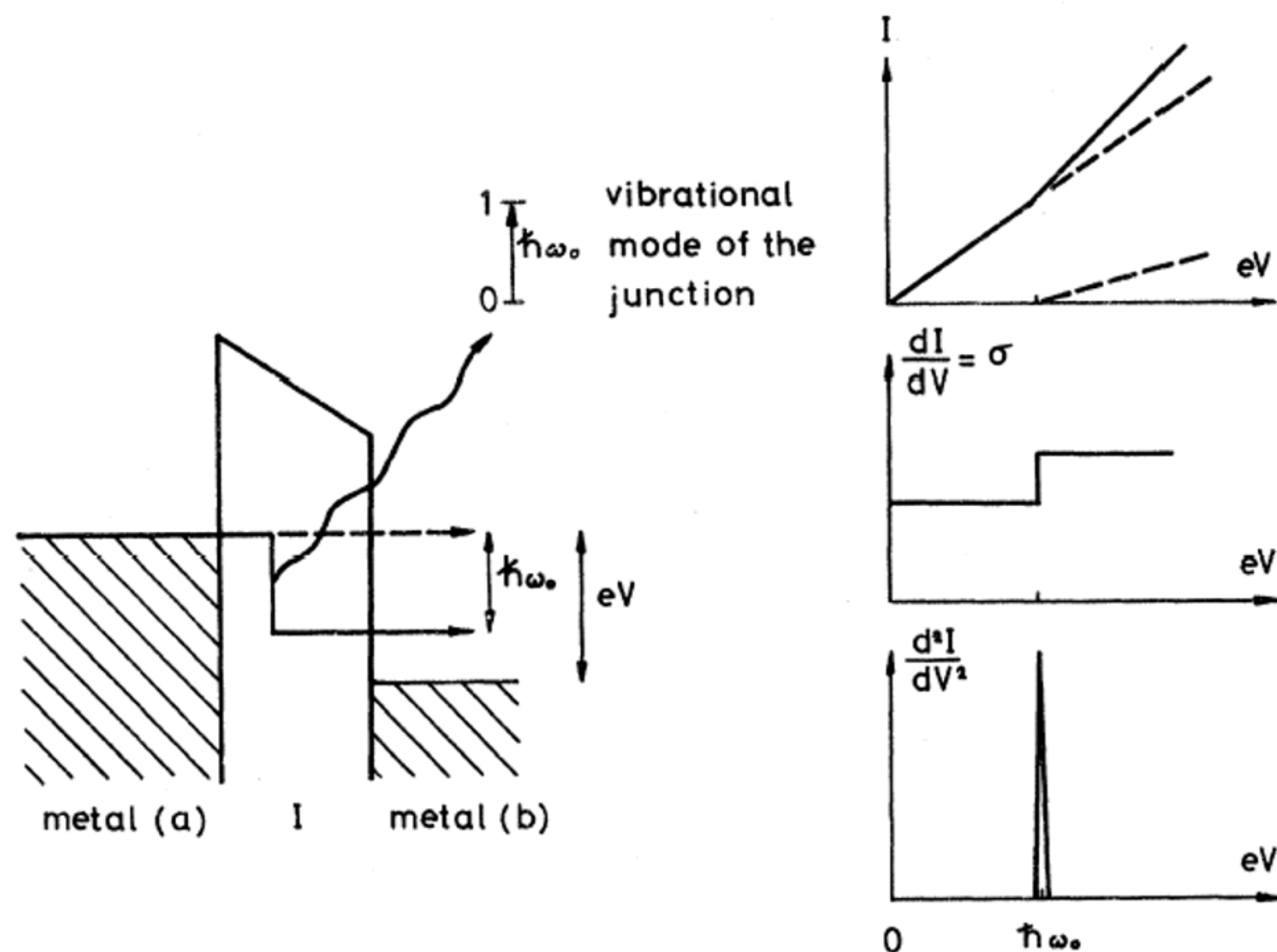


- For elastic tunneling with a normal tip, we obtain single particle LDOS

$$\sigma^{\text{el}}(U) = \frac{dI^{\text{el}}(U)}{dU} = -\sigma_0 \int_{-\infty}^{\infty} d\epsilon \tilde{\nu}_s(\epsilon) n'_F(\epsilon - eU)$$

- For inelastic tunneling, final state of electron and excited boson share total energy and momentum of tunneling electron

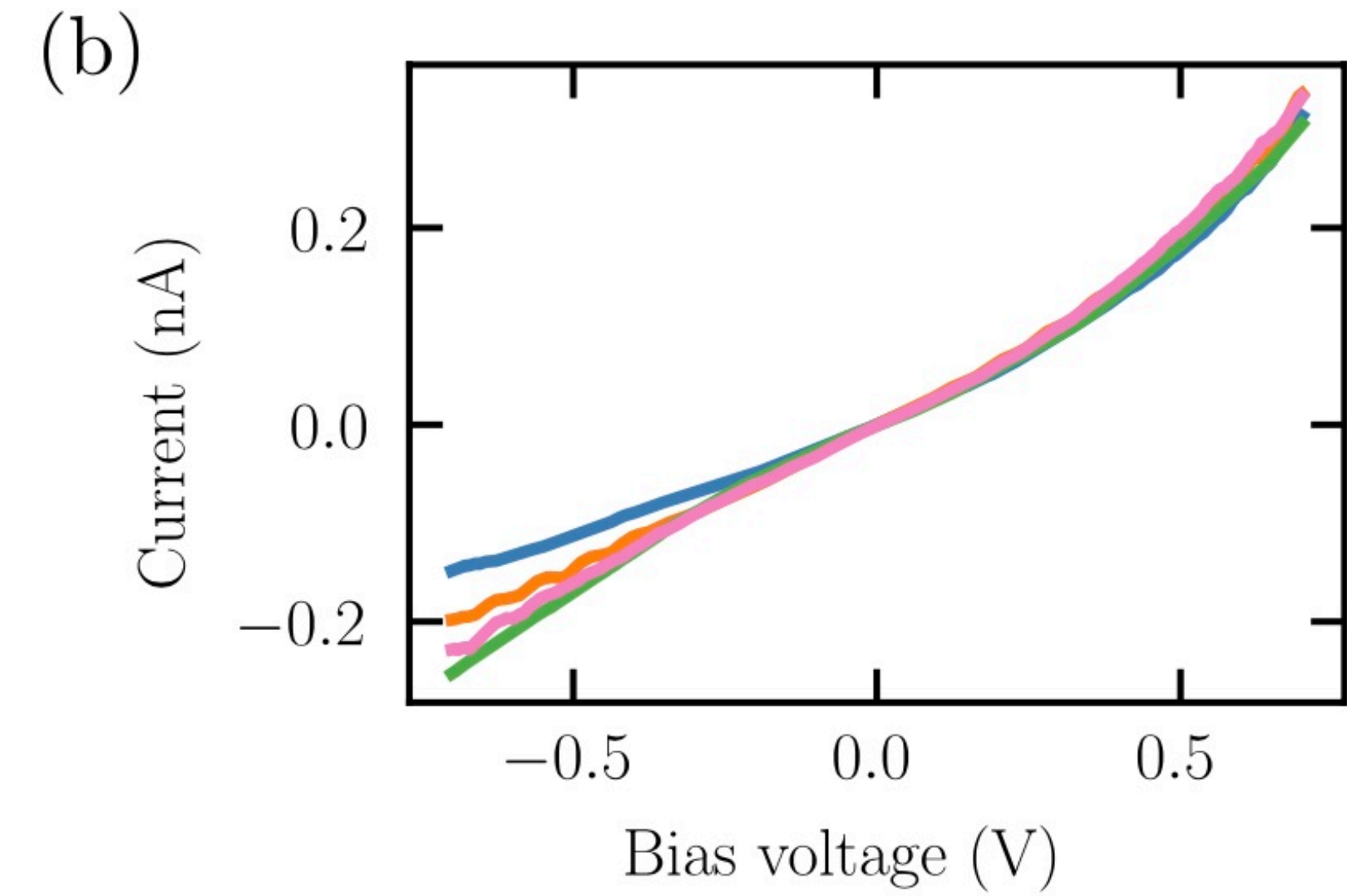
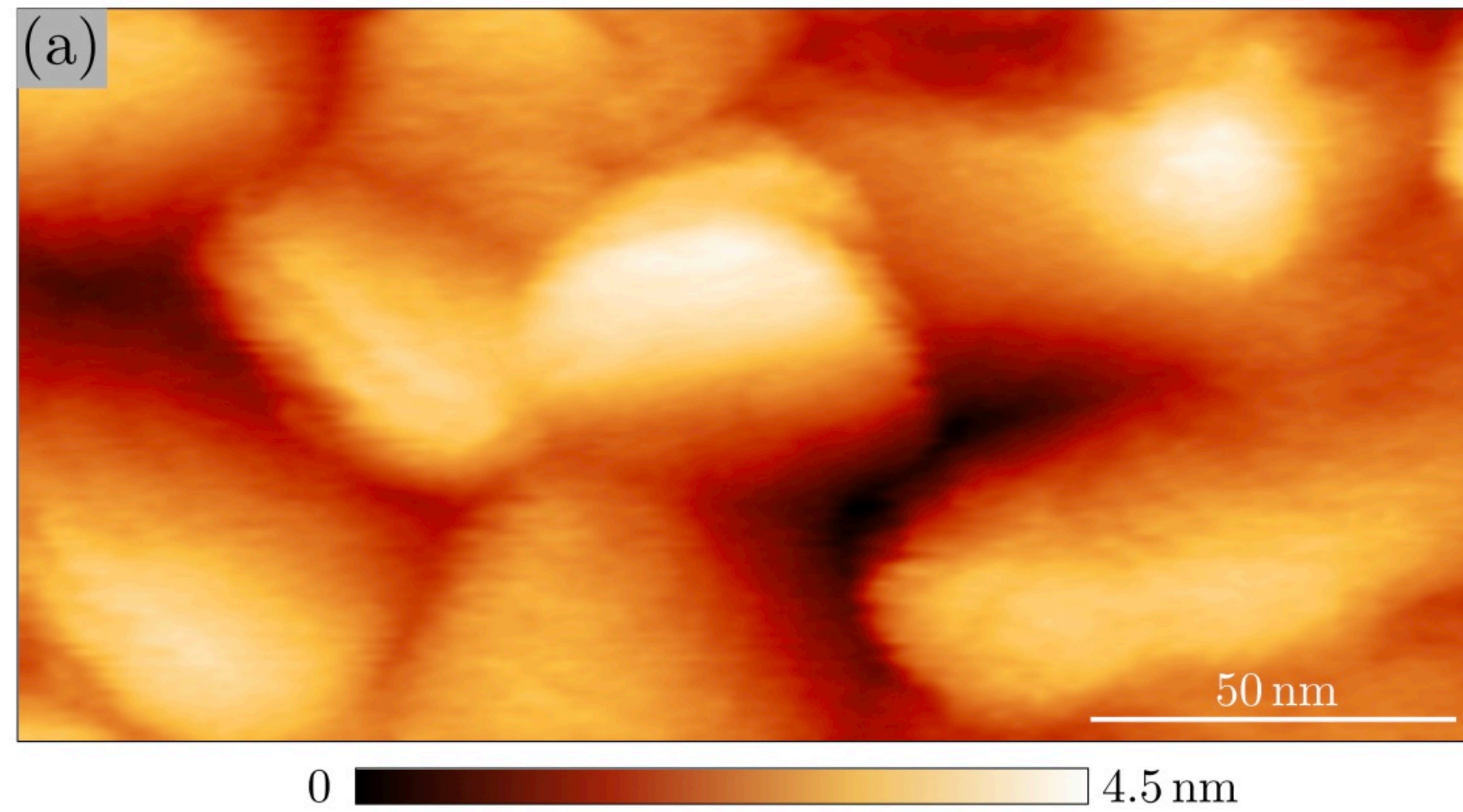
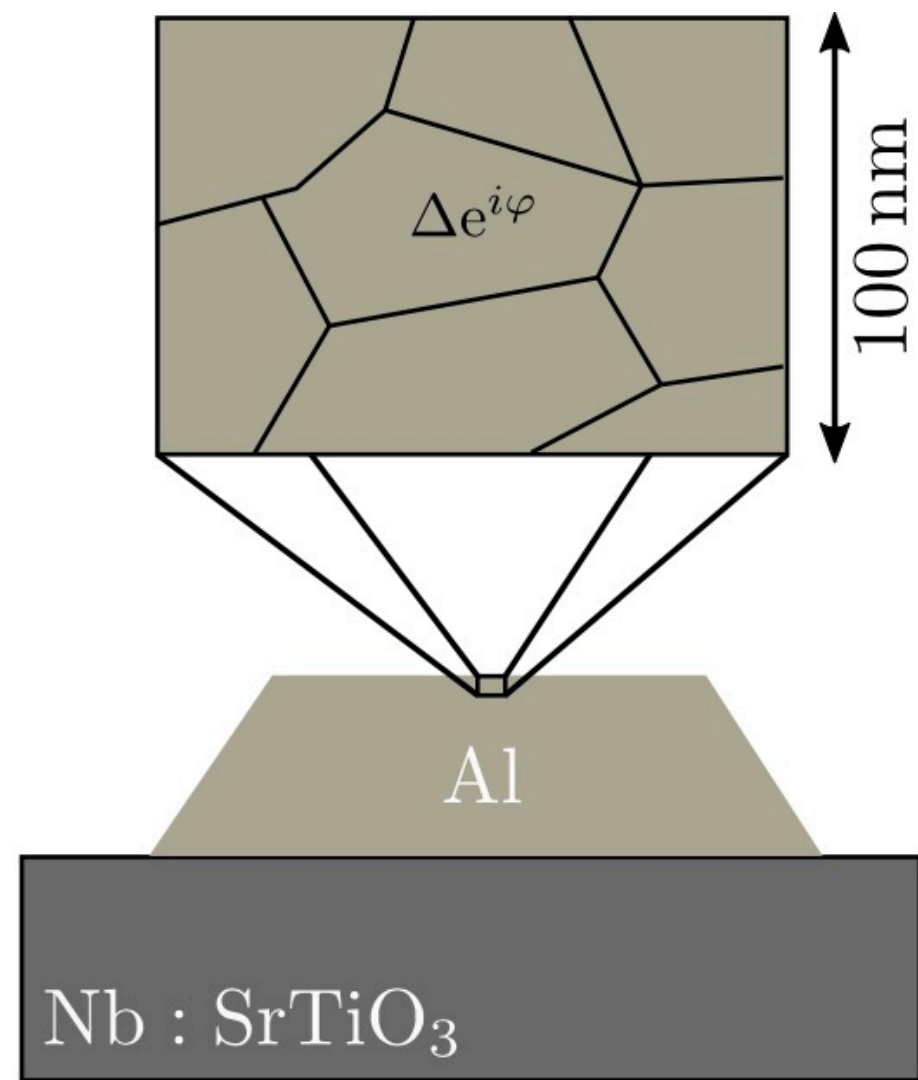
$$\sigma^{\text{inel}}(U > 0) \xrightarrow{T \rightarrow 0} \frac{\sigma_0}{\nu_s^F D^2} \int_0^{eU} d\omega \alpha^2 F(\omega) \tilde{\nu}_s(eU - \omega)$$



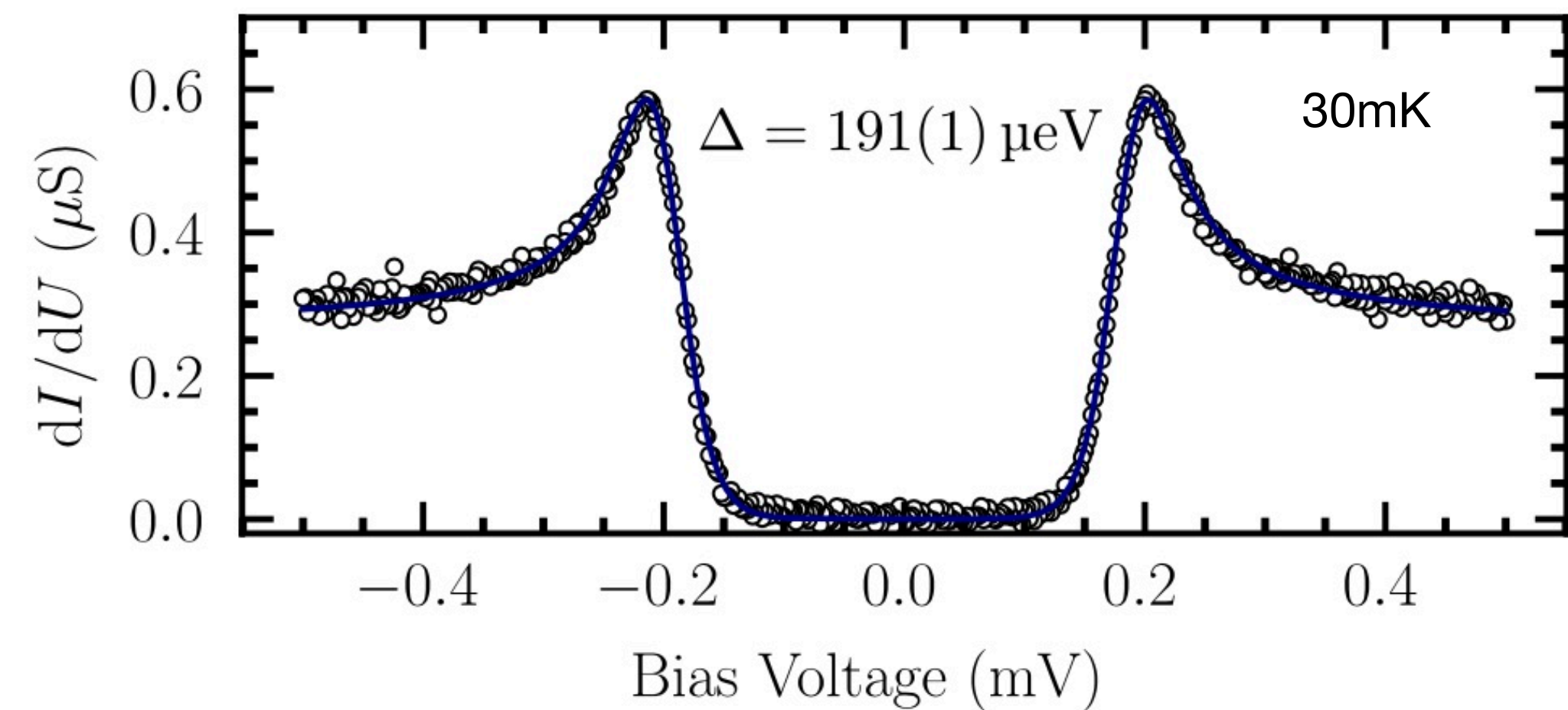
- When sample is superconducting, we see excitations at a bias of $eV = \Delta + \omega$

- Full transport should consider addition/subtraction spectrum and path of current
Landauer Büttiker

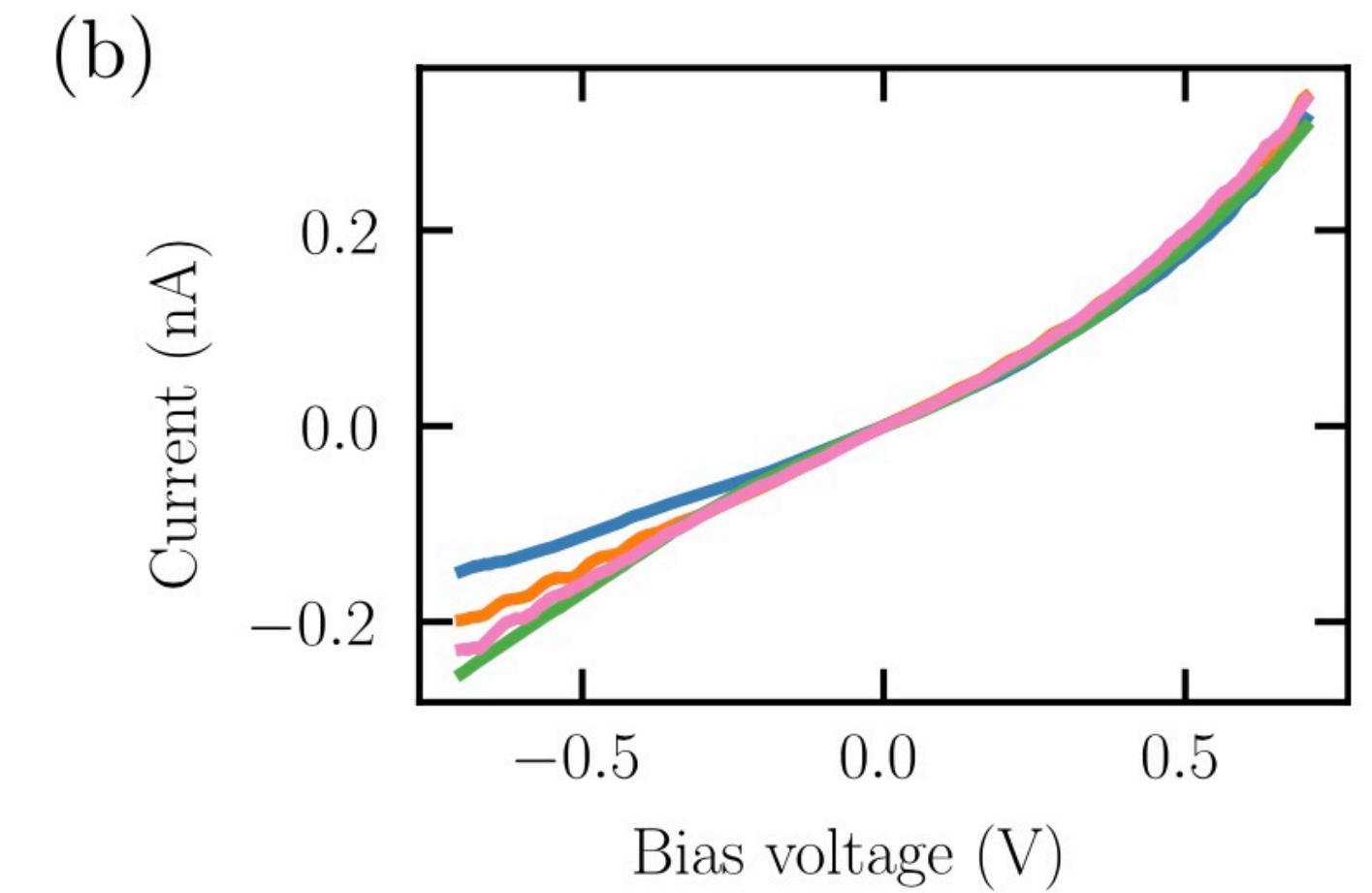
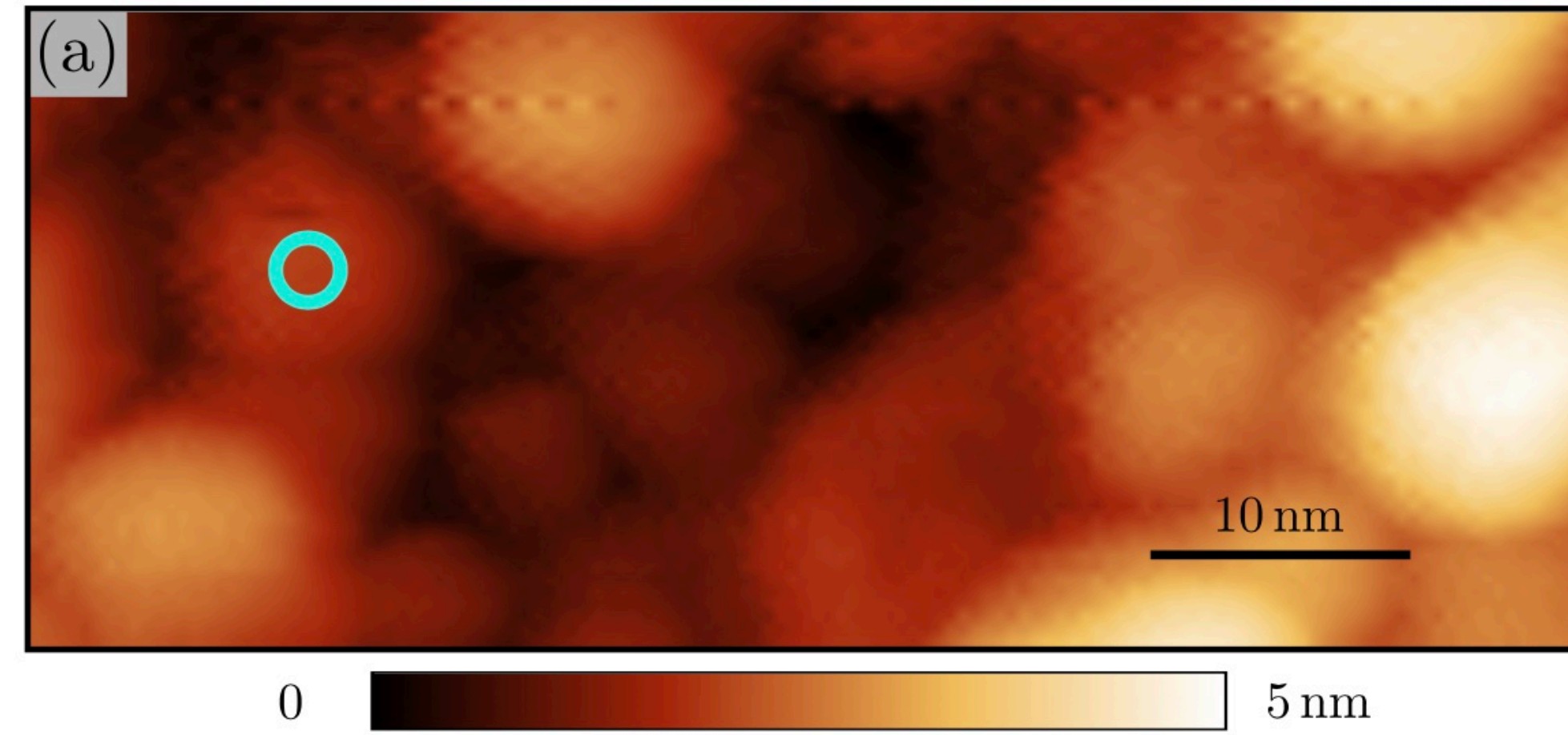
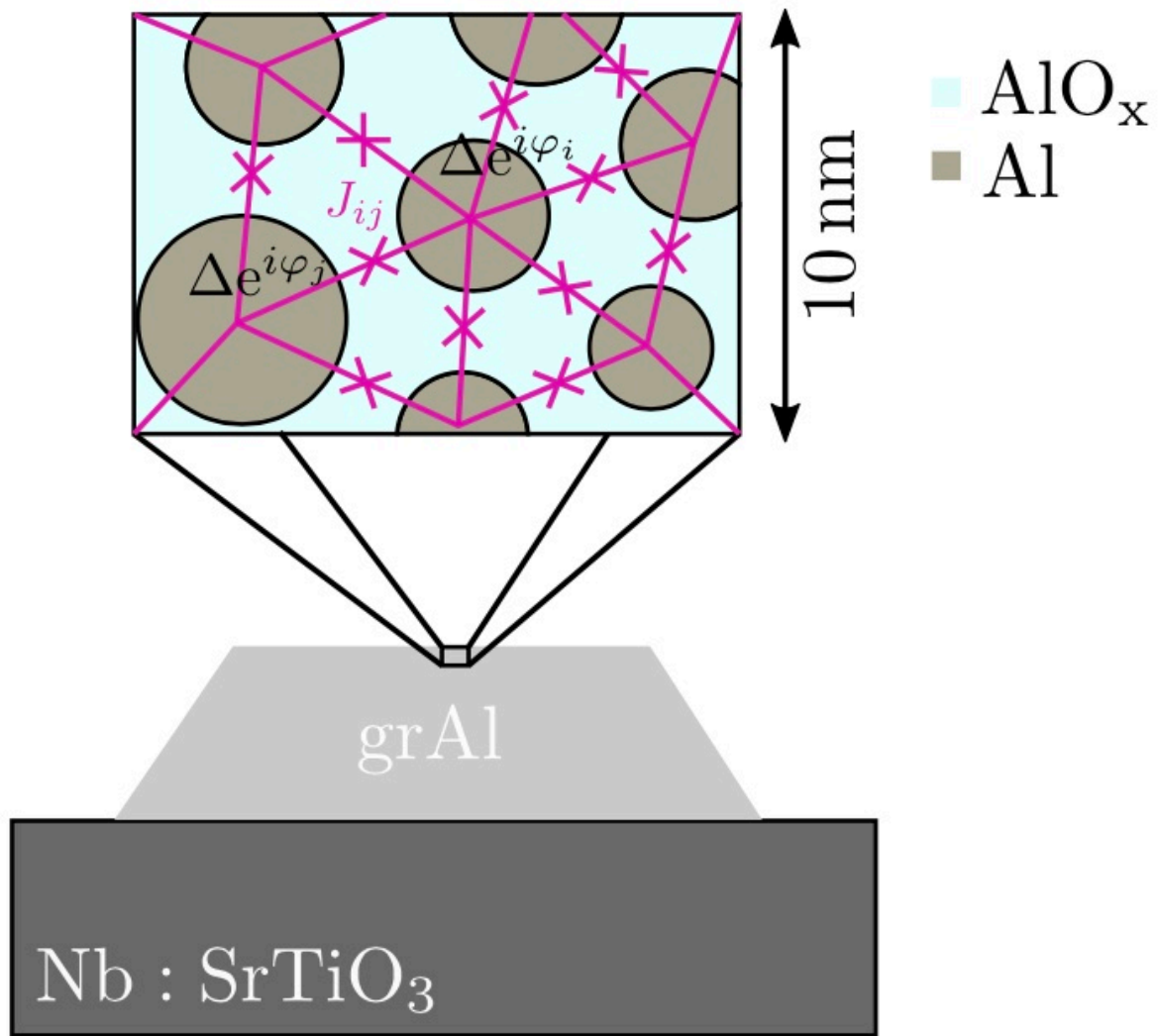
Pure Al



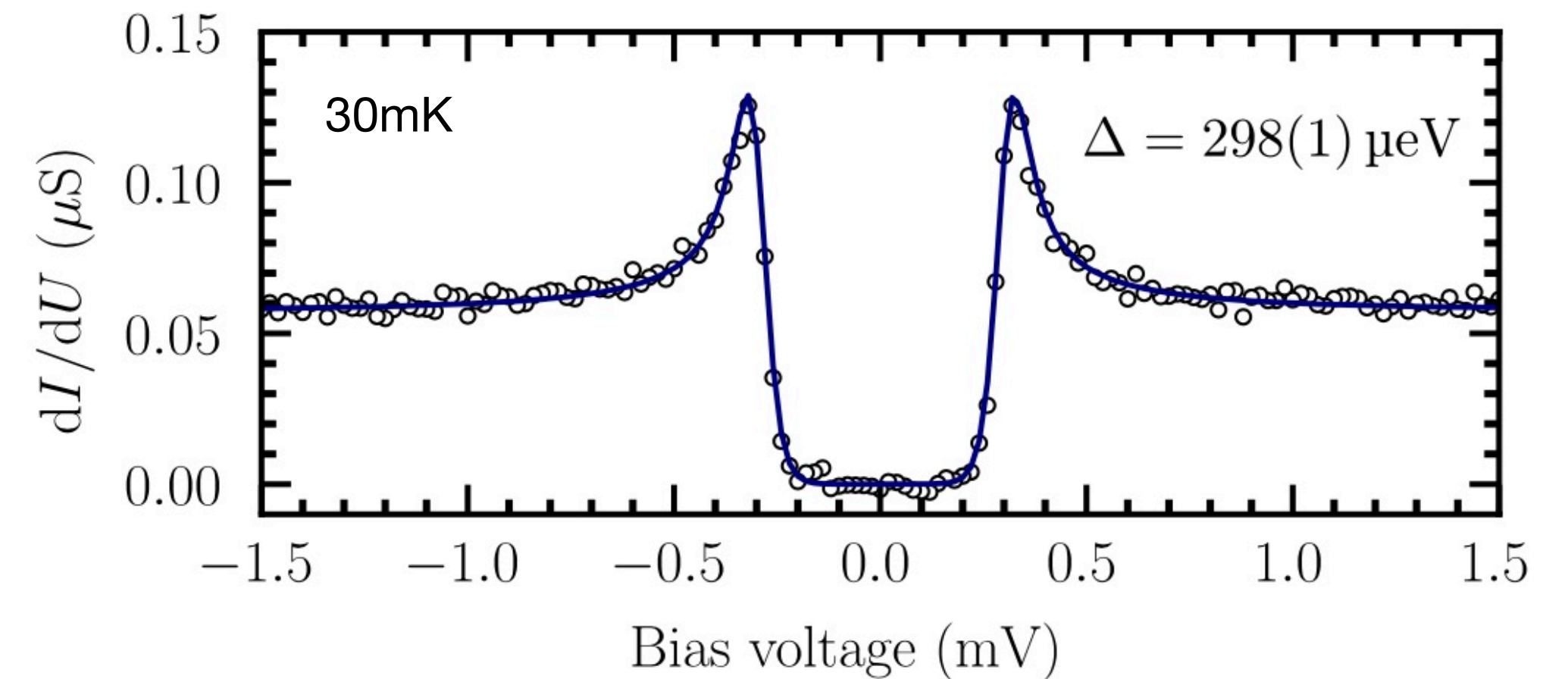
- Efficient Al diffusion leads to large grains
- Metallic I(V) curve
- Gap is close to literature value of Al films ($200\mu\text{eV}$)
- Gap is homogeneous and no in-gap states found
- Surface is clean



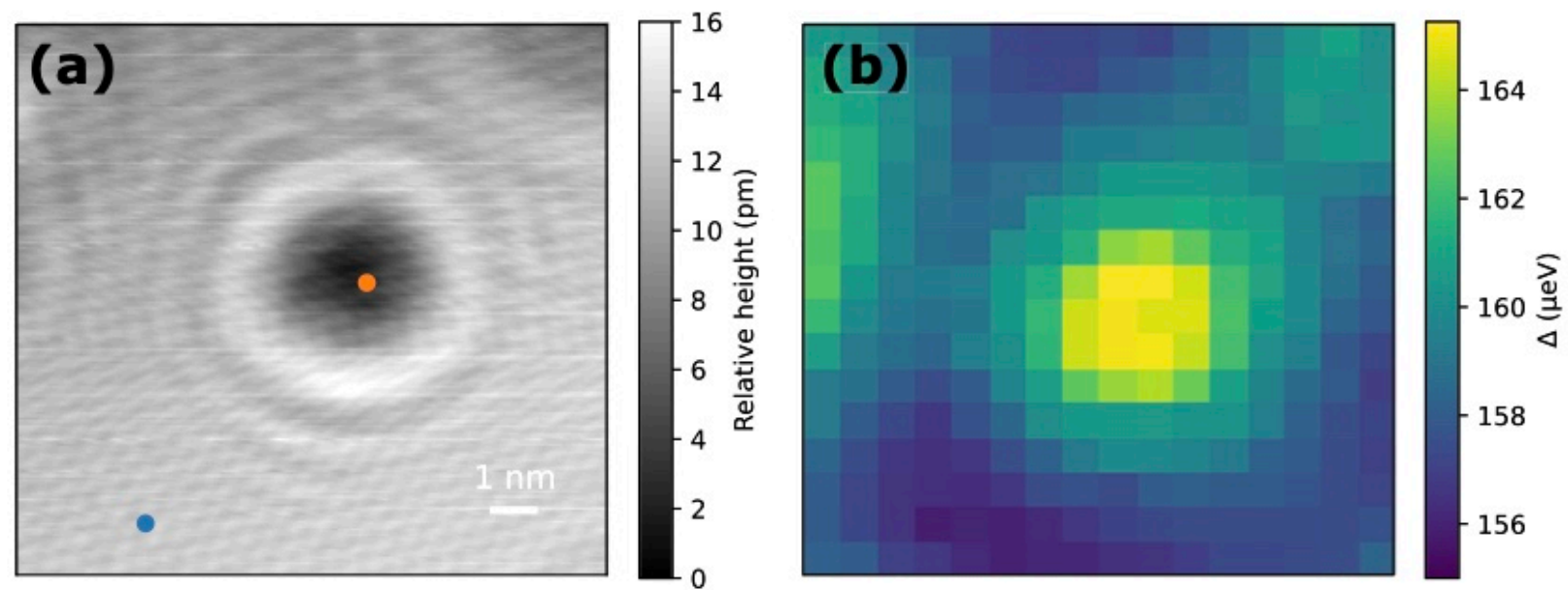
Oxygen poor samples ($300 \mu\Omega\text{cm}$)



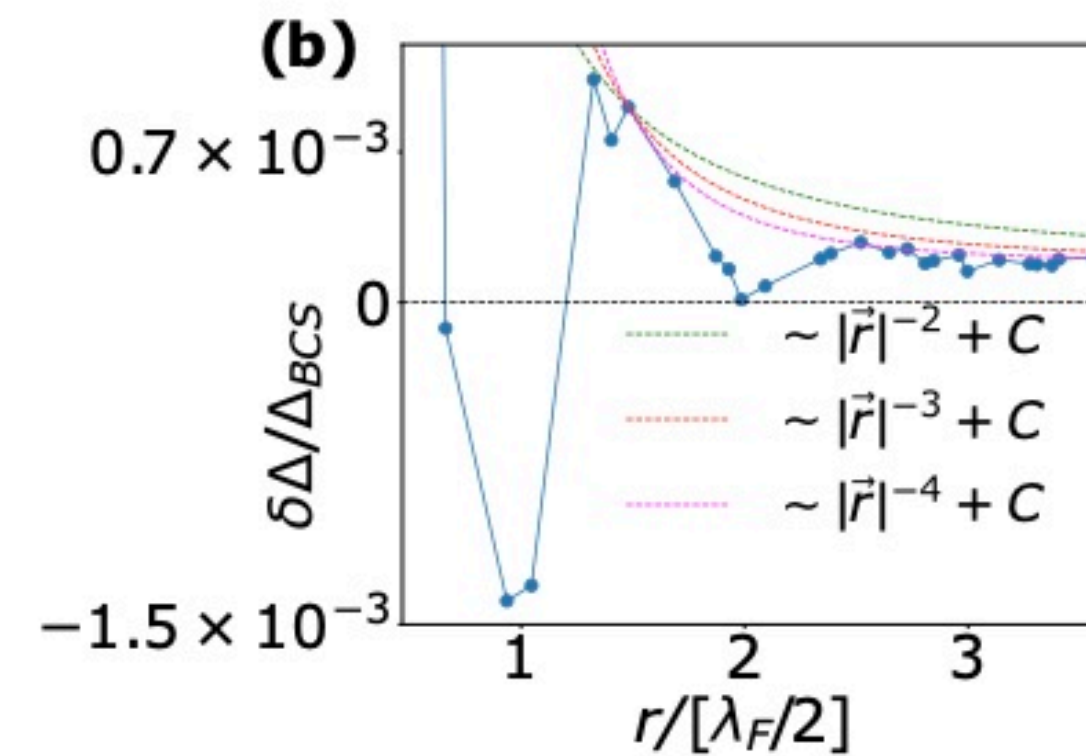
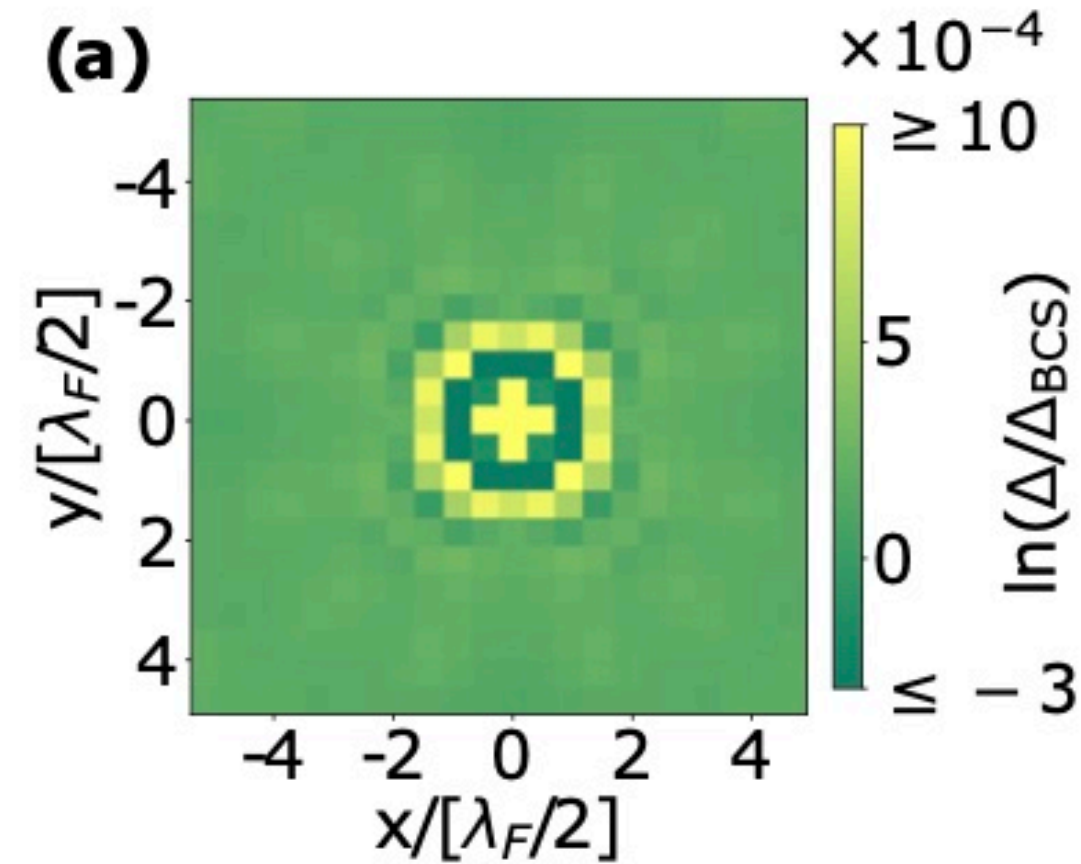
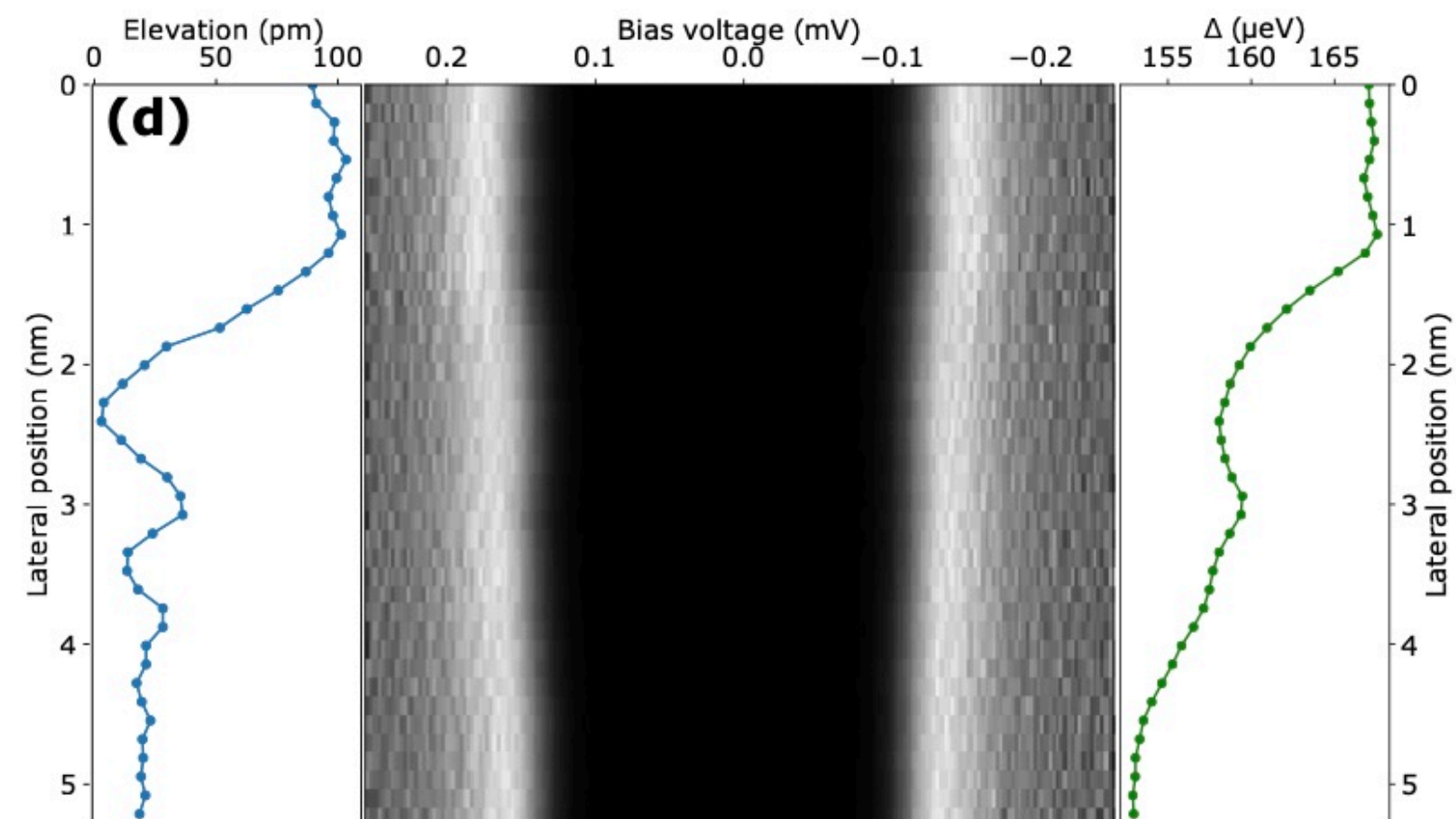
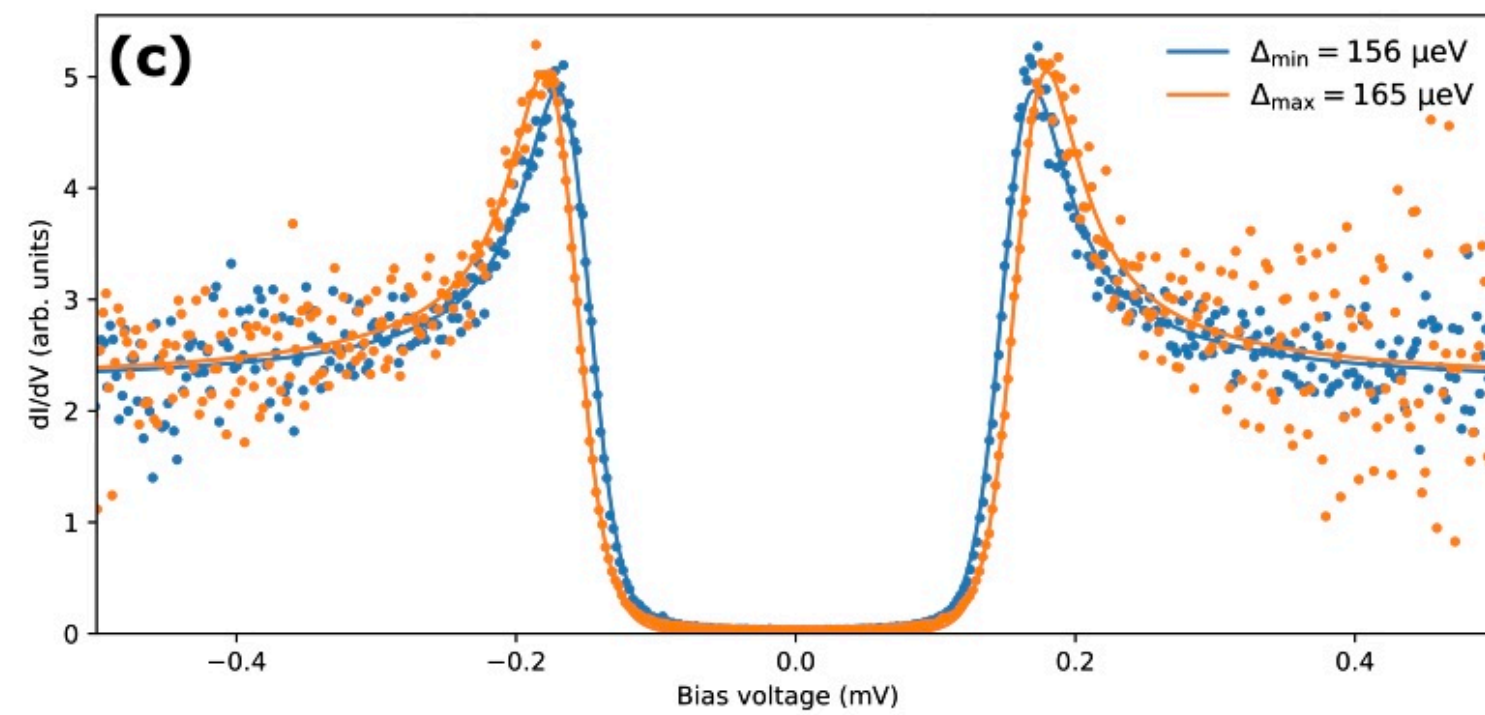
- Al diffusion hampered by AlO_x with grains 5-10 nm
- Metallic I(V) curve
- Gap is much larger than pure Al
- Gap is homogeneous and no in-gap states found



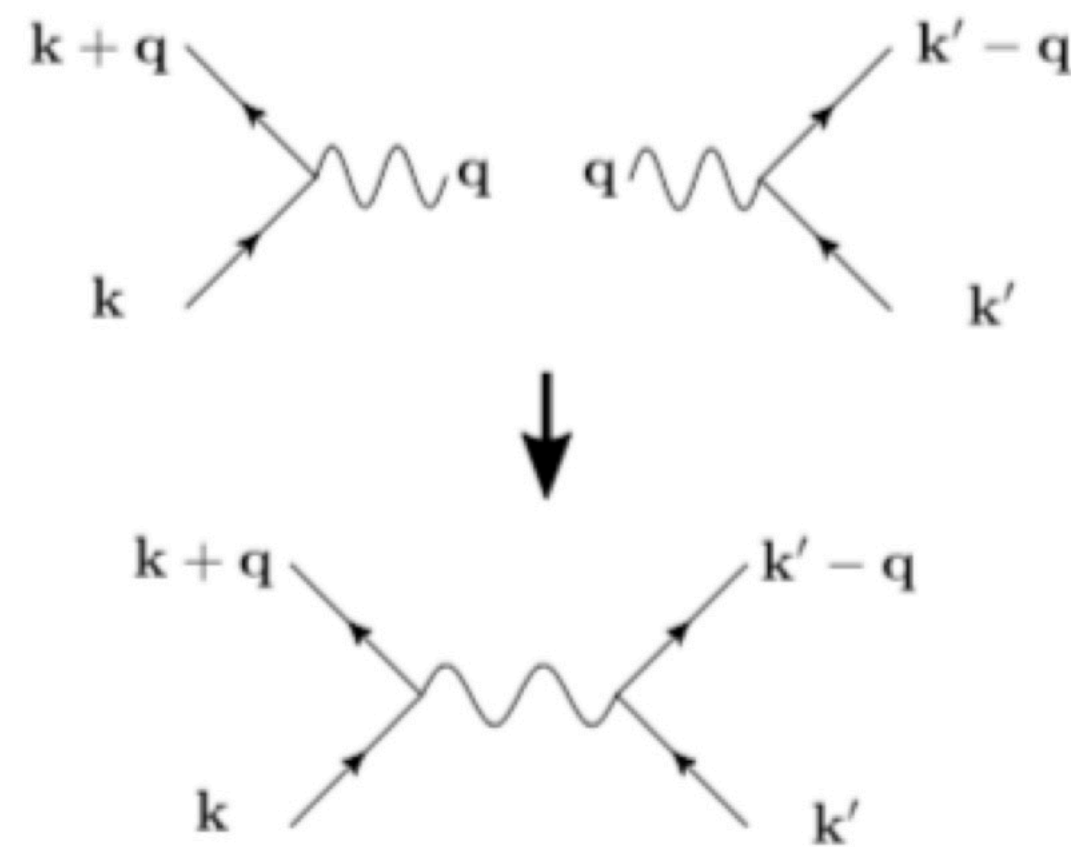
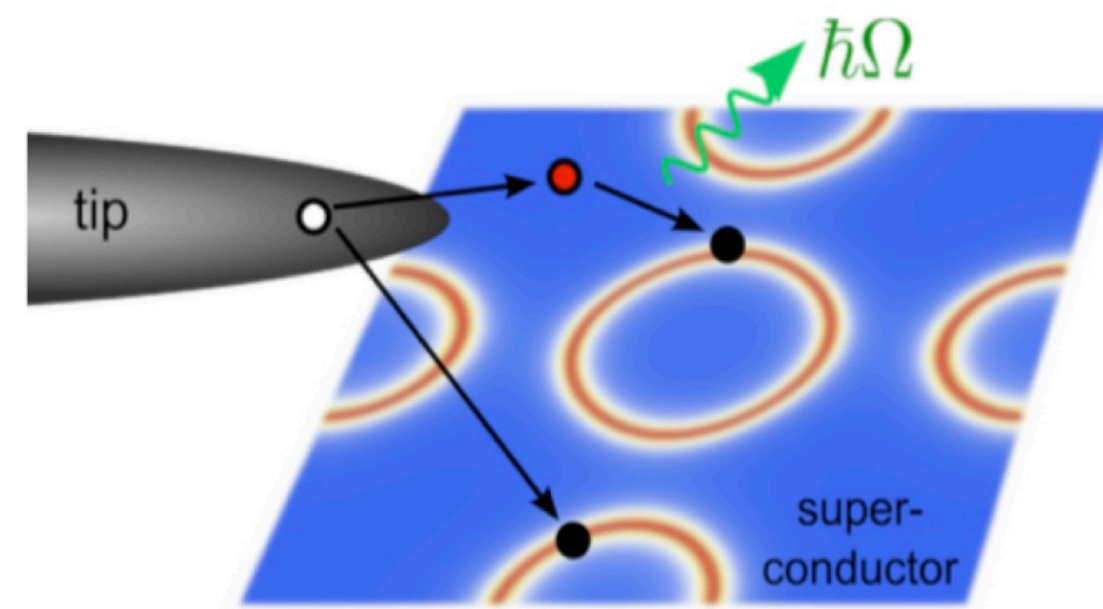
Increase of the gap by disorder



- Single implanted Ar atom in Al(111)
- Local increase of gap by 7%
- Damped Friedel oscillations in gap
- Reproduced in model calculations

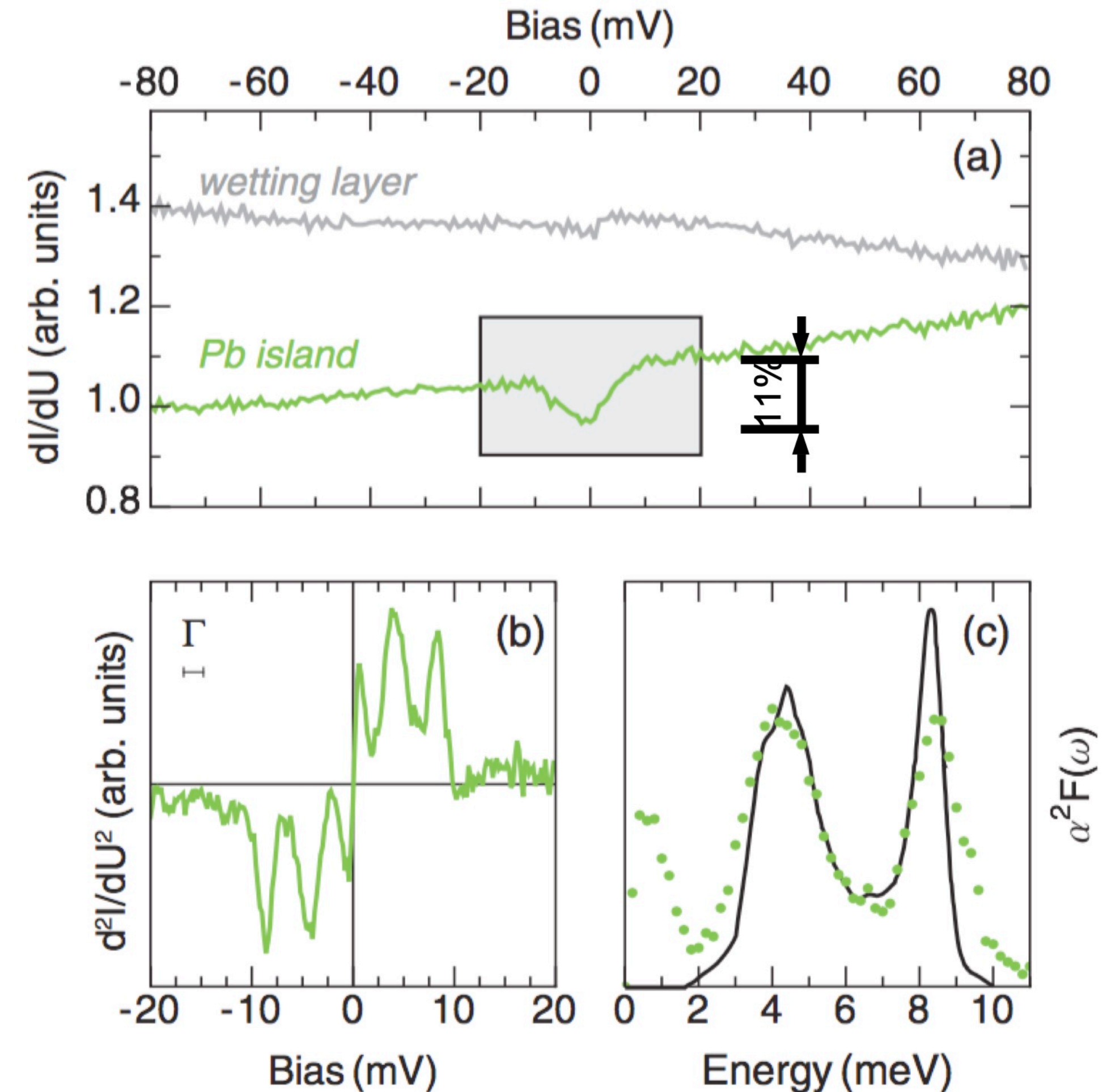


Detecting phonons with ITS

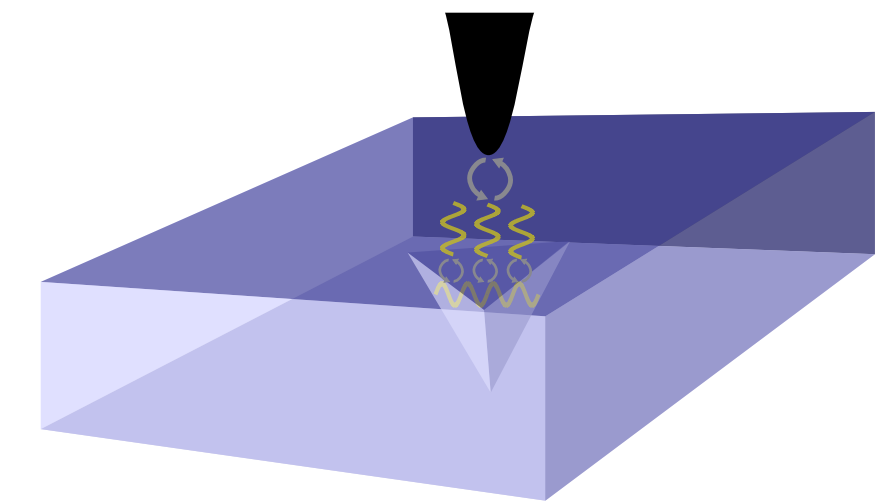
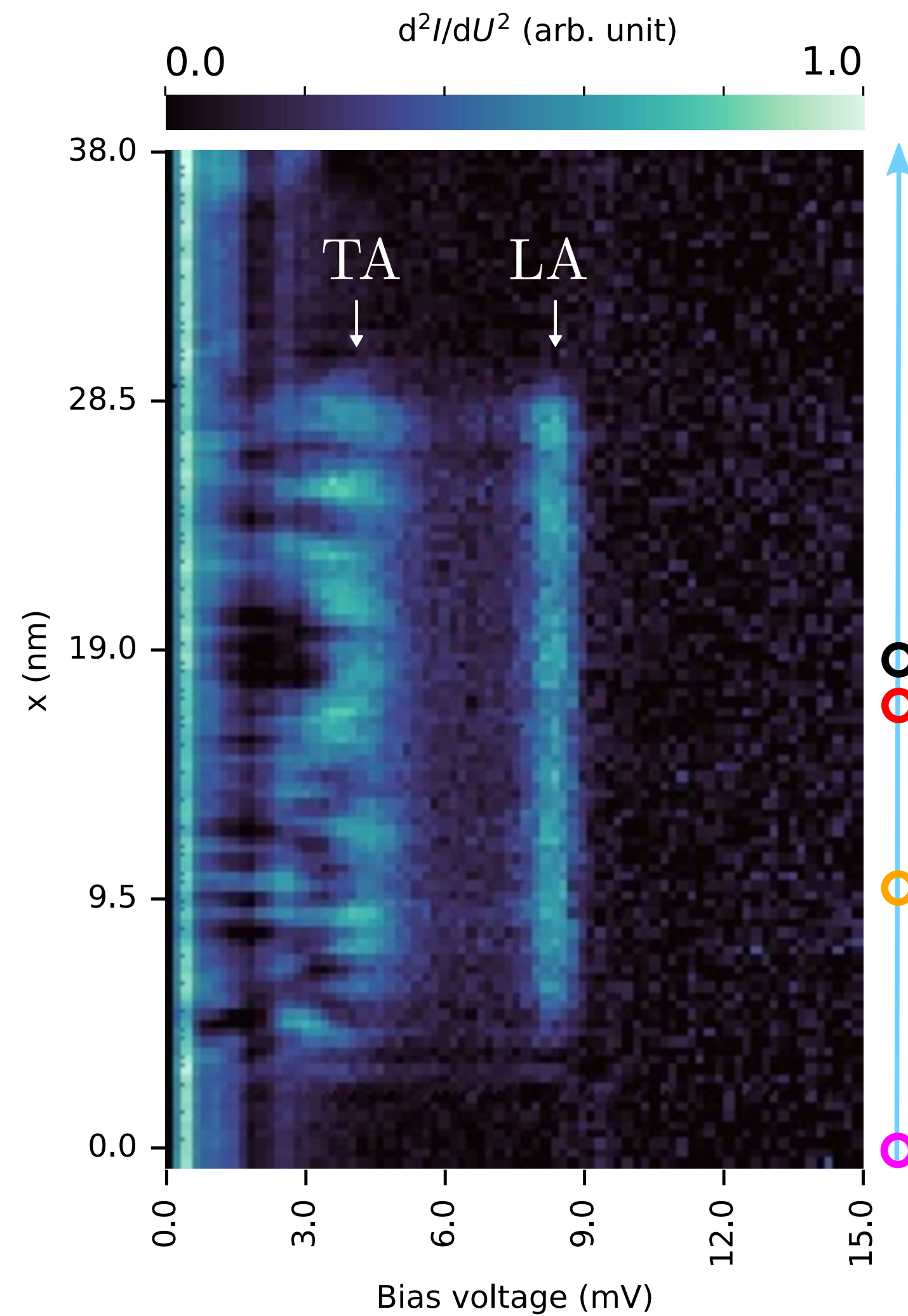
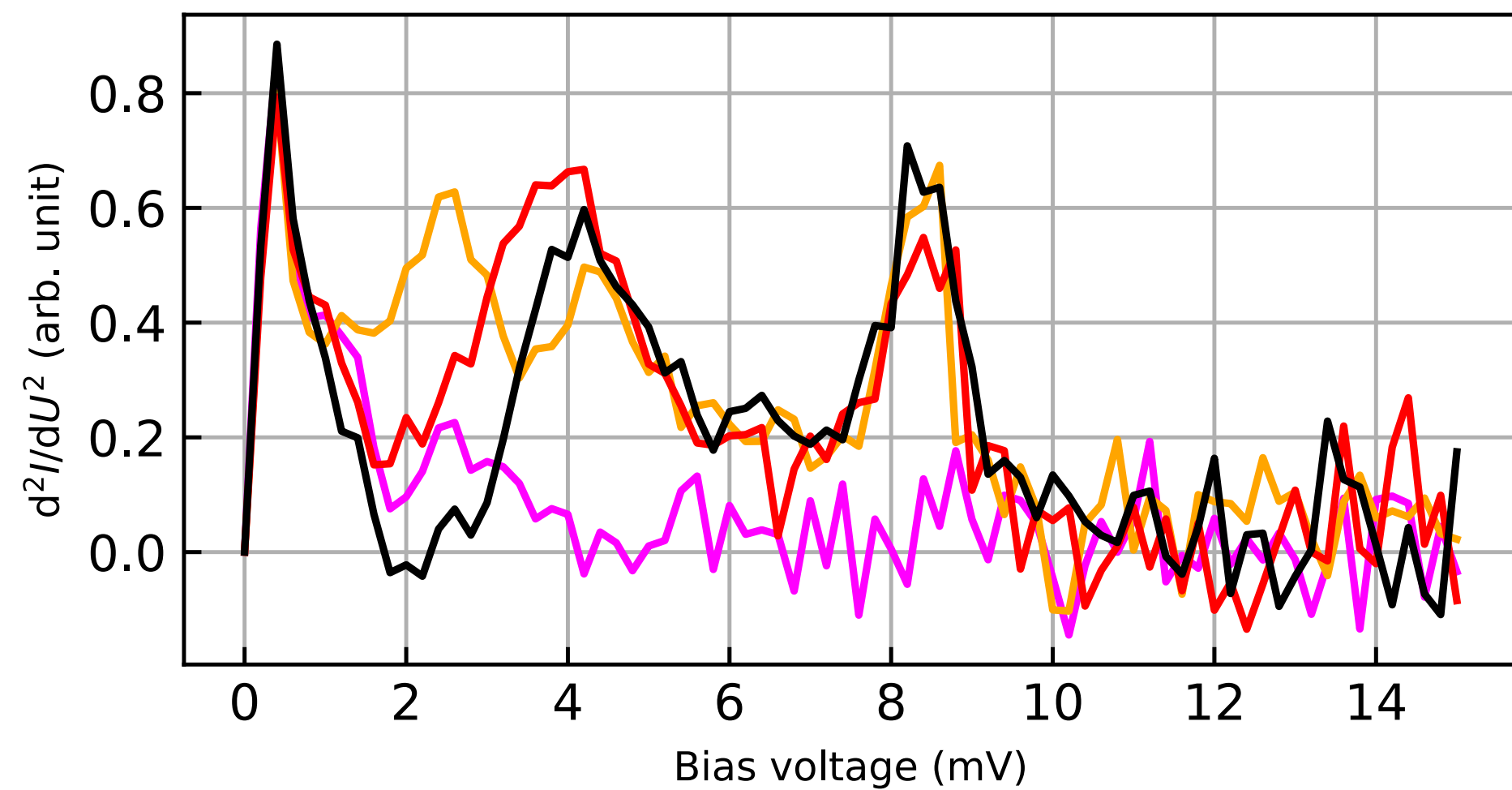
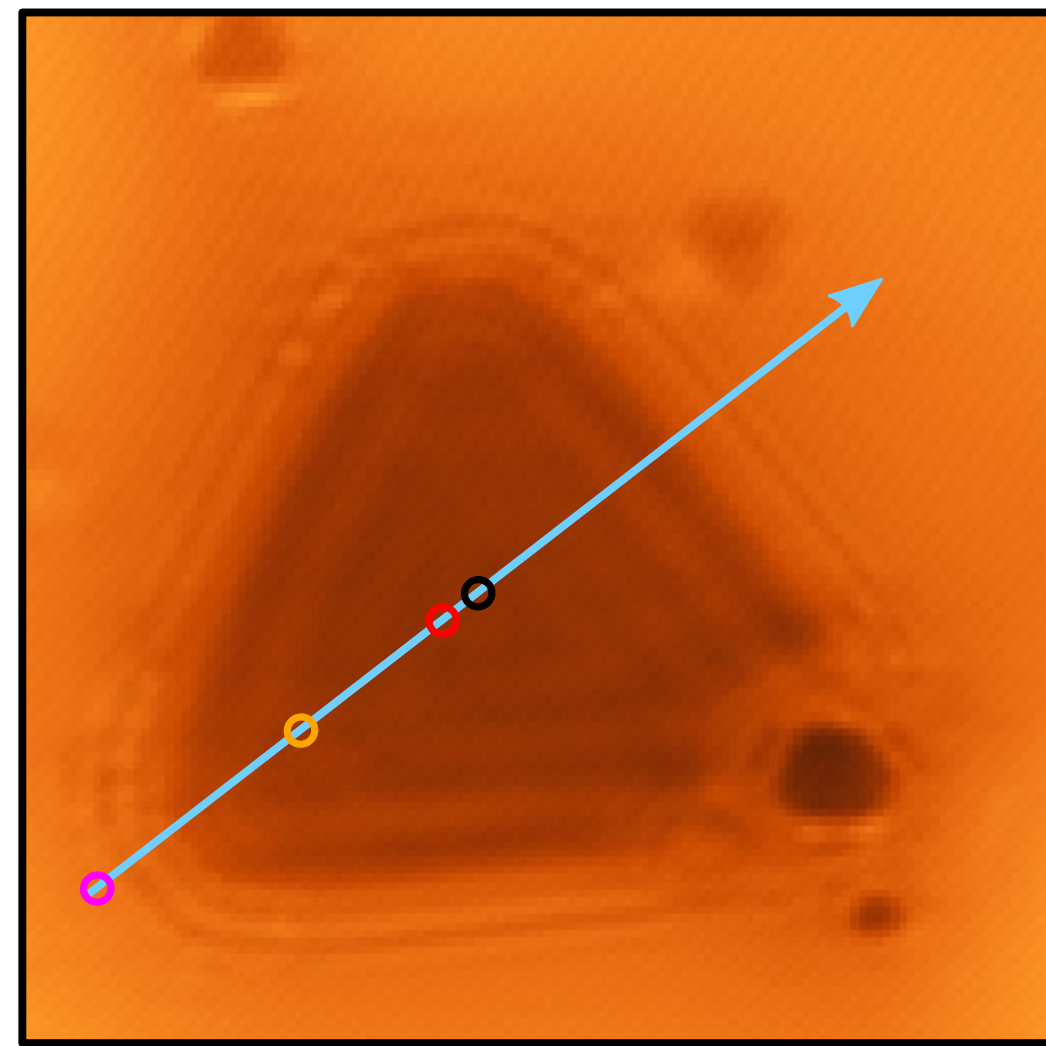


M. Schackert et al., PRL 114, 42002 & J. Jandke et al., PRB R060505

- Inelastic tunneling spectroscopy (ITS): $\frac{\partial^2 I}{\partial U^2} \propto \alpha^2 F(\omega)$
- Initial tip state near $k_{\parallel}^e = 0, E$: final on shell sample state: $k_{\parallel}^e = -q_{\parallel}, E - \omega, q_{\parallel}^p, \omega$
- Phase space for inelastic scattering restricted by momentum conservation
- Can be enlarged by breaking translational symmetry

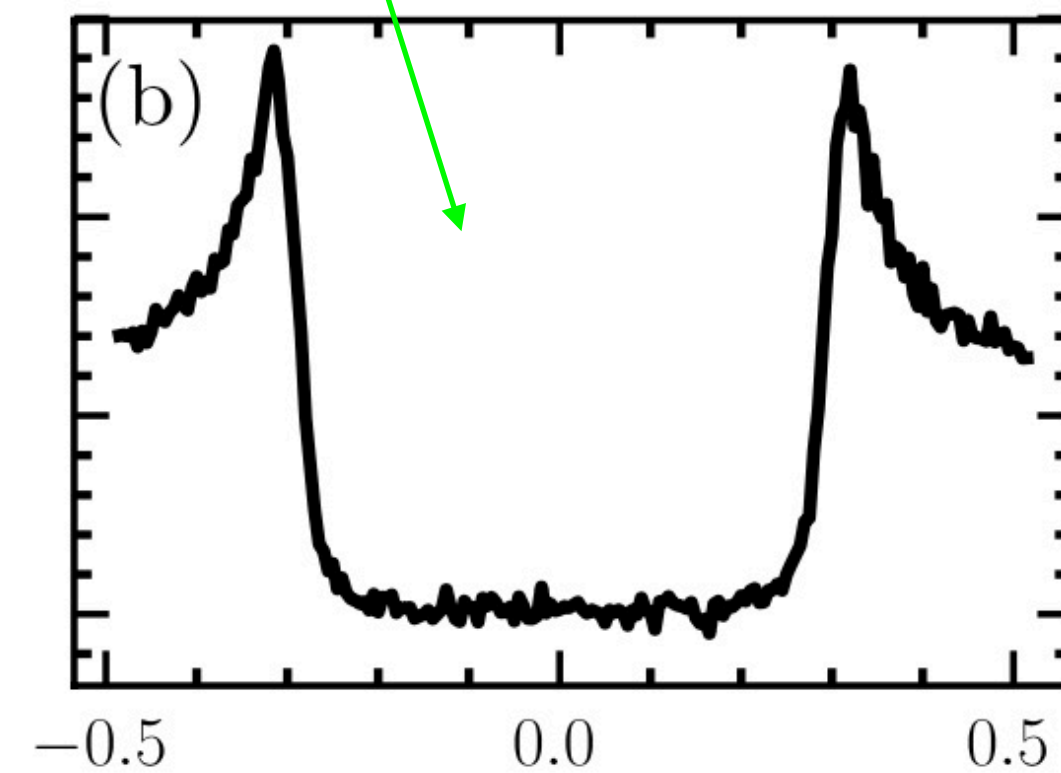
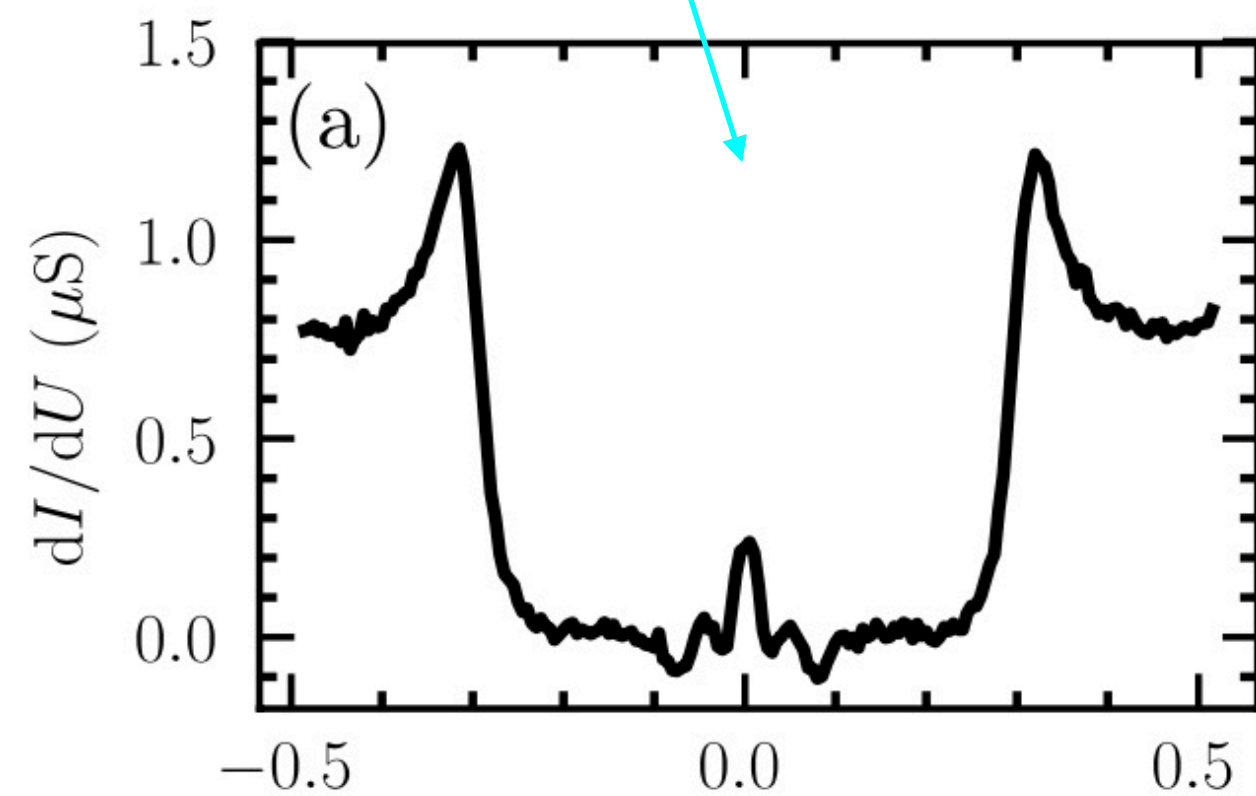
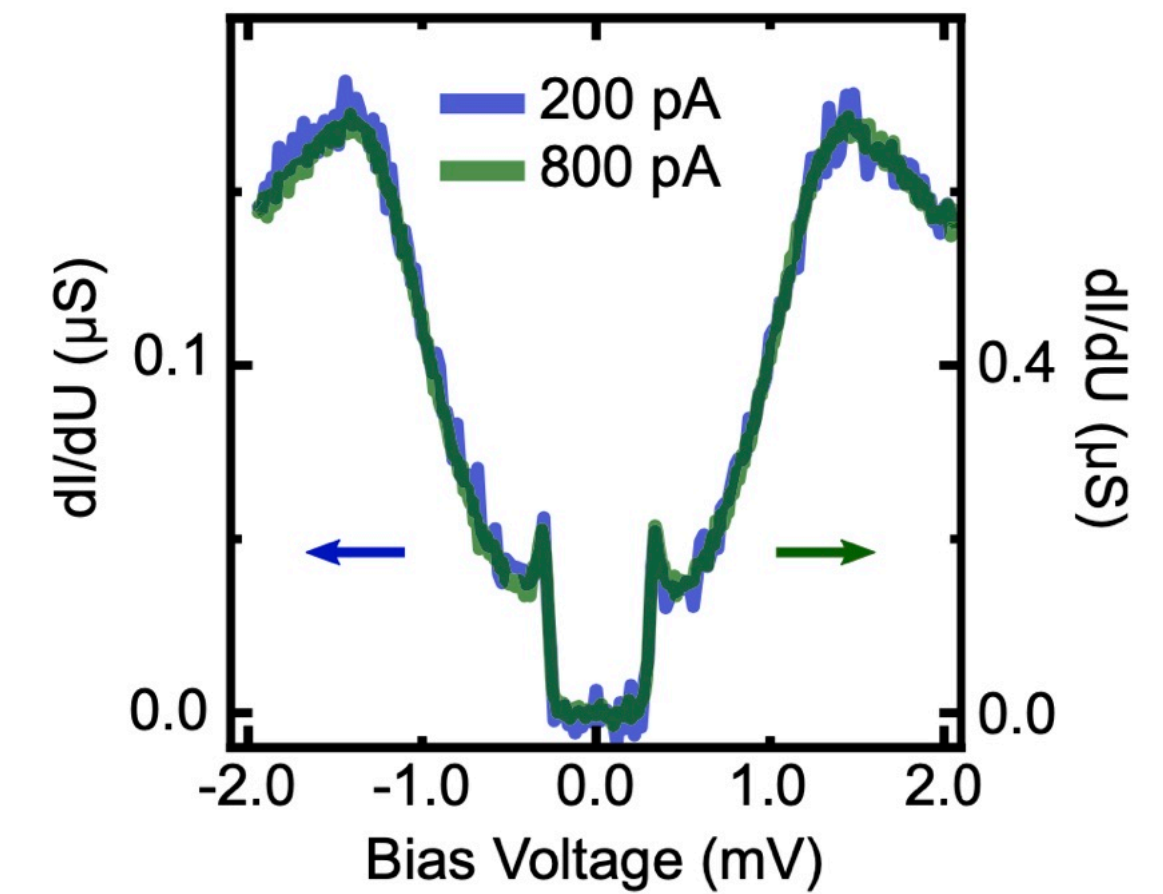
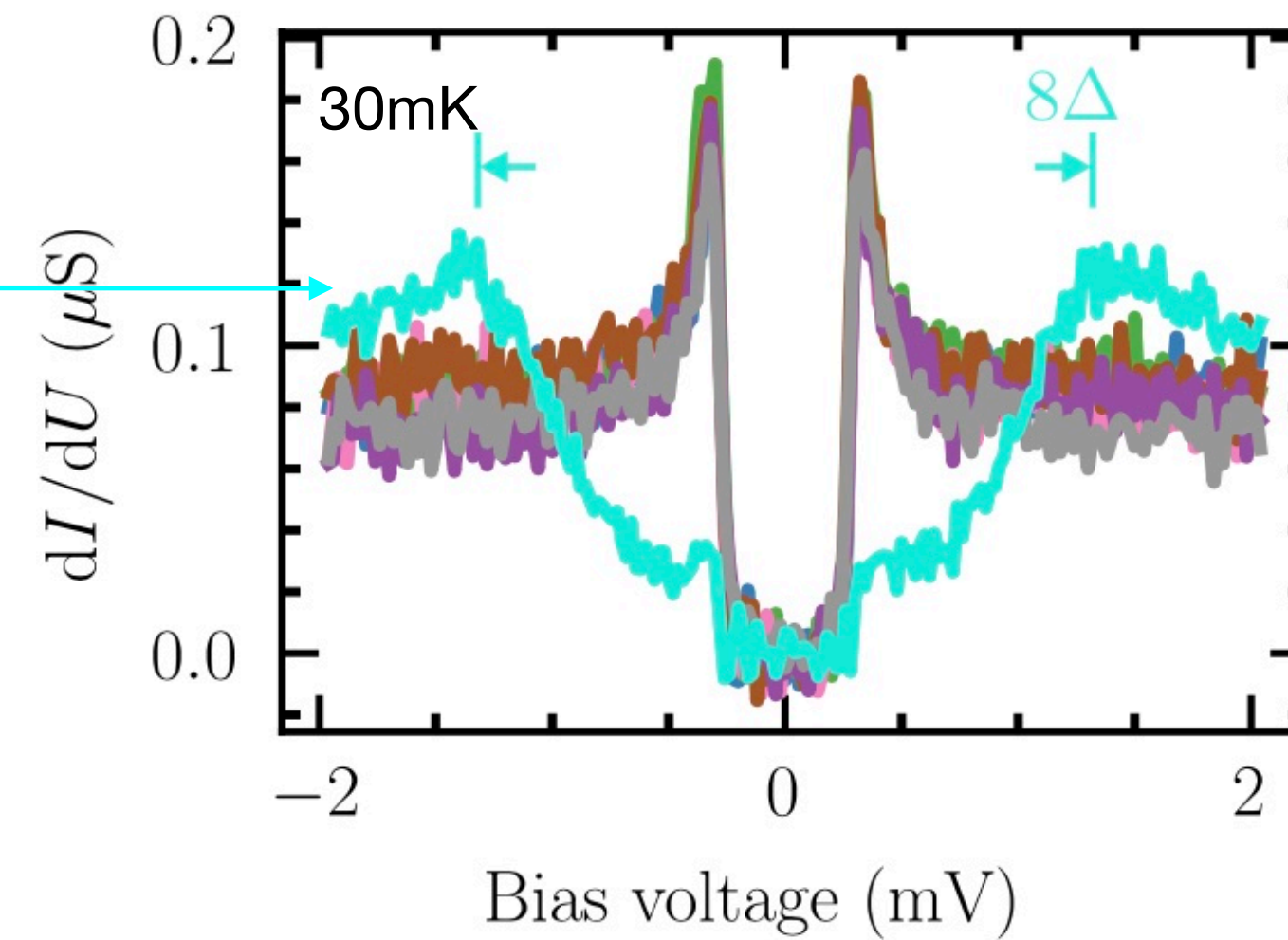
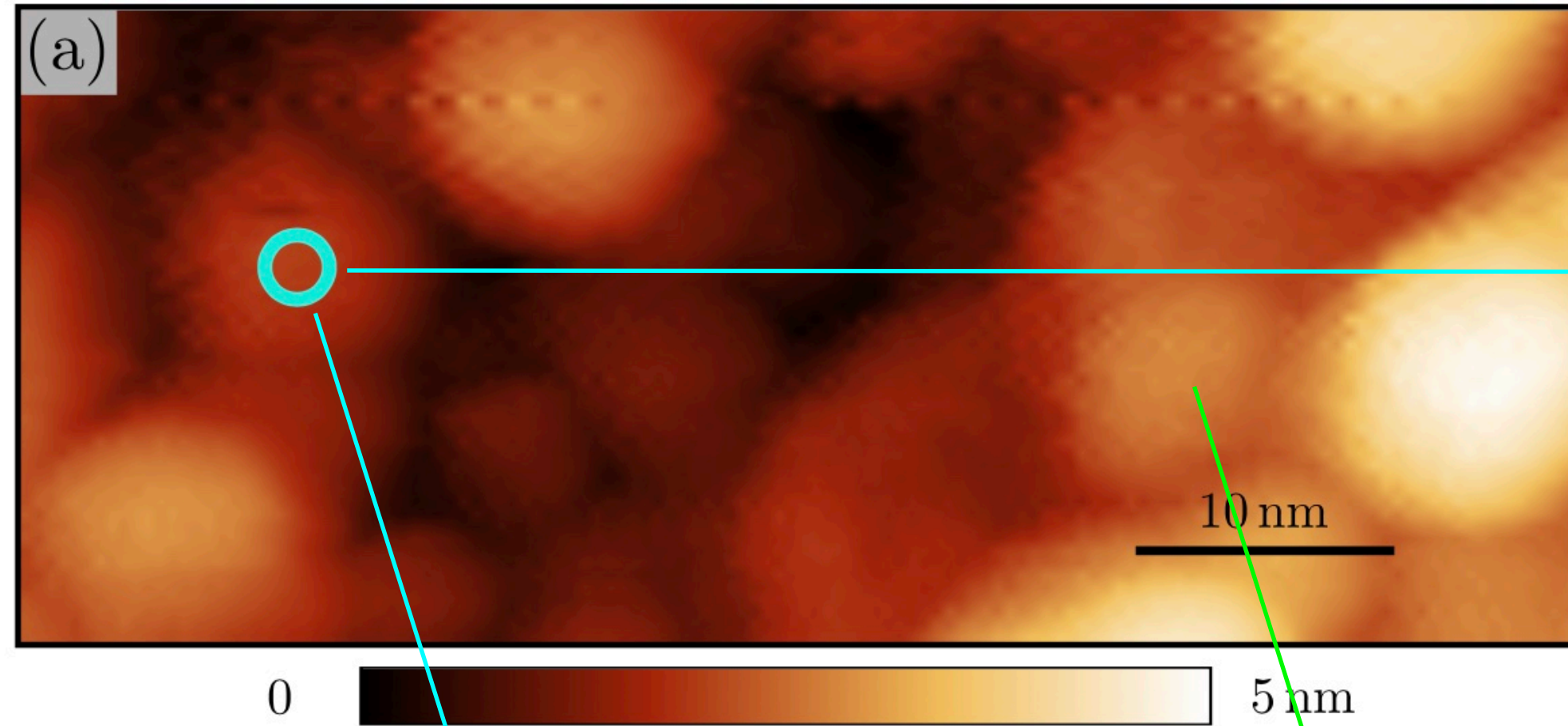


Stacking fault tetrahedron in Pb(111)



- Enhanced electron-phonon interaction inside tetrahedron
- Clear van Hove peaks for transversal and longitudinal phonon branch
- The tetrahedron acts as a box for standing electrons, lifting the strict selection rules
- Transversal phonons show structure

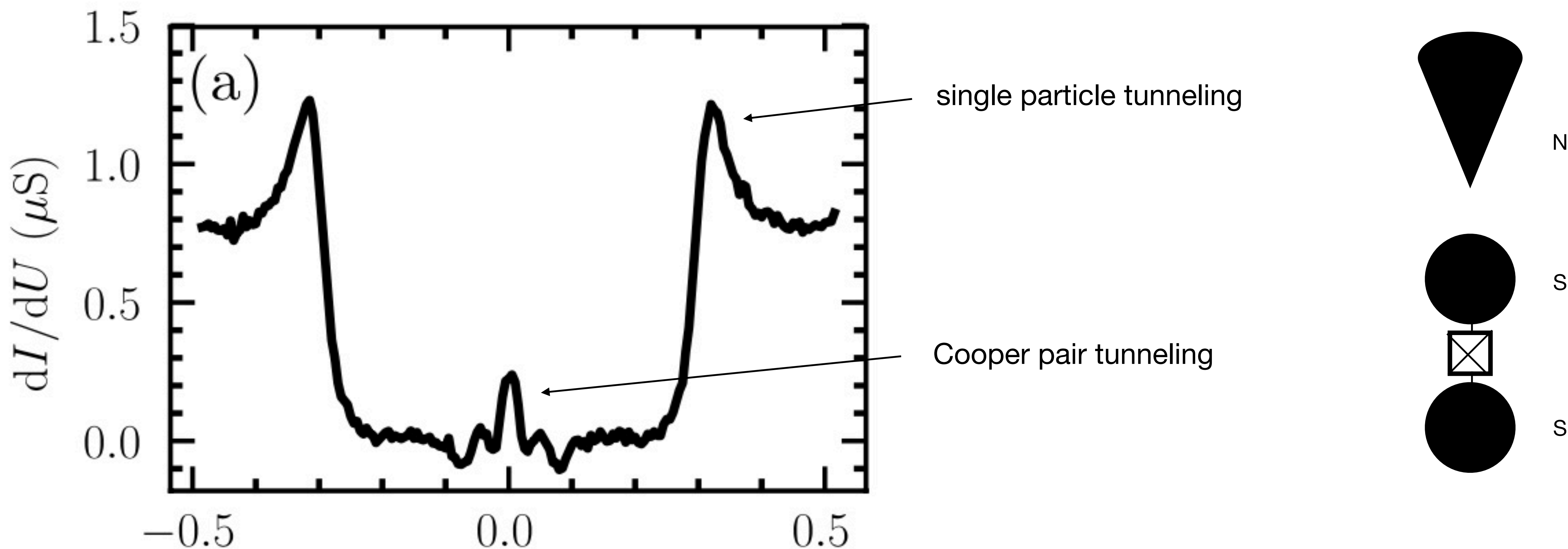
Oxygen poor samples ($300 \mu\Omega\text{cm}$)



Bias voltage (mV)

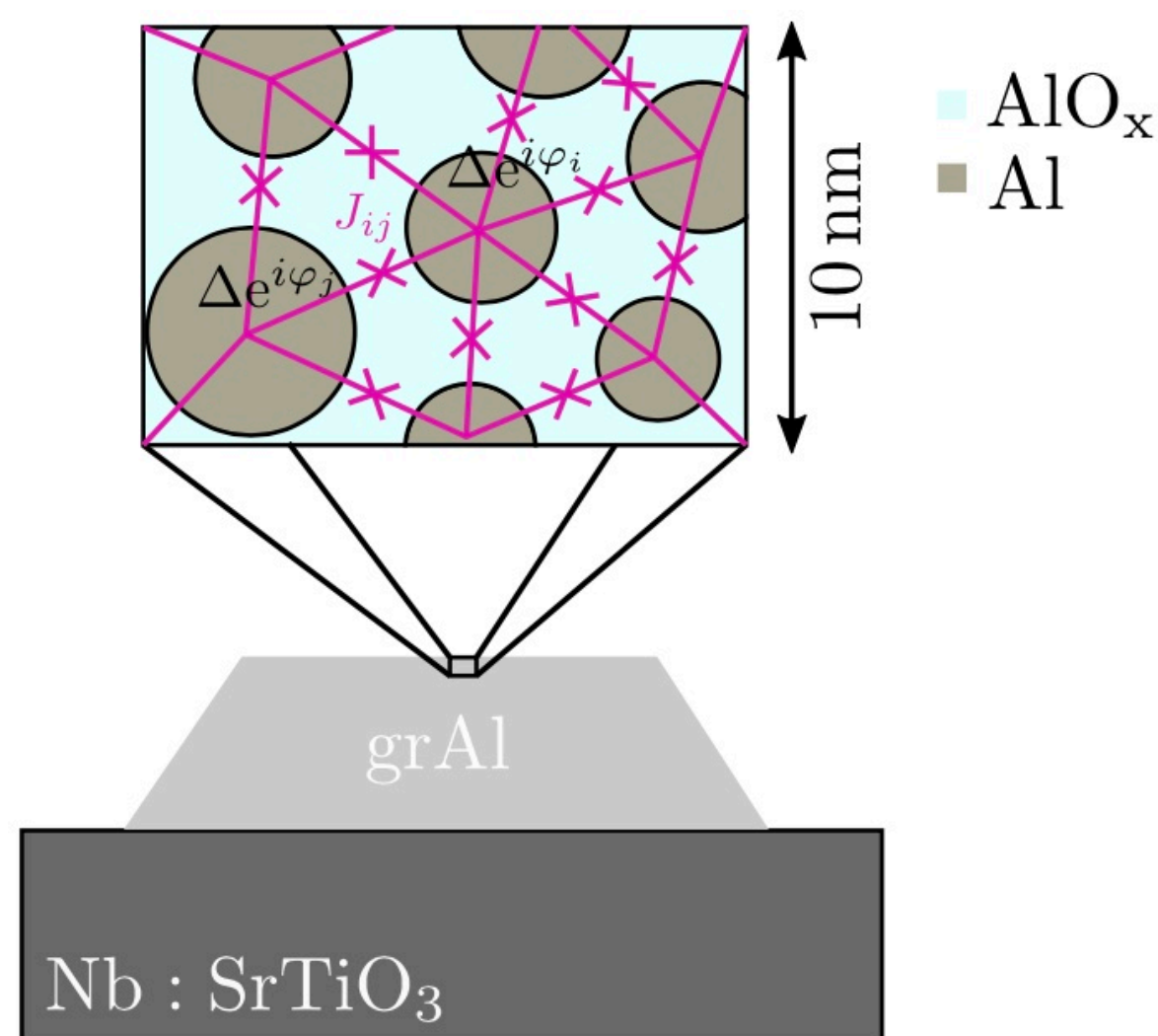
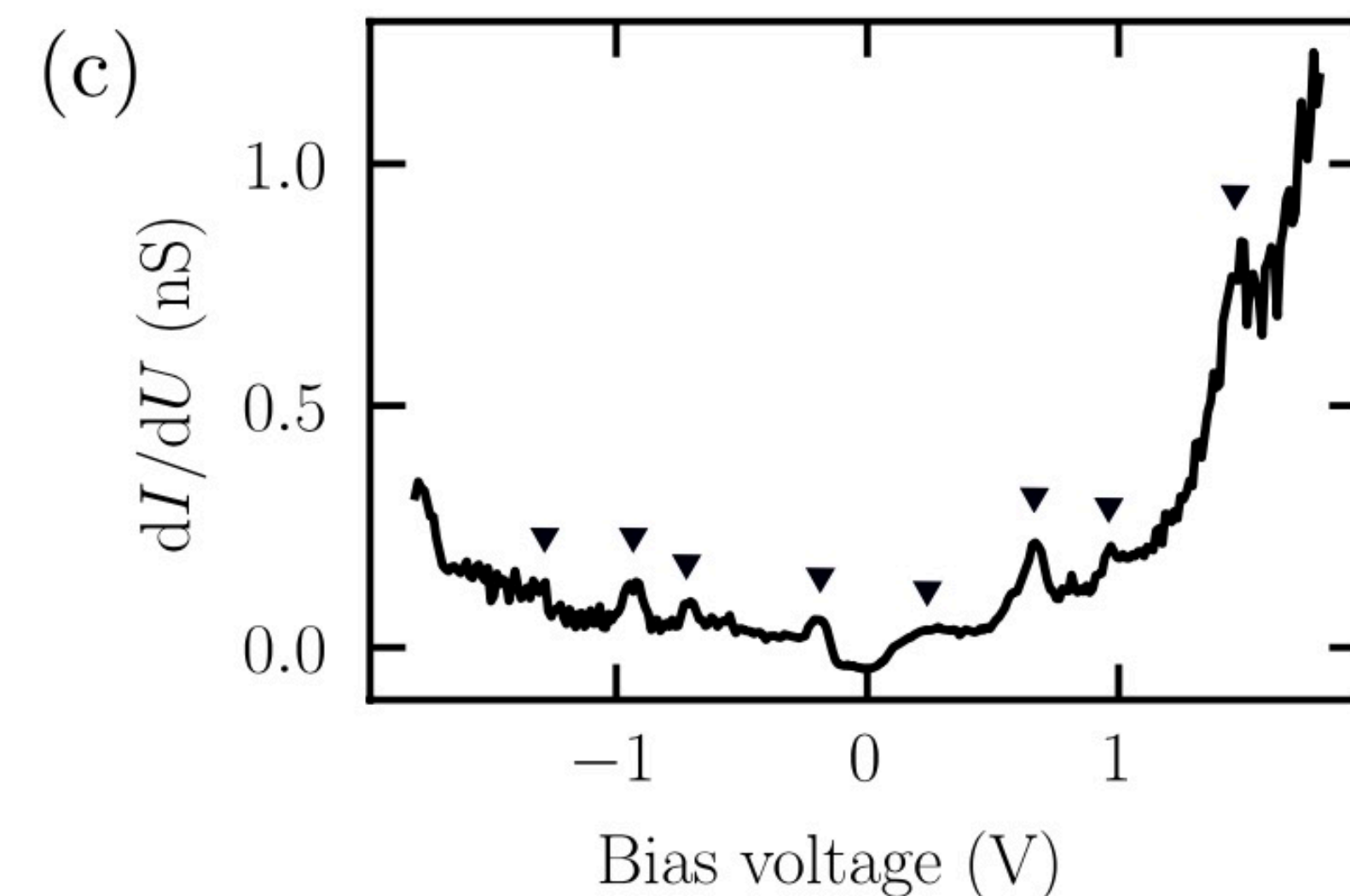
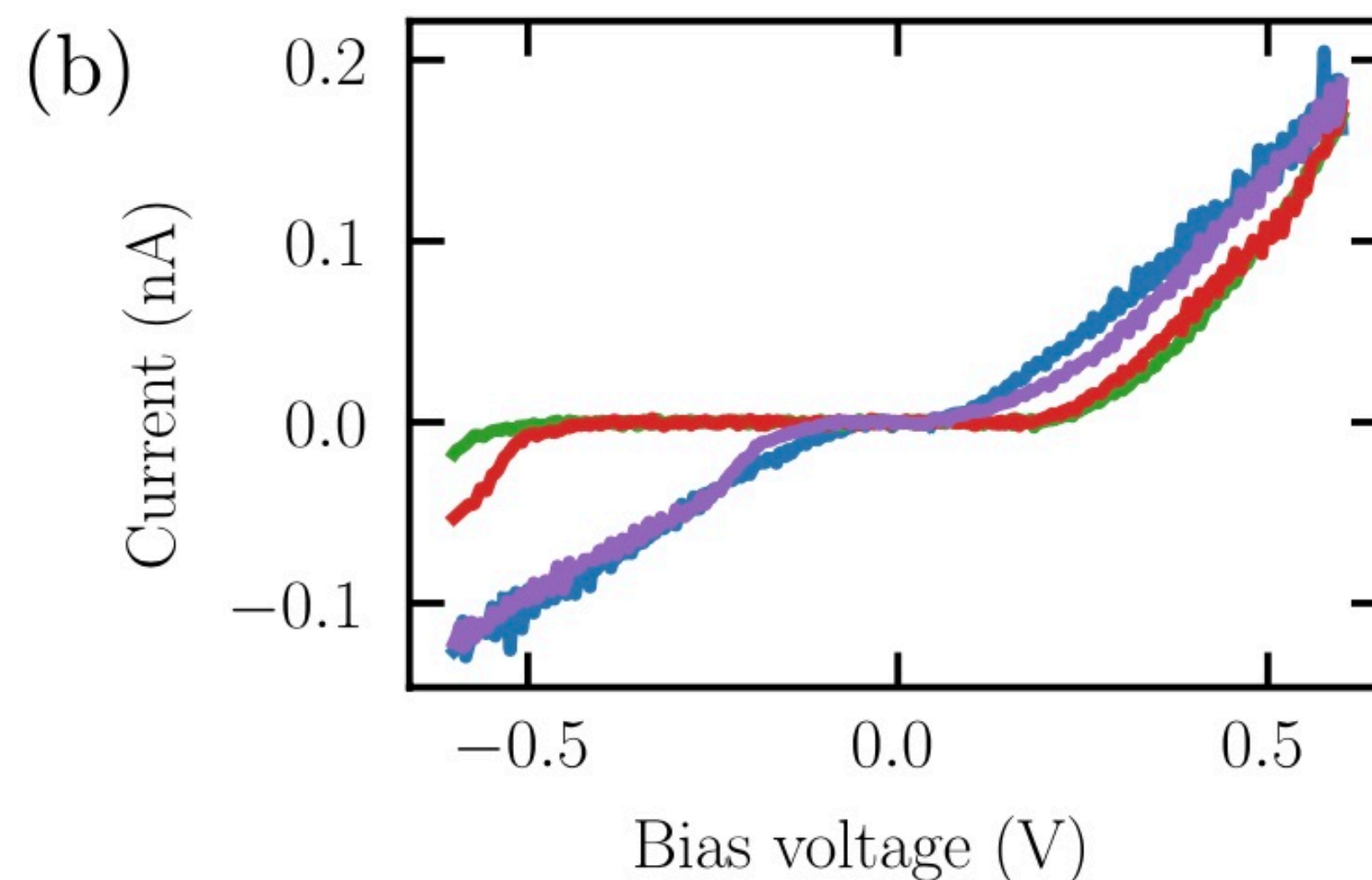
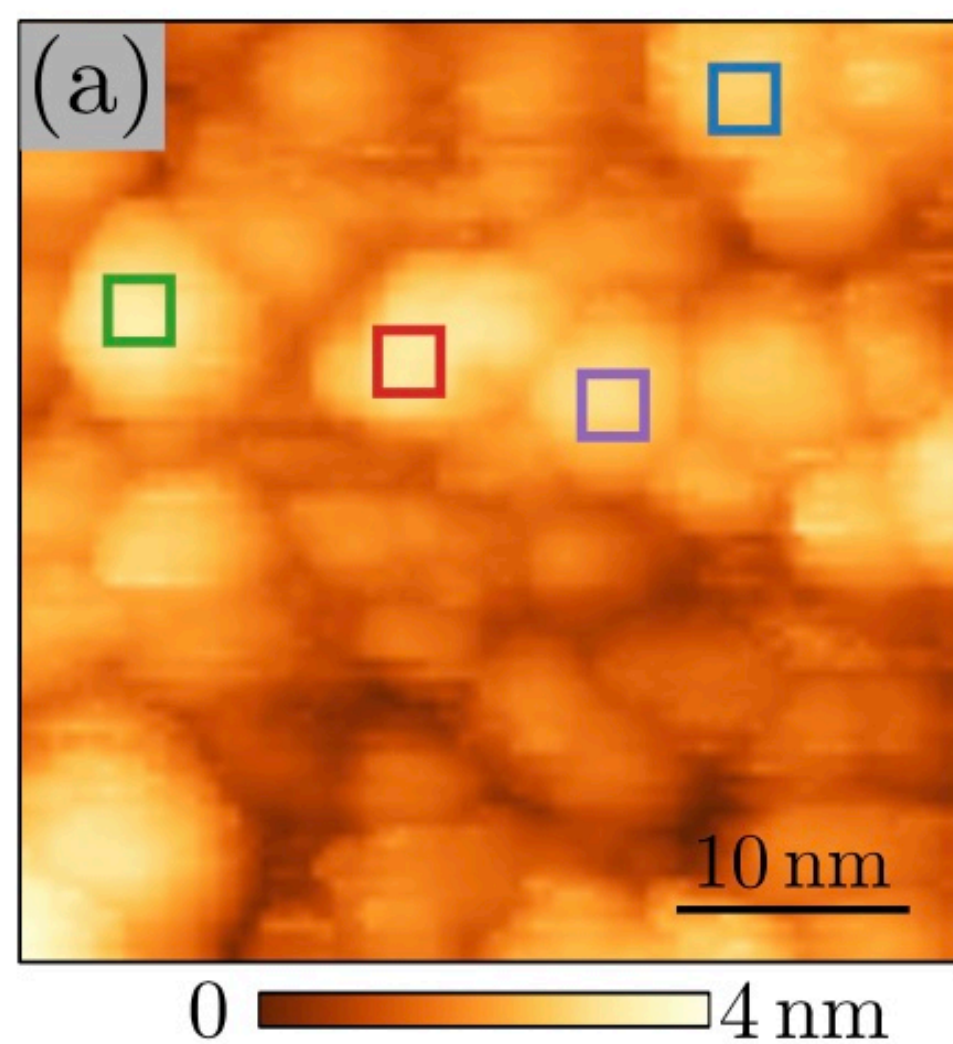
- Few grains show an additional pseudo-gap of $\approx 8\Delta$
- Pseudo gap is no function of current
- First signs of decoupling detected at high current densities for grains with pseudo gap
- Josephson coupling seen around 0V

Oxygen poor samples ($300 \mu\Omega\text{cm}$)



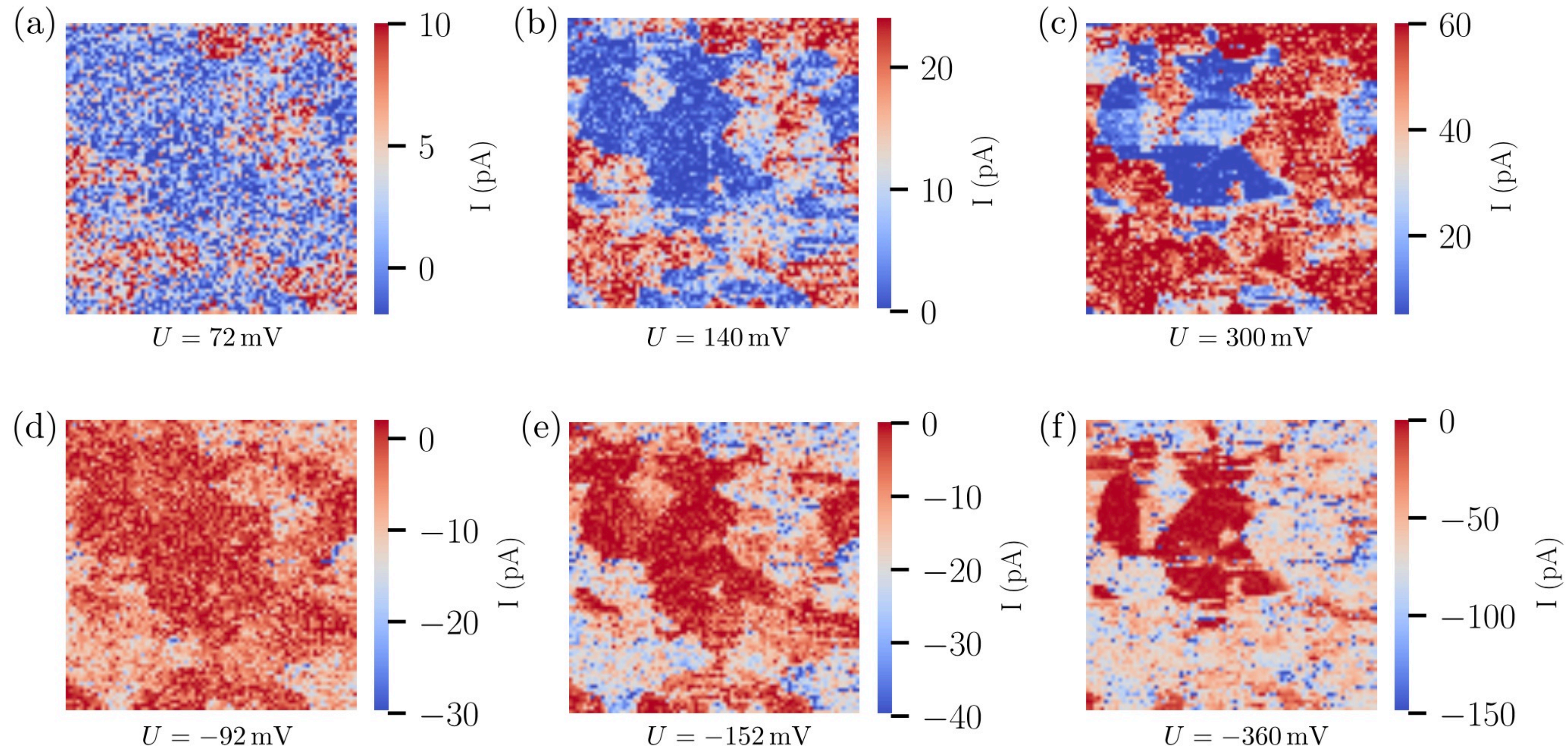
- At high currents and with decoupled grains, part of the bias voltage needs to drop between grains
- Combination of Andreev reflection and Josephson tunneling
- Can only be explained, when we take into account the full charge transport

Oxygen rich samples ($2000 \mu\Omega\text{cm}$)



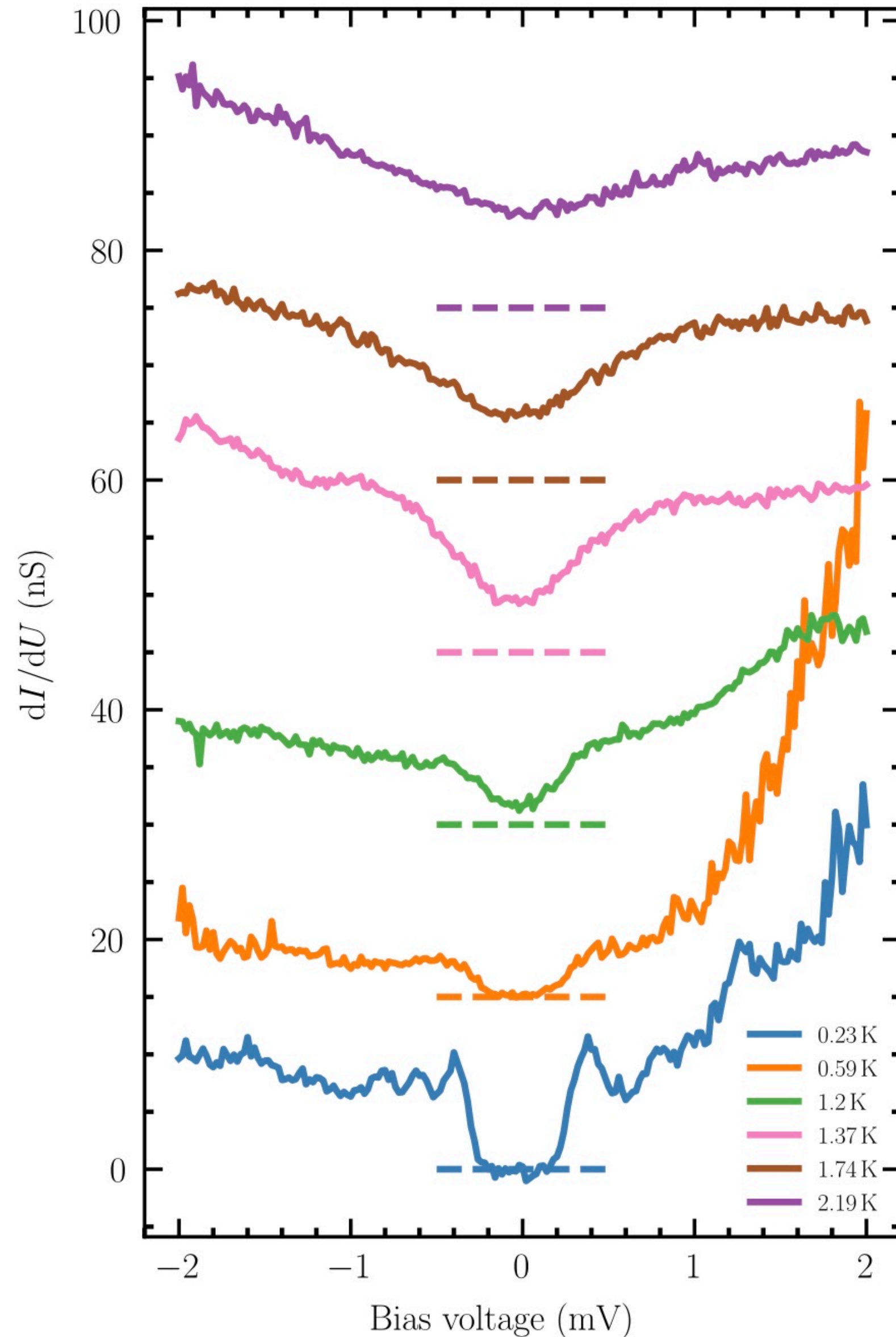
- No relevant change in grain size
- Strong variations from grain to grain in $I(V)$ curve
- Clear charging effects observable
- Grains start to decouple, Coulomb blockade sets in
- Lifetime broadening of charging peaks $\Gamma \gg \Delta$
- Film is not yet insulating

Oxygen rich samples ($2000 \mu\Omega\text{cm}$)

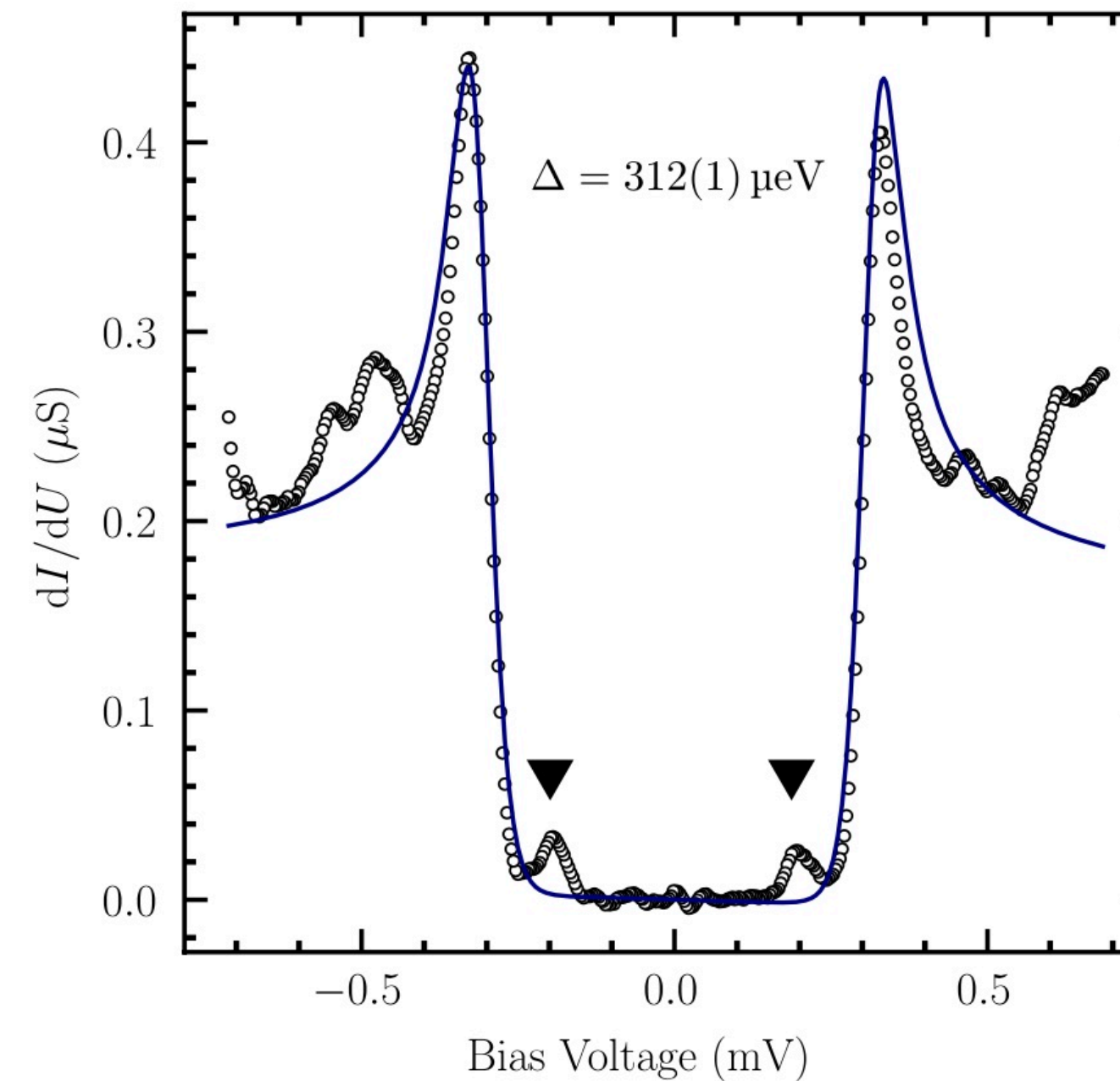


- I(V) maps show charging steps extended over several grains
- With $E_c = \frac{e^2}{2C}$ and charging energies between 70 and 300mV, we can estimate capacitances between 0.3-1.1 aF ($\epsilon_r = 9.0$)
- Coulomb clusters of about 10 grains also agrees with recent transmon qubit experiments (Winkel et al. PRX 10,031032)

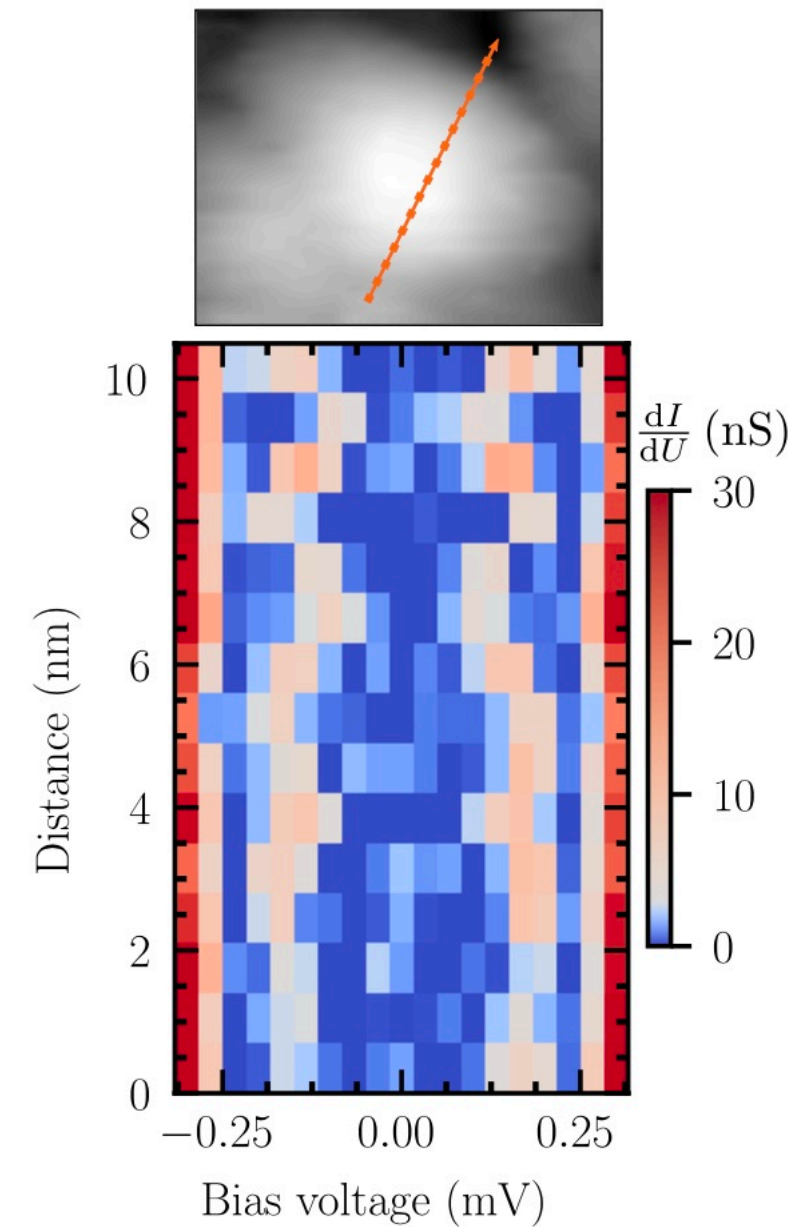
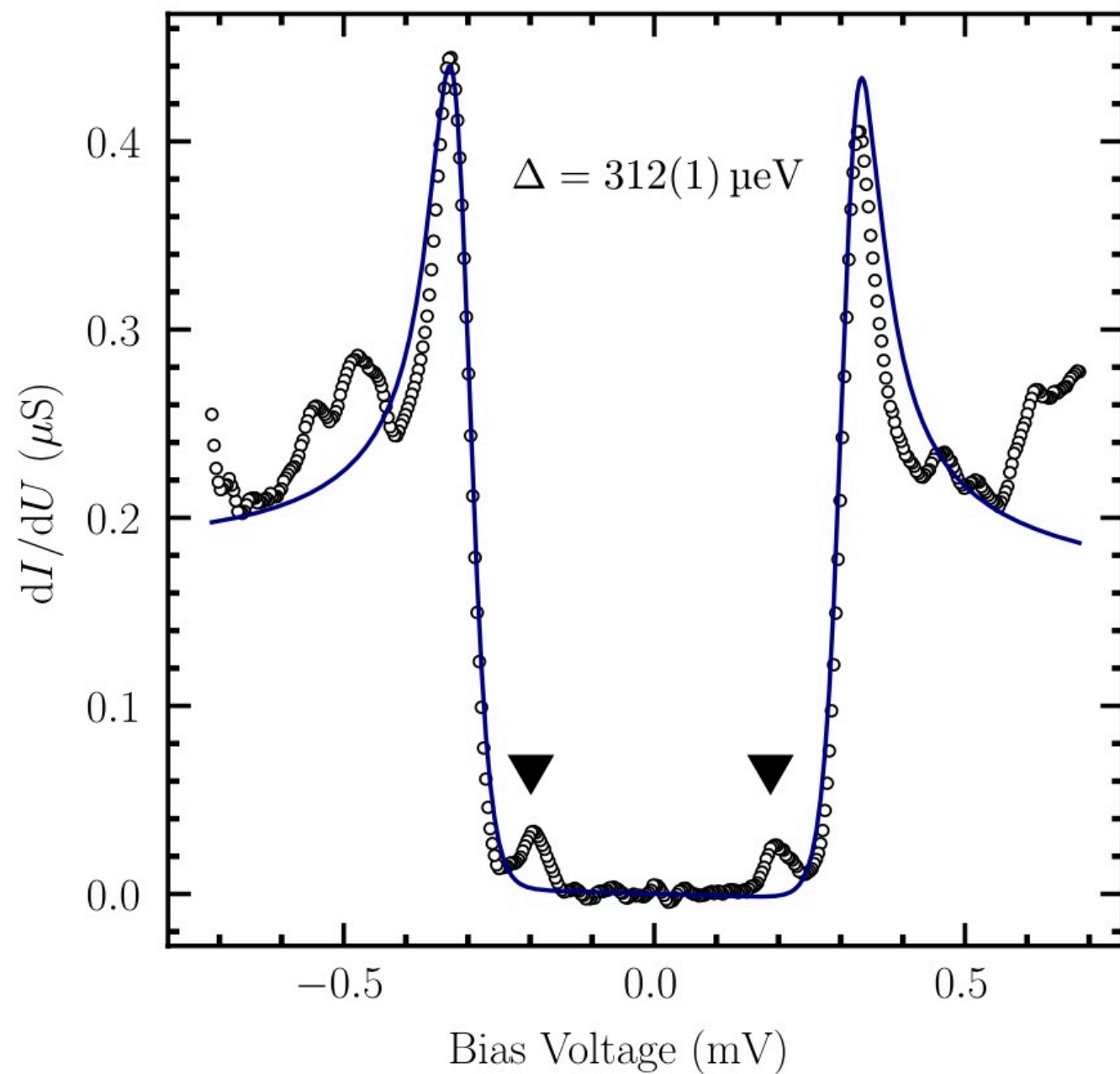
Oxygen rich samples ($2000 \mu\Omega\text{cm}$)



- Sample still shows superconducting gap in low-energy spectrum
- Gaps is even larger than in oxygen poor samples
- Gap is homogeneous
- T_c is much enhanced compared to bulk Al
- In gap states are occasionally found on individual grains
- In gap states can cause decoherence

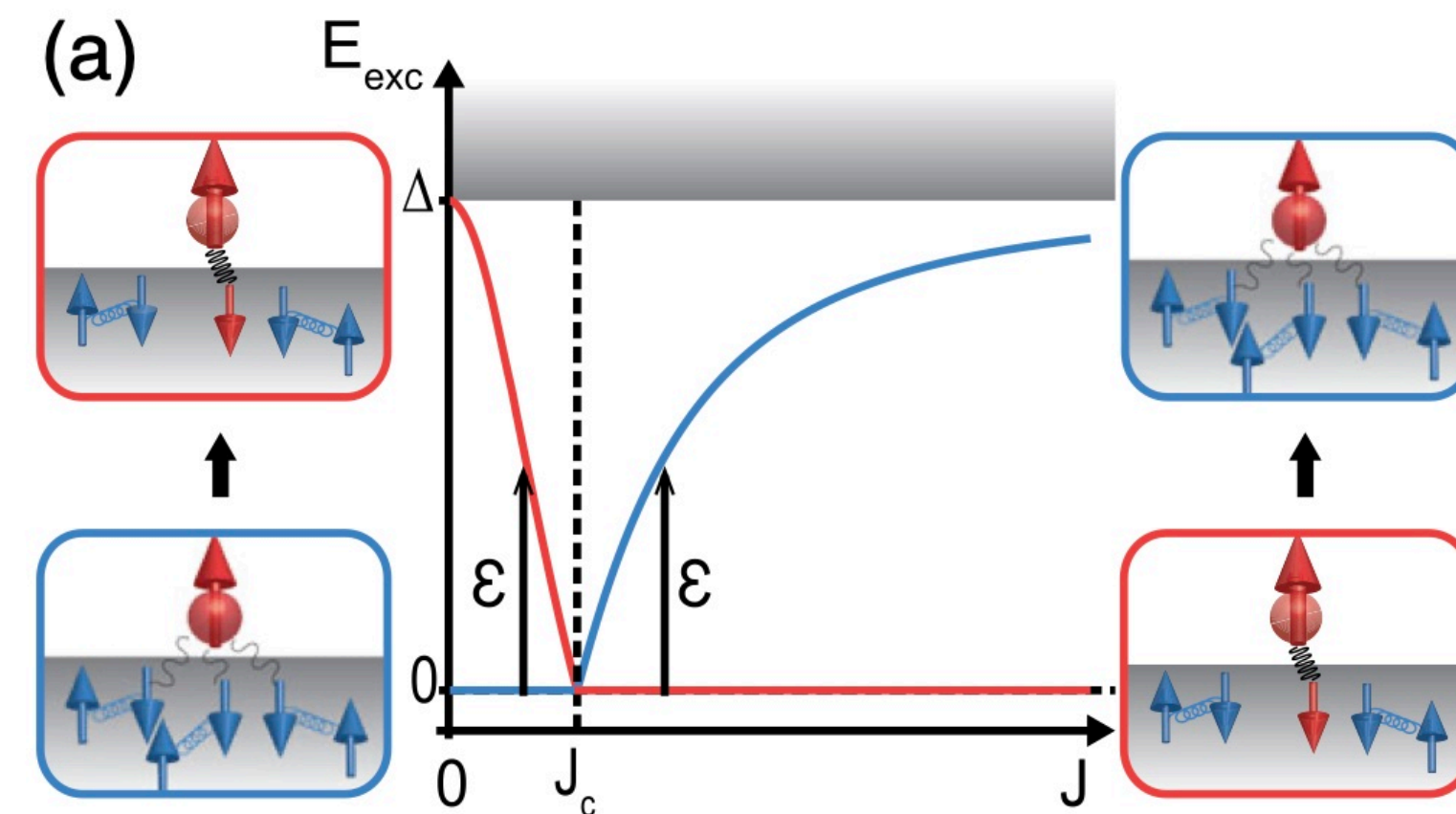


In gap states in oxygen rich samples ($2000 \mu\Omega\text{cm}$)



- Sample is (super)conducting, i.e. no carrier localization
- Energy of coherence peak does not change when moving tip → no change of chemical potential of grain due to electric field
- Energy of YSR peak does change
- Impurity spin cannot be located on grain but inside the oxide → unpaired electron in dangling bonds of unordered AlO_x

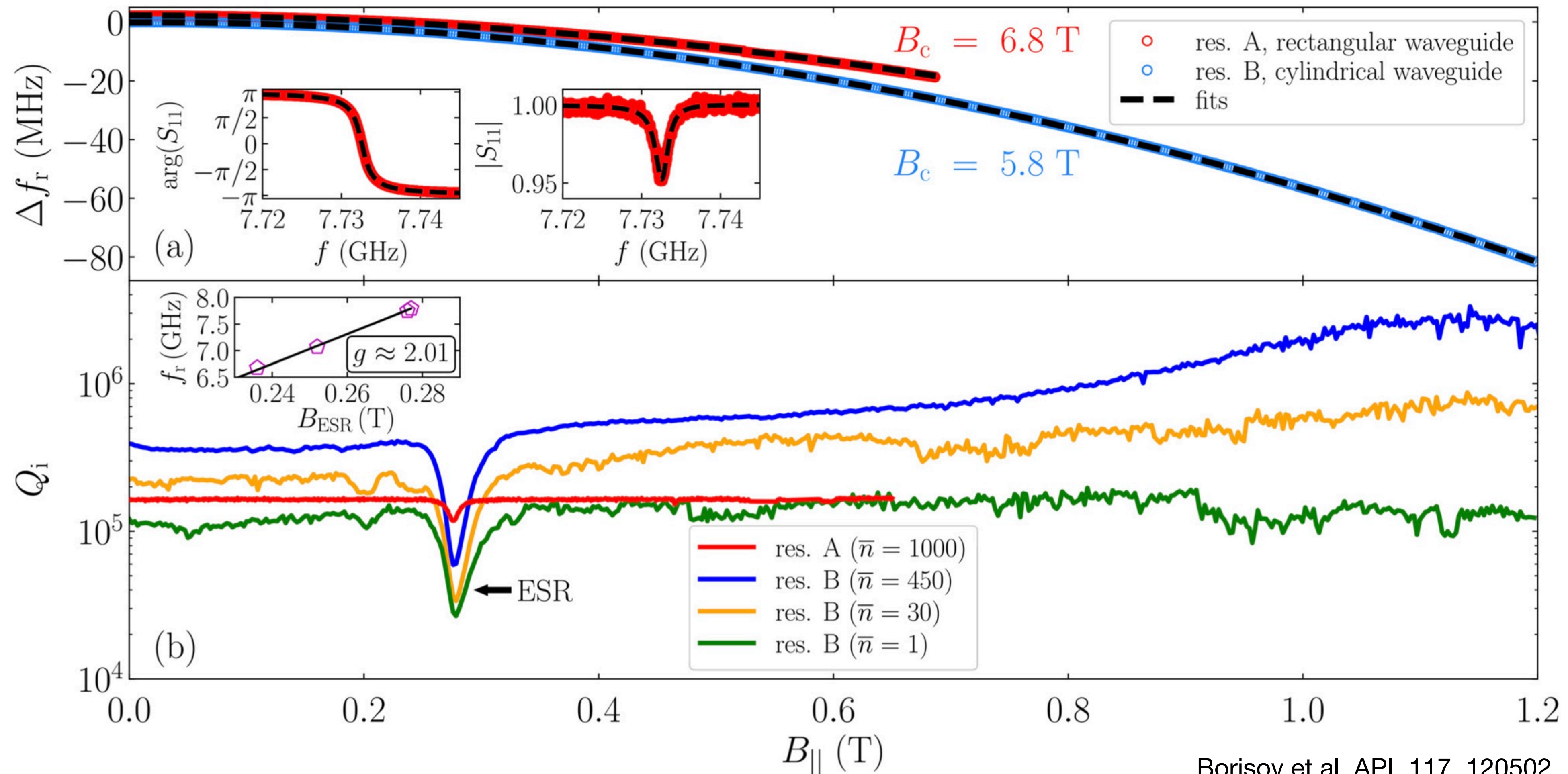
- Speculation of quantized carriers on individual grains, odd number of carriers leads to unpaired electrons
- Unpaired electrons interact with the condensate such that Yu-Shiba-Rusinov states may form
- Competition between pair breaking/screening of the localized spin and pairing



Farinacci et al.,
PRL 121, 196803

- Agrees with Kondo effect near metal-to-insulator transition (see Bachar et al. PRB 87, 214512)

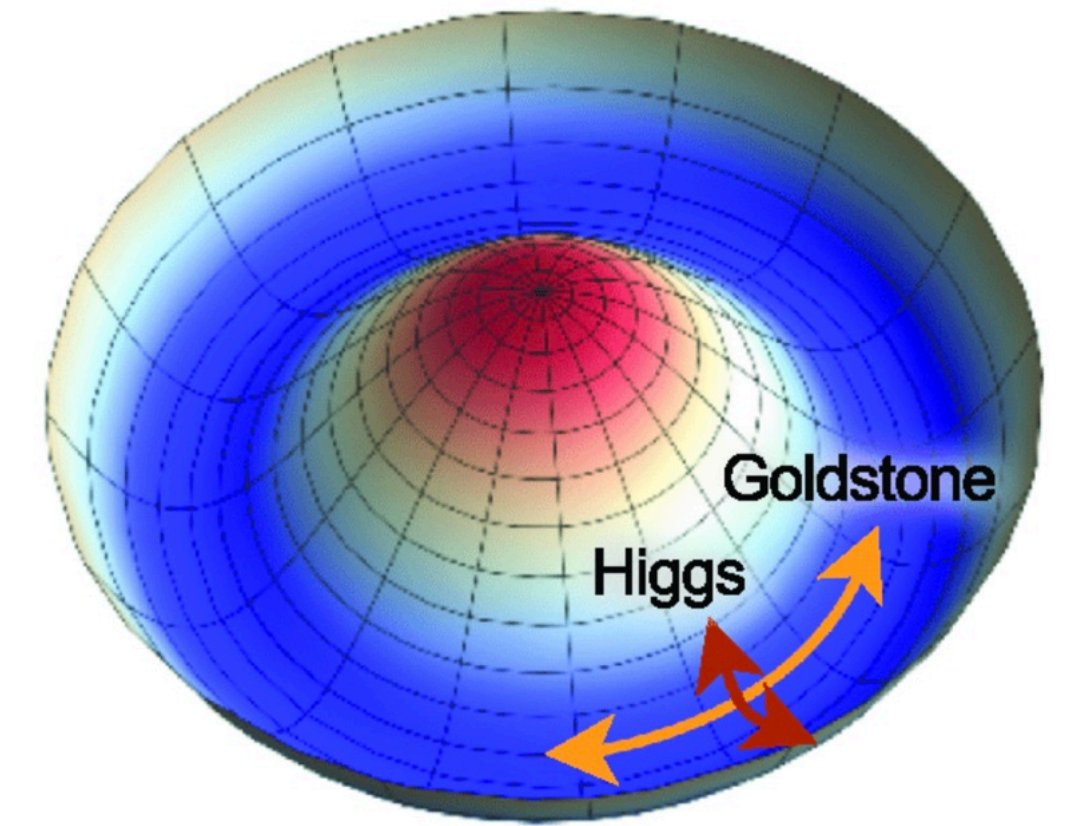
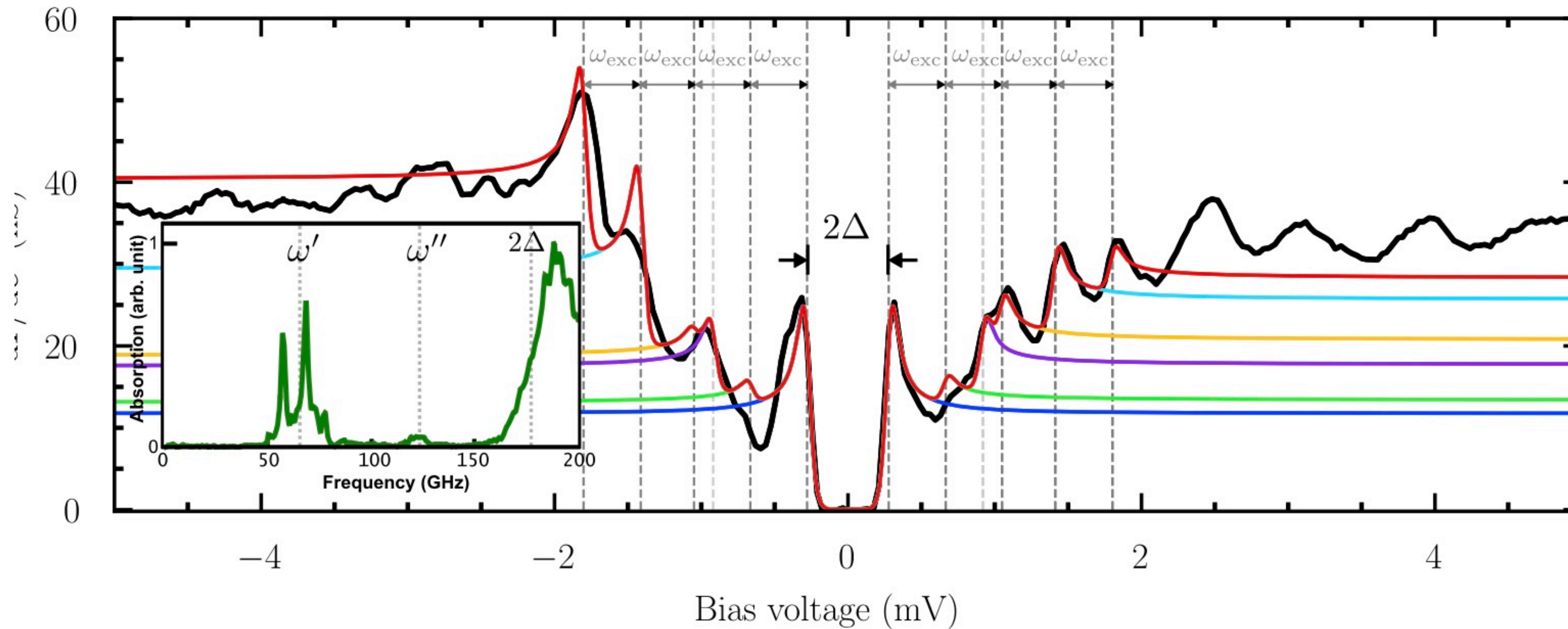
ESR signals in grAl resonators



Borisov et al. APL 117, 120502

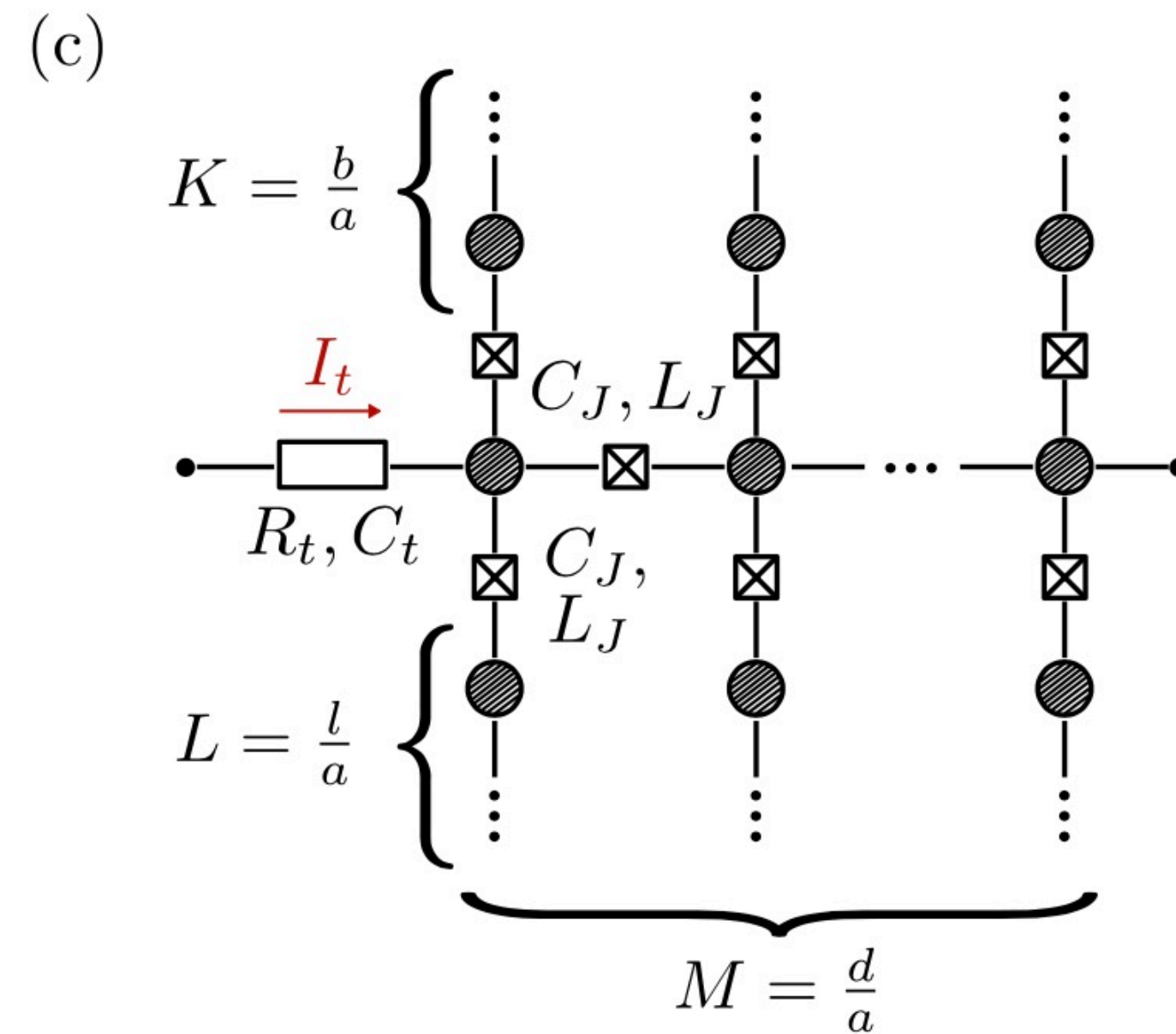
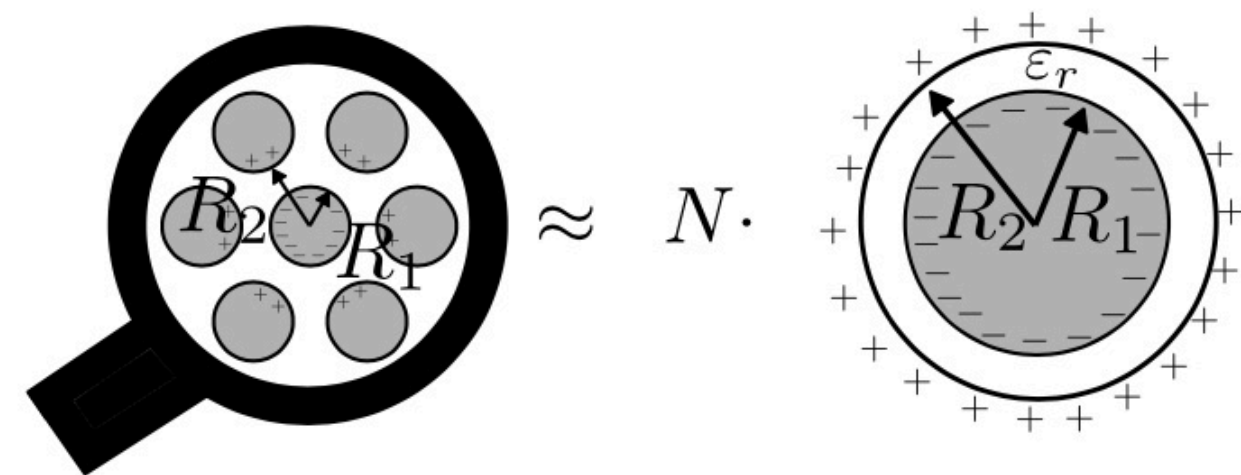
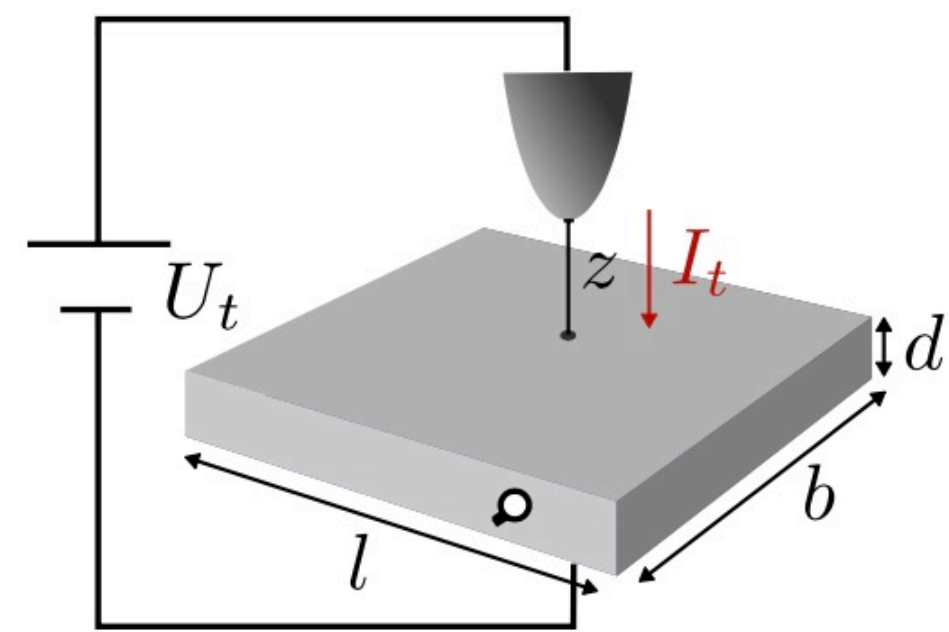
- Unpaired electrons ($s=1/2$) with $g \approx 2$ were confirmed by ESR signal with field in the plane manifested as drop in quality factor in resonators

Excitations in oxygen rich samples ($2000 \mu\Omega\text{cm}$)



- Nature of the pseudo gap ?
- In oxygen rich samples, clear inelastic excitations exist outside the gap with energies roughly $E = \Delta + n\hbar\omega_{exc}$
- Spectrum can be fitted with up to 5 excitations per tunneling electron
- $\hbar\omega_{exc} \approx 1.4\Delta$ agrees well with THz absorption measurements on grAl samples with same sheet resistance (Levy-Bertrand et al., PRB 99 094506)
- Higgs mode near S-I-transition can be long-lived excitations with $\hbar\omega < 2\Delta$ (Sherman et al. Nature Phys. 11, 118)
- Why only 5 excitations?

Plasmon modes oxygen rich samples ($2000 \mu\Omega\text{cm}$)



- LC resonator model

$$C_J = 4\pi\epsilon_0\epsilon_r \frac{R_1 R_2}{R_1 + R_2}$$

$$L_J = \frac{\Phi_0}{2\pi I_c}$$

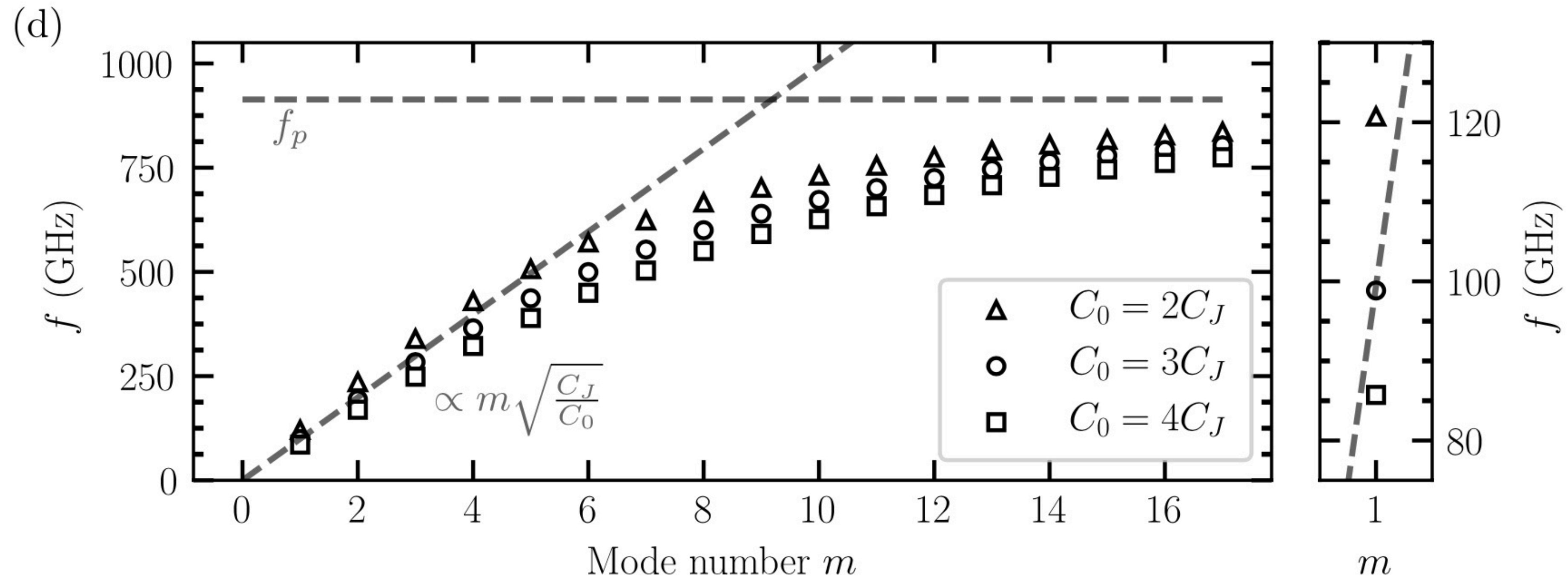
$$R_1 = 1.25 \text{ nm} \quad R_2 = 1.75 \text{ nm} \quad C_J = 0.73 \text{ aF}$$

$$j_c = 0.88 \text{ mA}/(\mu\text{m})^2$$

$$f_p = \frac{\omega_p}{2\pi} = \frac{1}{2\pi} \sqrt{\frac{1}{L_J C_J}}$$

$$f_c = 914 \text{ GHz}$$

Plasmon modes oxygen rich samples ($2000 \mu\Omega\text{cm}$)



- Plasmon modes confined in thin film:

$$\omega_m = \frac{m\pi}{M} \left(L_J \left(C_0 + \frac{m^2 \pi^2}{M^2} C_J \right) \right)^{-1/2}$$

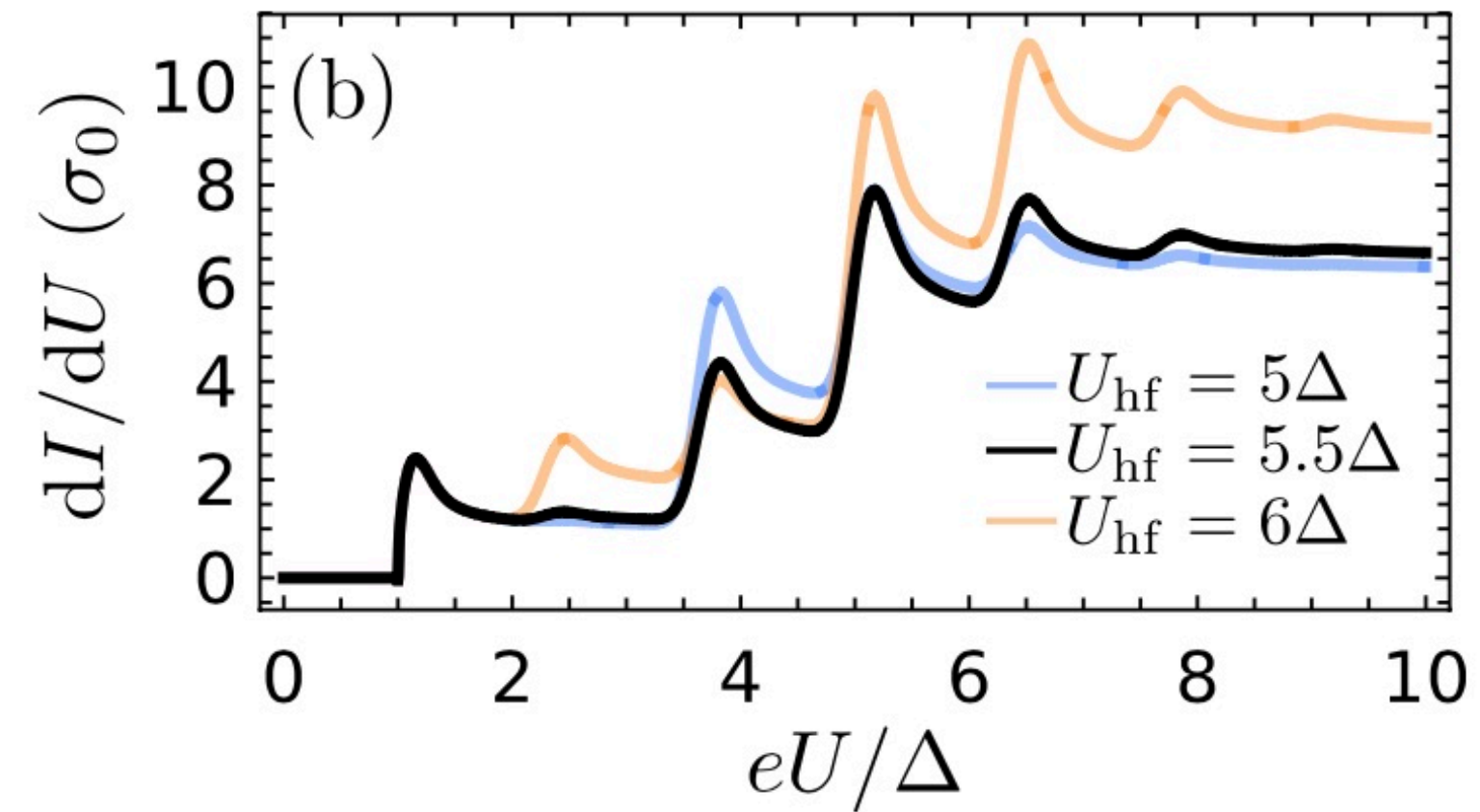
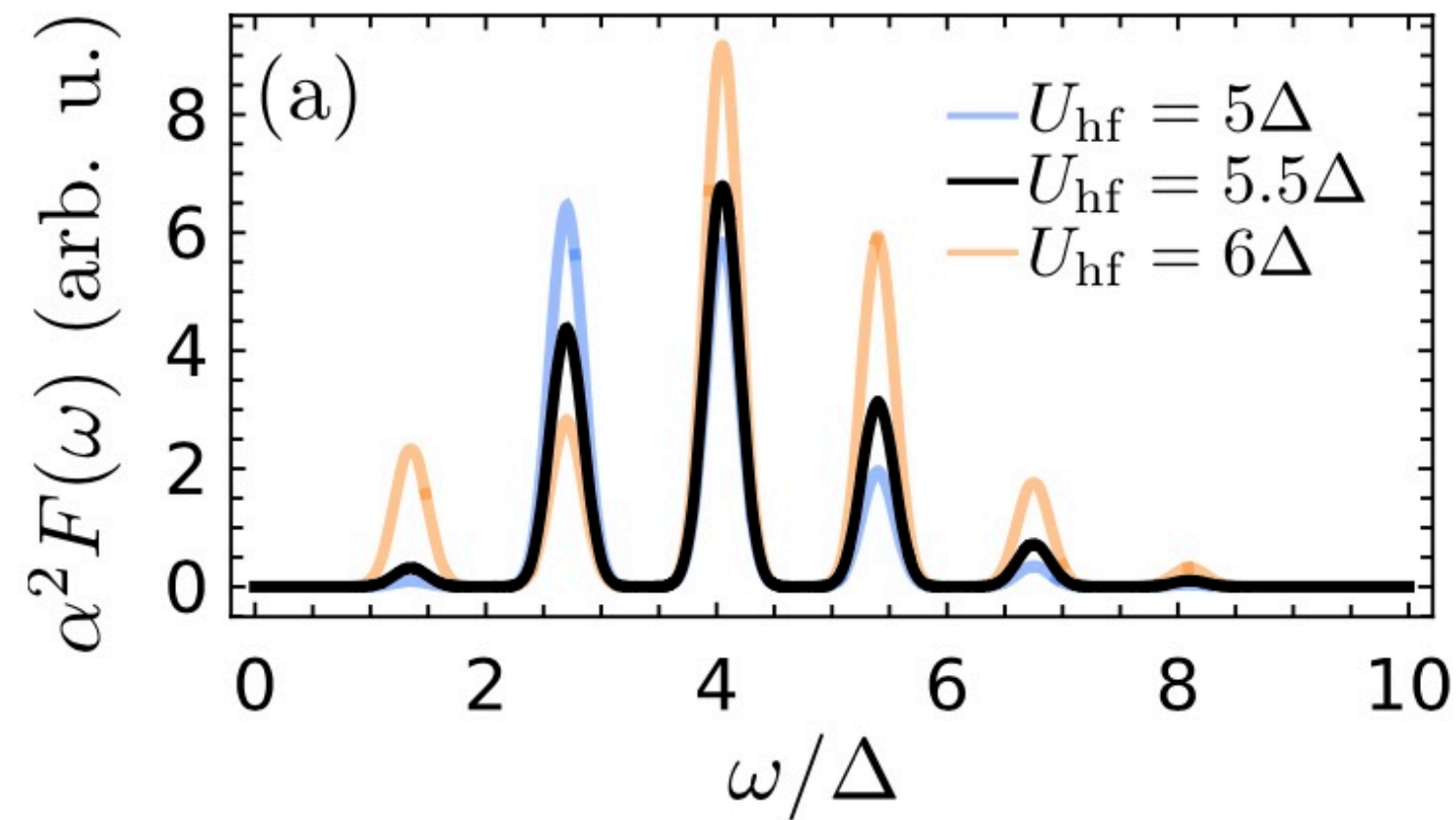
$$\rightarrow \omega_1 = 1.28 - 1.8\Delta$$

Tien-Gordon Model for spontaneous plasmon emission

$$\begin{aligned}\sigma_s^{\text{tot}}(eU) &= \int_0^{eU} d\omega \sigma_s^{\text{el}}(eU - \omega) \sum_n J_n^2 \left(\frac{eU_{\text{hf}}}{\omega_{\text{exc}}} \right) \delta_a(\omega - n\omega_{\text{exc}}) \\ &= \sigma_s^{\text{el}}(eU) + \underbrace{\int_0^{eU} d\omega \sigma_s^{\text{el}}(eU - \omega) \sum_{n=1} J_n^2 \left(\frac{eU_{\text{hf}}}{\omega_{\text{exc}}} \right) \delta_a(\omega - n\omega_{\text{exc}})}_{\propto \alpha^2 F(\omega)}\end{aligned}$$

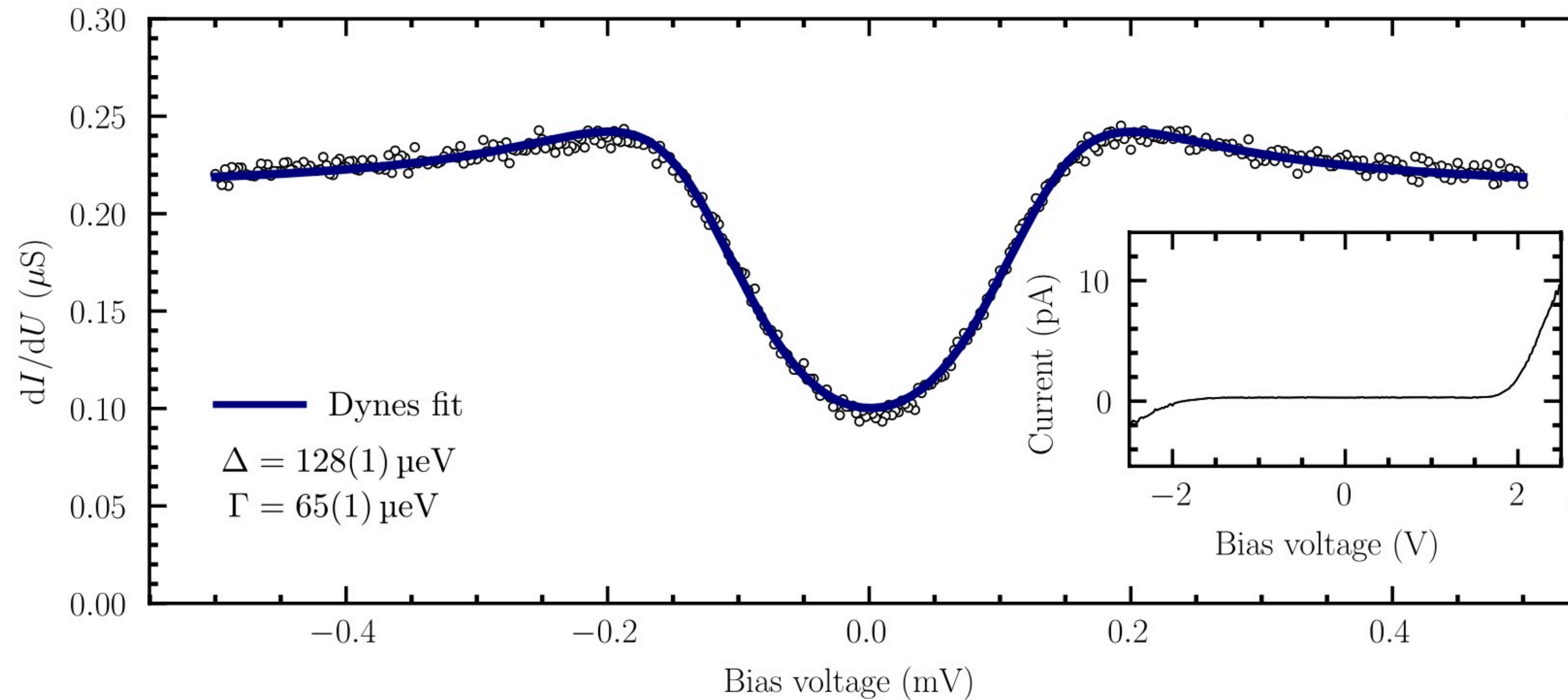
with

$$\delta_a = \frac{1}{|a|\sqrt{\pi}} e^{-(x/a)^2}.$$



- Tien-Gordon model naturally explains intensities of excitations

AlOx on single crystal Al(111)



- Preliminary results!
- Oxidation in UHV with 2.7×10^4 L, corresponds to 2 ML or 0.8 nm
- Clearly, the insulating oxide is detected as an insulating barrier in $I(V)$ curves
- Incomplete oxidation, many dangling bonds
- Local DOS very smeared, reduced gap (128 versus $166 \mu eV$) and short life time (Dynes fit)
- Oxide barrier measured locally is far from ideal insulator

Thank you for your attention!

Questions ?