



# Magnifying quantum phase fluctuations with Cooper-pair pairing

*Smith et al. PRX 2022*

*Smith & Borgognoni et al. (in preparation)*



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*Mines Paris, Inria, ENS, Université PSL, CNRS*

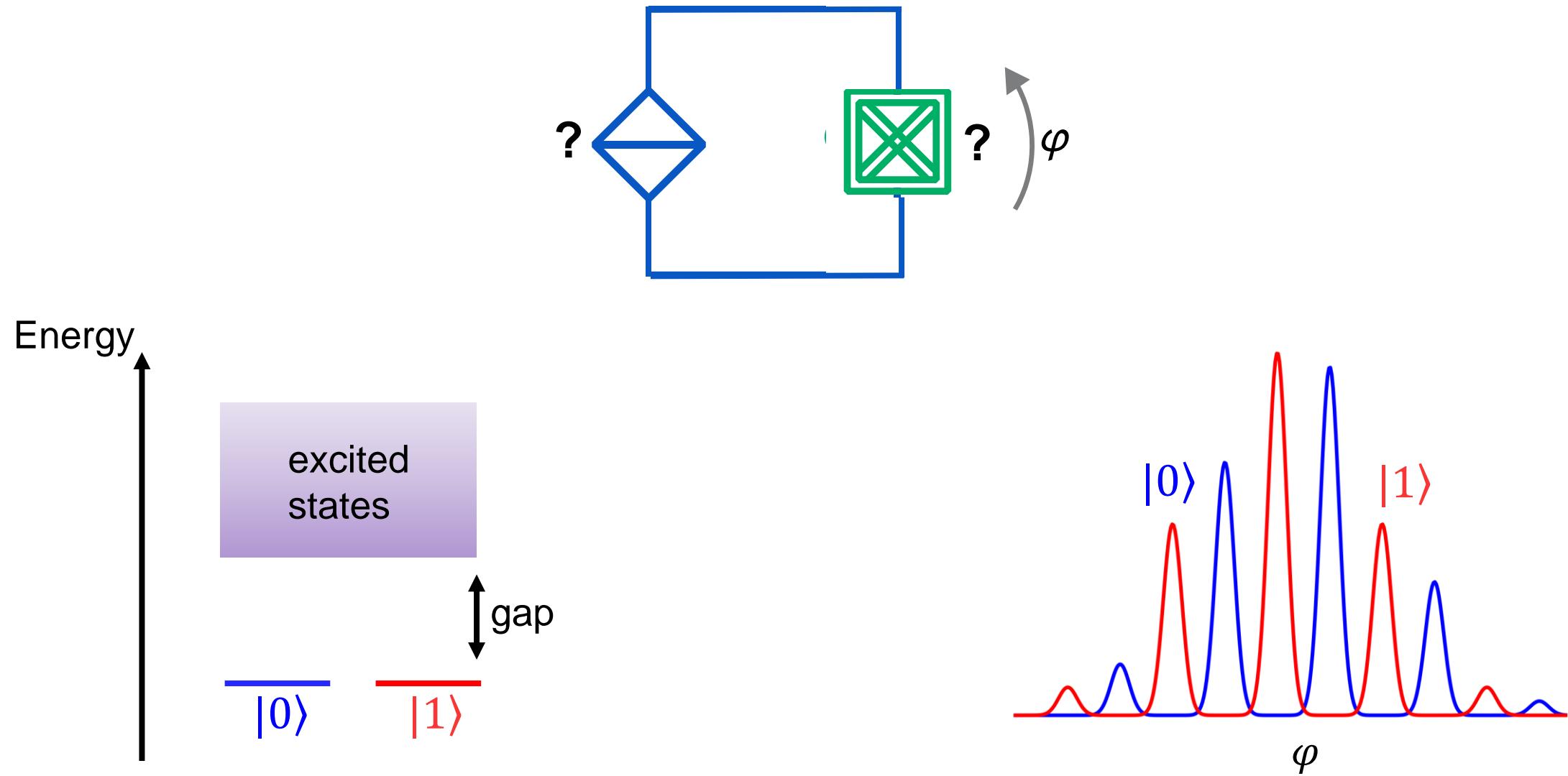
**W. C. Smith, A. Borgognoni, E. Rover'ch, M. Villiers, A. Marquet, J. Palomo, M. R. Delbecq, T. Kontos, P. Campagne-Ibarcq, B. Douçot, and Z. Leghtas**



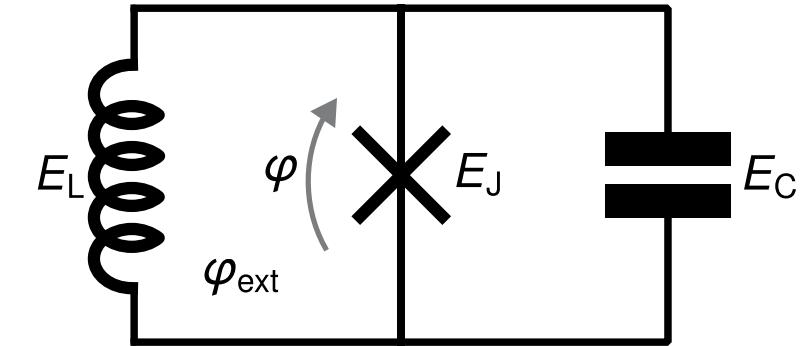
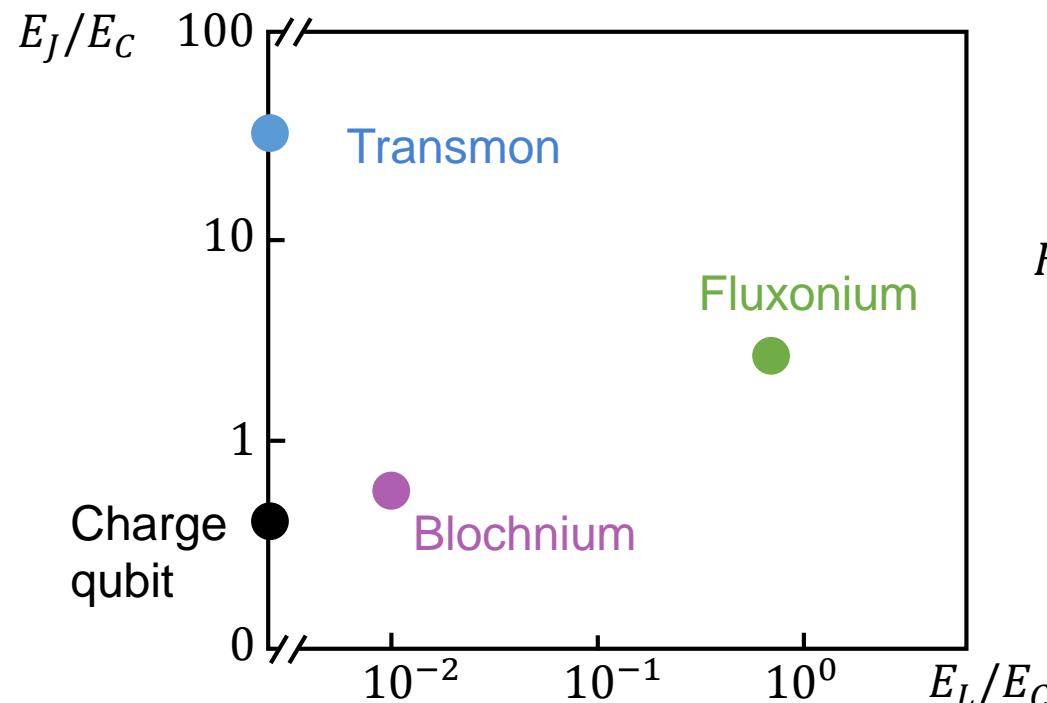
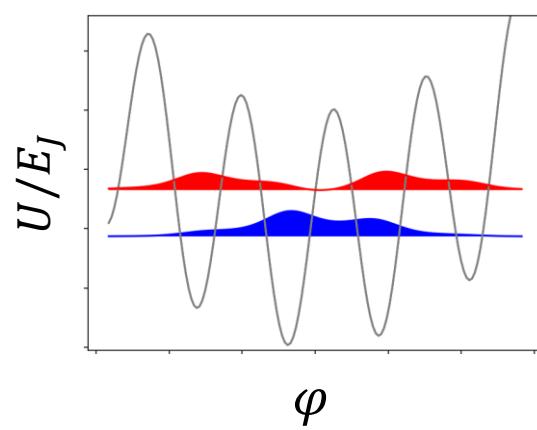
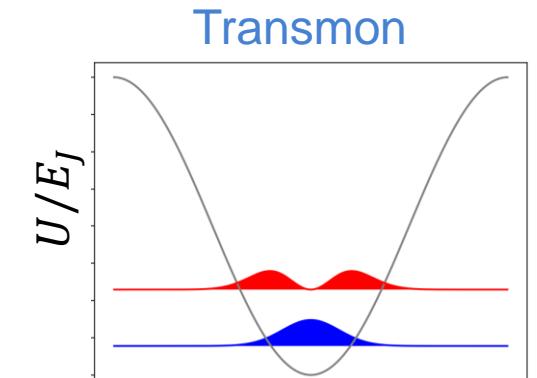
# Protected qubit

*Engineering non-local ground-states*

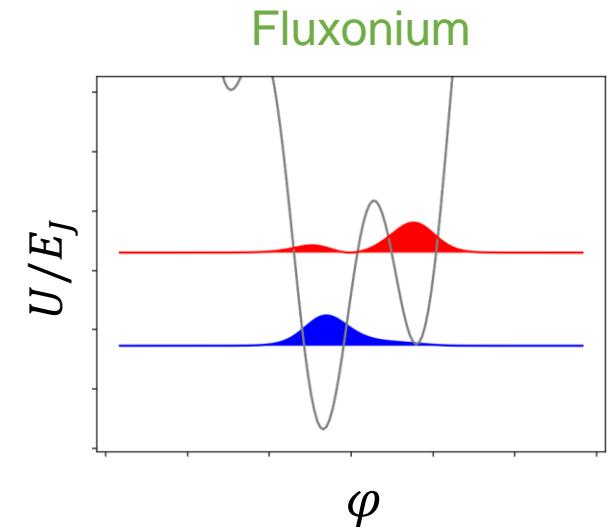
# Towards non-local and non-overlapping ground states



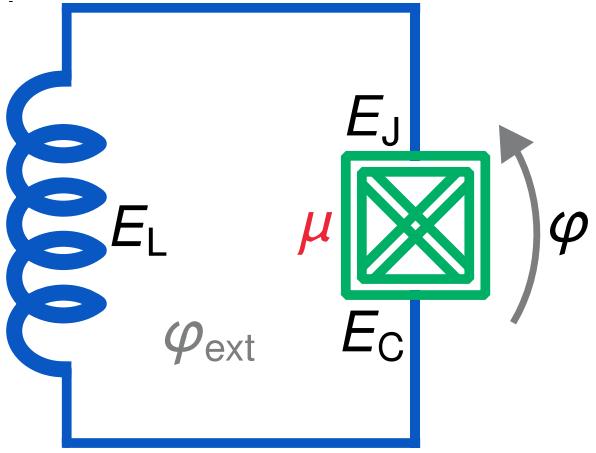
# Mendeleev table of artificial atoms



$$H = 4E_C N^2 + \frac{1}{2} E_L (\varphi - \varphi_{ext})^2 - E_J \cos(\varphi)$$

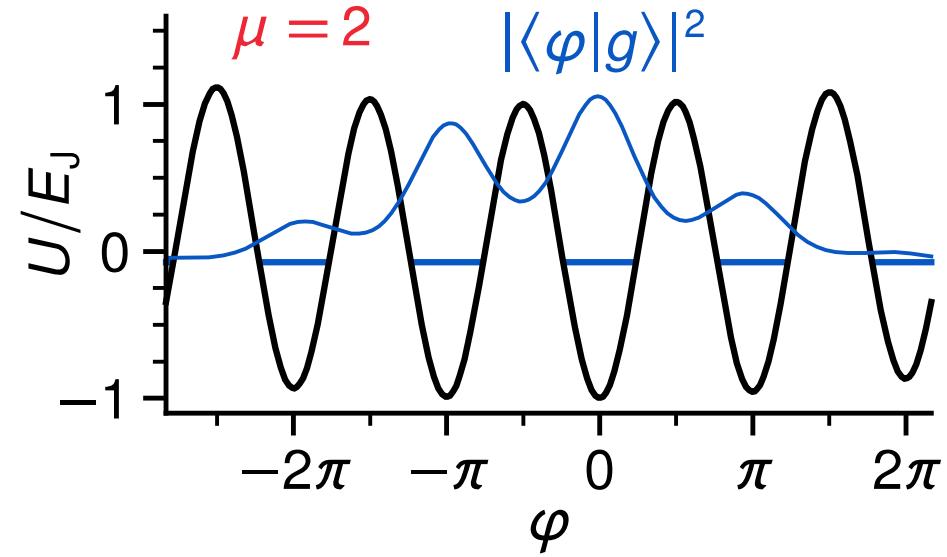
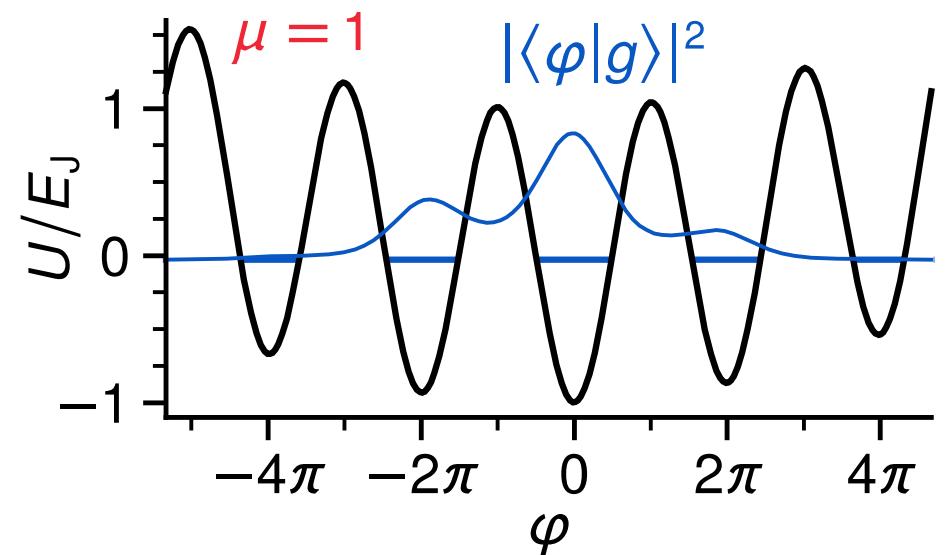


# The generalized Josephson element

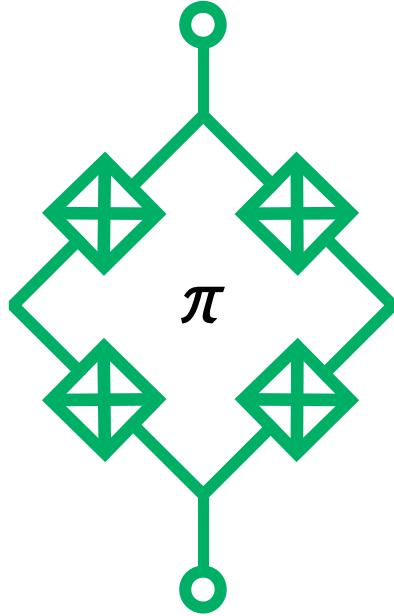


$$H = 4E_C \left( \frac{N}{\mu} \right)^2 + \frac{1}{2} E_L (\varphi - \varphi_{\text{ext}})^2 - E_J \cos(\mu\varphi)$$

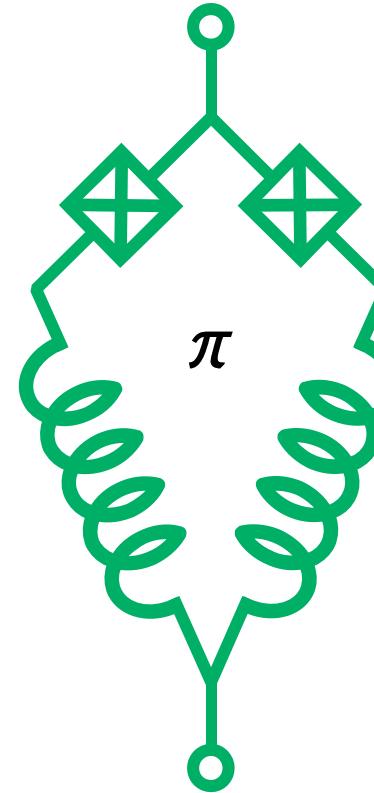
$$\cos(\mu\varphi) = \frac{1}{2} \sum_{N=-\infty}^{\infty} (|N\rangle\langle N + \mu| + |N + \mu\rangle\langle N|)$$



# Two-Cooper-pair tunneling elements



Rhombus



KITE  
(Kinetic Interference  
coTunneling Element)

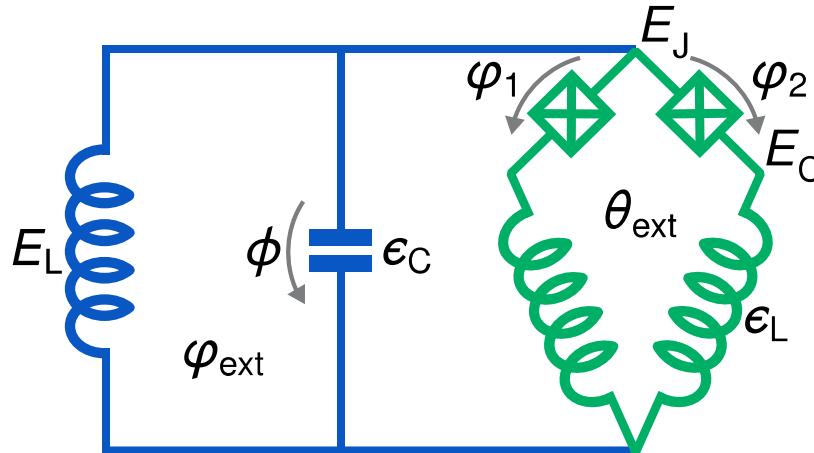
Blatter, Geshkenbein, and Ioffe. *PRB* (2001)  
Gladchenko et al. *Nature Physics* (2009)  
Douçot and Ioffe. *RPP* (2012)

Bell et al. *PRL* (2014)  
Smith et al. *npj Quantum Info* (2020)

# Model reduction: Born-Oppenheimer approximation

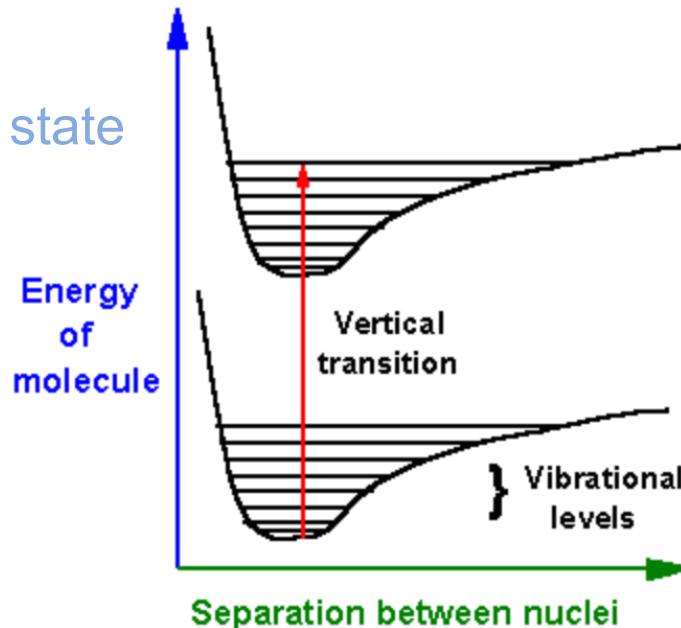
Target regime :

$$E_L \lesssim \epsilon_L \ll E_J \approx E_C \lesssim \epsilon_c$$



$$\varphi_{\Sigma} = \frac{1}{2}(\varphi_1 + \varphi_2)$$
$$\varphi_{\Delta} = \frac{1}{2}(\varphi_1 - \varphi_2)$$

$\phi$ : high-frequency “electronic”  
degree of freedom  
→ freeze in quantum ground state

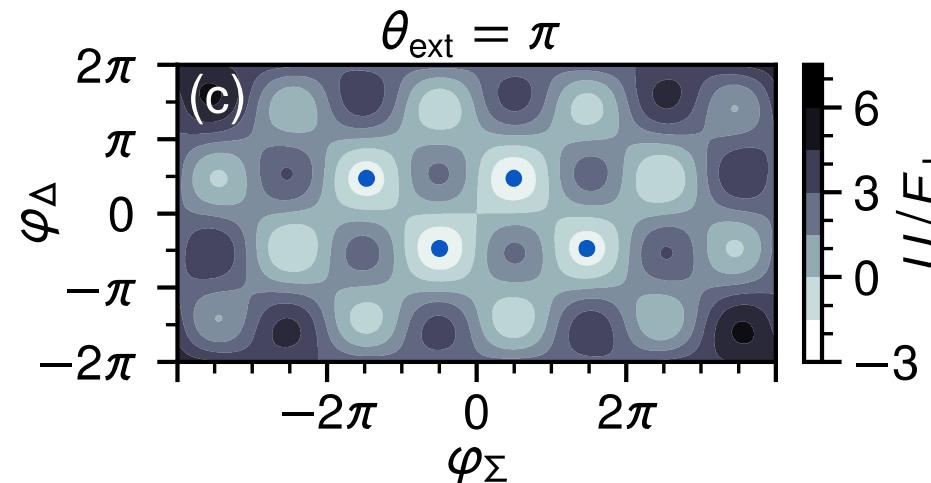


$\varphi_{\Sigma,\Delta}$ : low-frequency “nuclear”  
degrees of freedom  
→ temporarily fix to classical values

# Model reduction: tight-binding approximation

Low-energy Hamiltonian has two degrees of freedom:

$$H_n = 2E_C(N_\Sigma^2 + N_\Delta^2) + \frac{E_L \epsilon_L}{E_L + 2\epsilon_L} (\varphi_\Sigma + \varphi_{\text{ext}} + \frac{1}{2}\theta_{\text{ext}})^2 + \epsilon_L (\varphi_\Delta - \frac{1}{2}\theta_{\text{ext}})^2$$
$$- 2E_J \cos \varphi_\Sigma \cos \varphi_\Delta$$

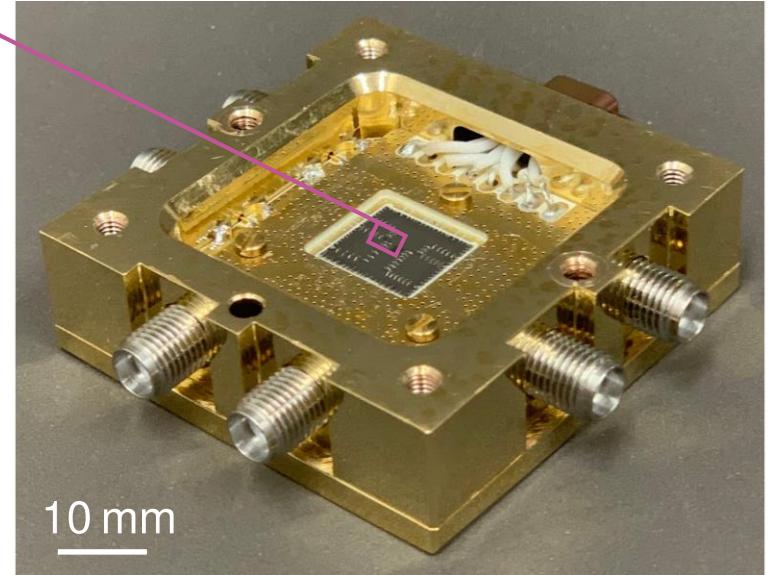
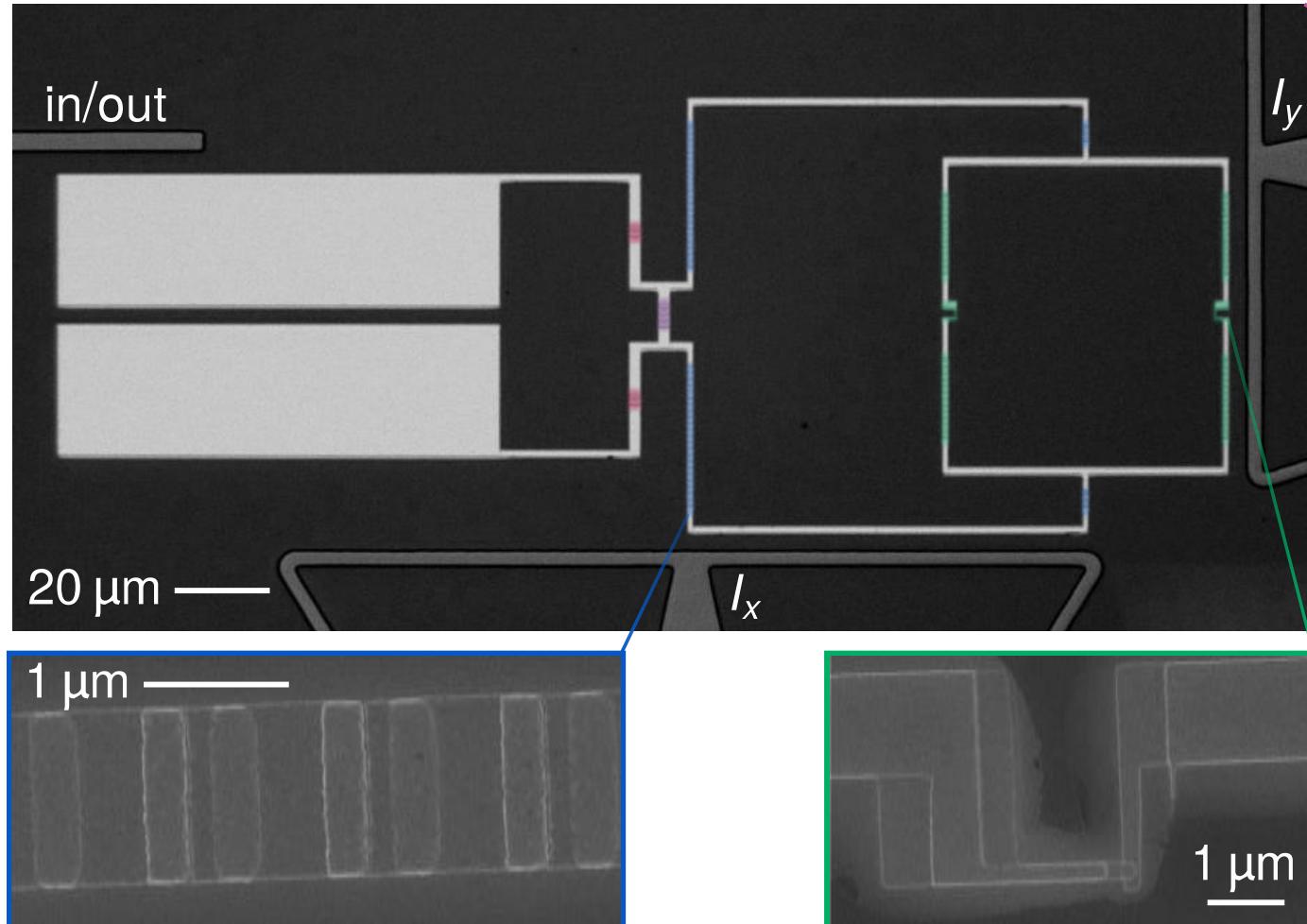


$$H_\pi^{\text{tight-binding}} = \sum_s \frac{E_L \epsilon_L}{E_L + 2\epsilon_L} \left( s\pi + \frac{\pi}{2} + \varphi_{\text{ext}} \right)^2 |s\rangle\langle s| + \sum_s \frac{1}{2} \Gamma (|s\rangle\langle s+1| + |s+1\rangle\langle s|)$$

$$H_\pi = E_C N^2 + \frac{E_L \epsilon_L}{E_L + 2\epsilon_L} (\varphi + \varphi_{\text{ext}})^2 + E_J \cos 2\varphi$$

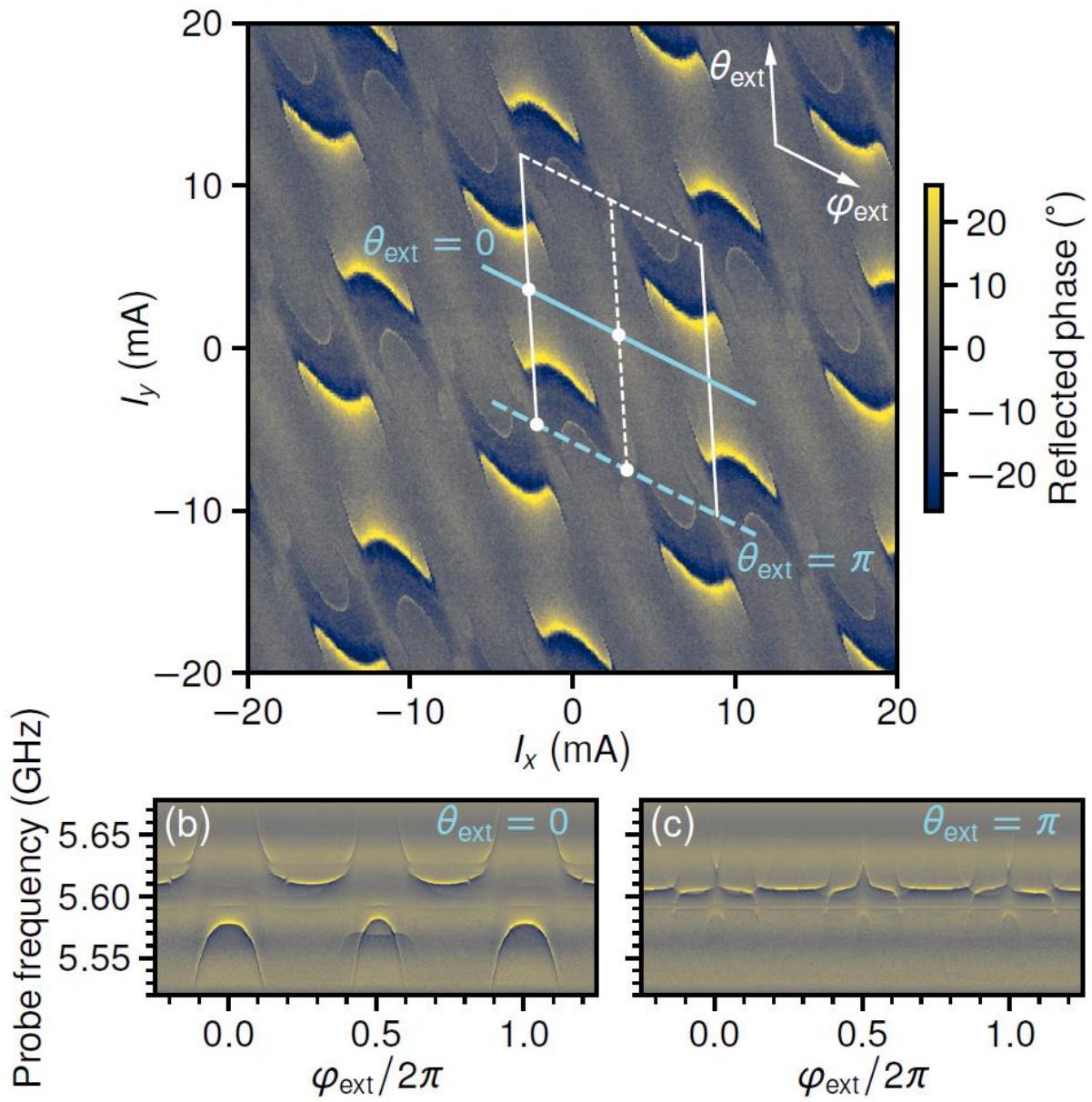
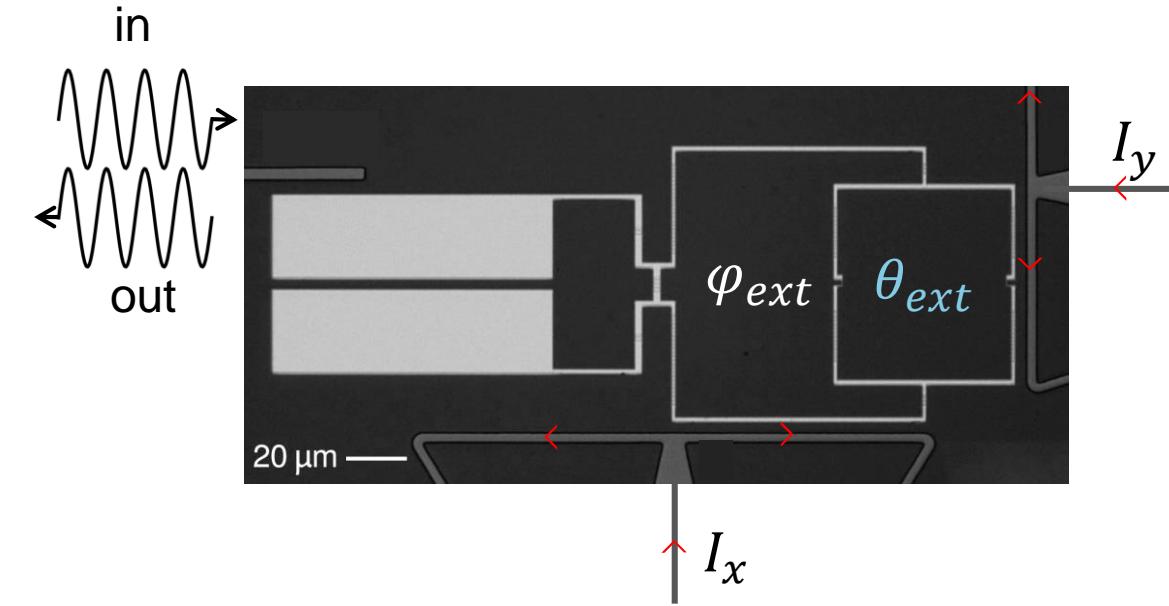
$$\Gamma = \frac{4}{\sqrt{\pi}} (8E_J^3 E_C)^{1/4} \exp\left(-\sqrt{\frac{8E_J}{E_C}}\right)$$

# Experimental implementation



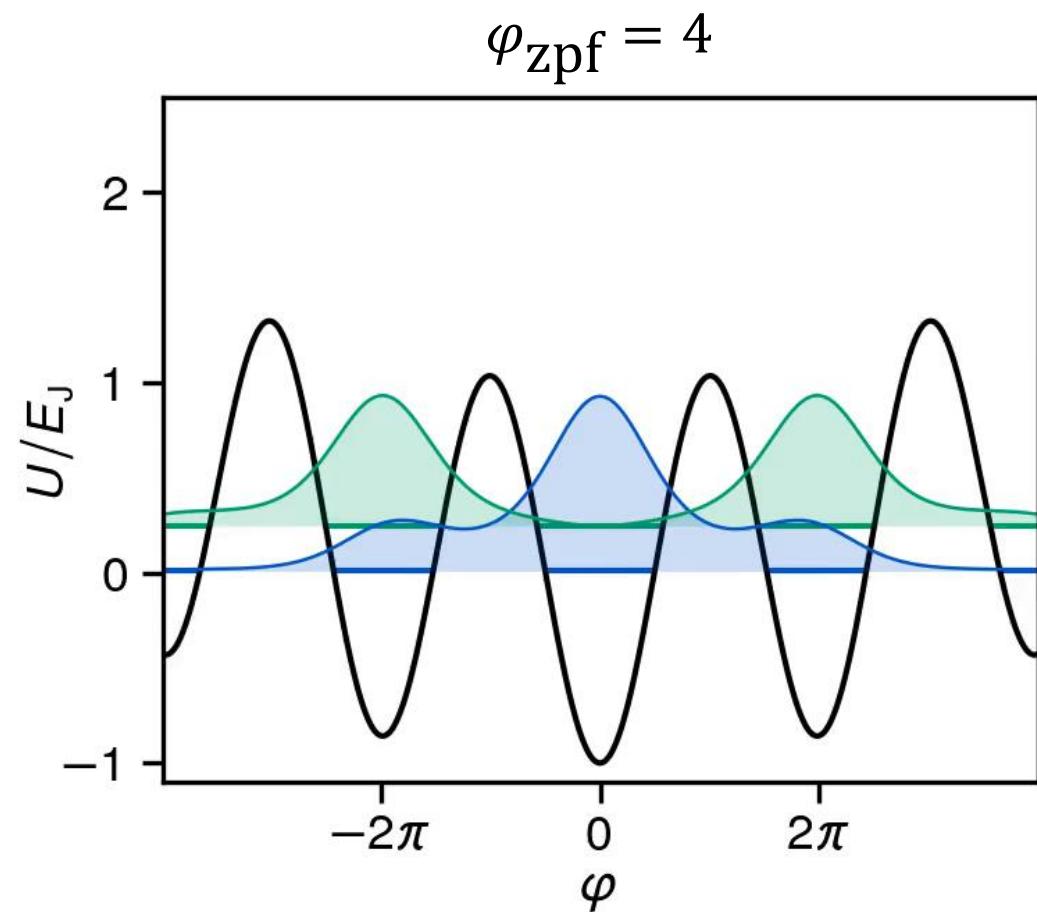
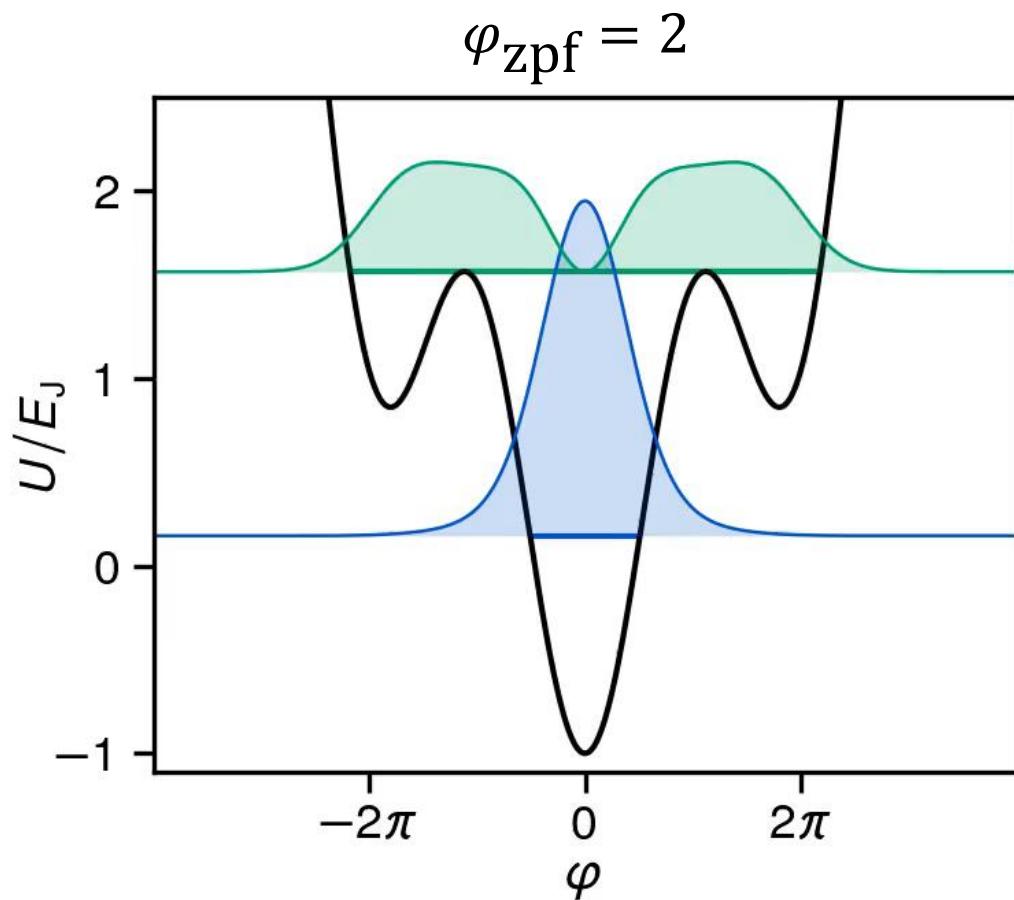
215 total junctions  
2 loops  
3 control lines  
4 electromagnetic modes

# External flux dependance

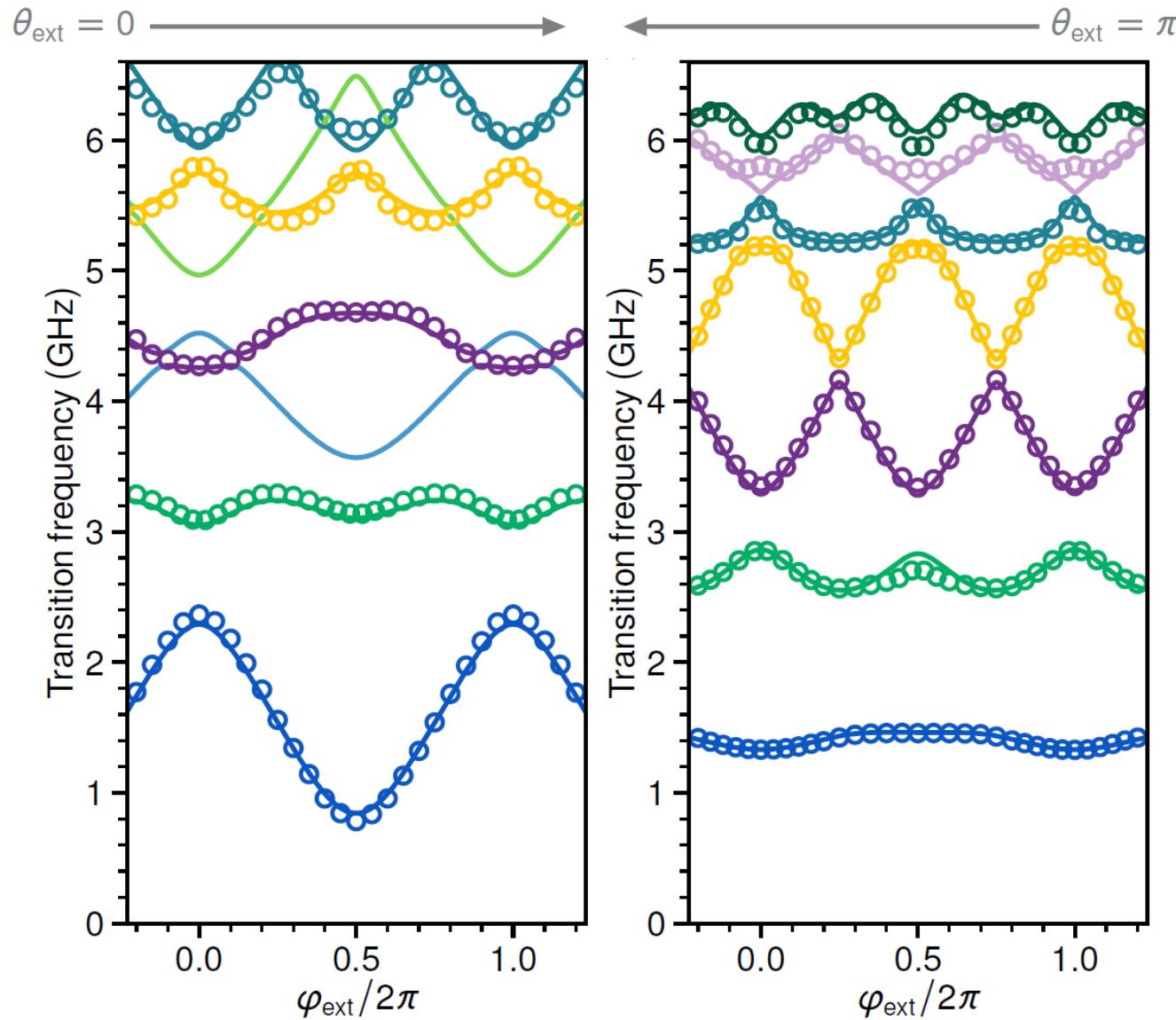


# Flux dispersion measures phase fluctuations

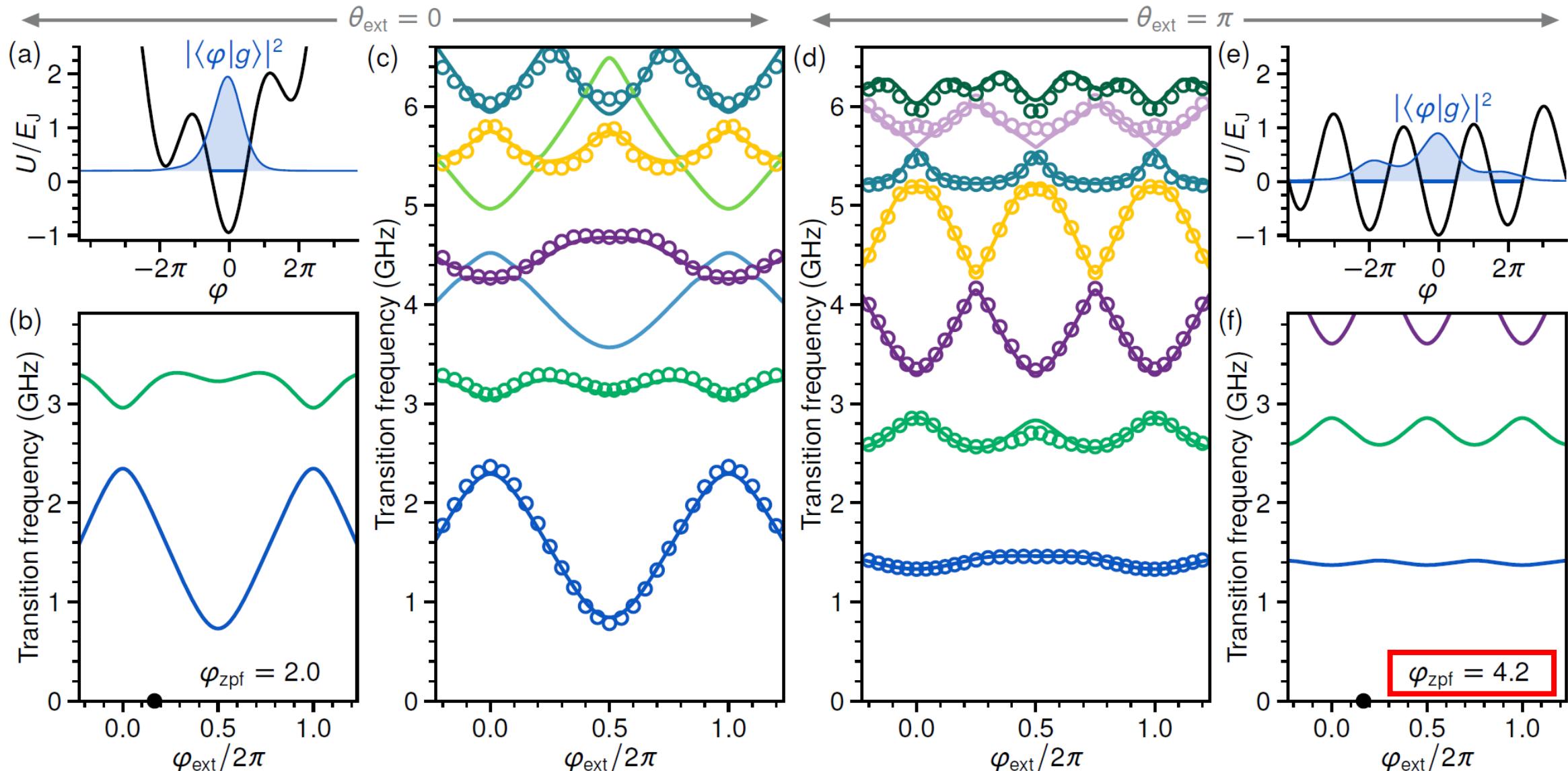
$$\varphi_{\text{zpf}} \equiv \left( \frac{2E_C}{E_L} \right)^{1/4}$$



# Measured transition energies



# Measured transition energies

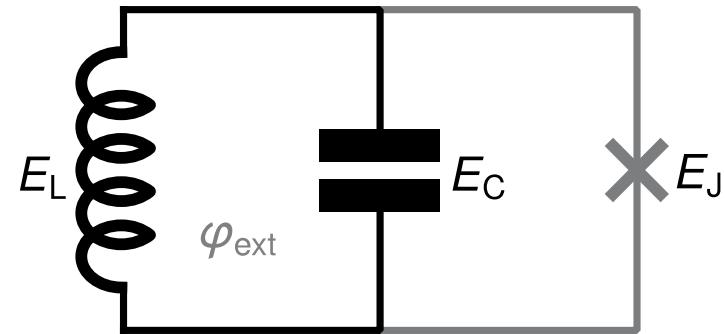


# Exploring a new regime of quantum optics

## *Spectral signature of high-order photon processes*

Smith\* & Borgognoni\* *et. al* in preparation

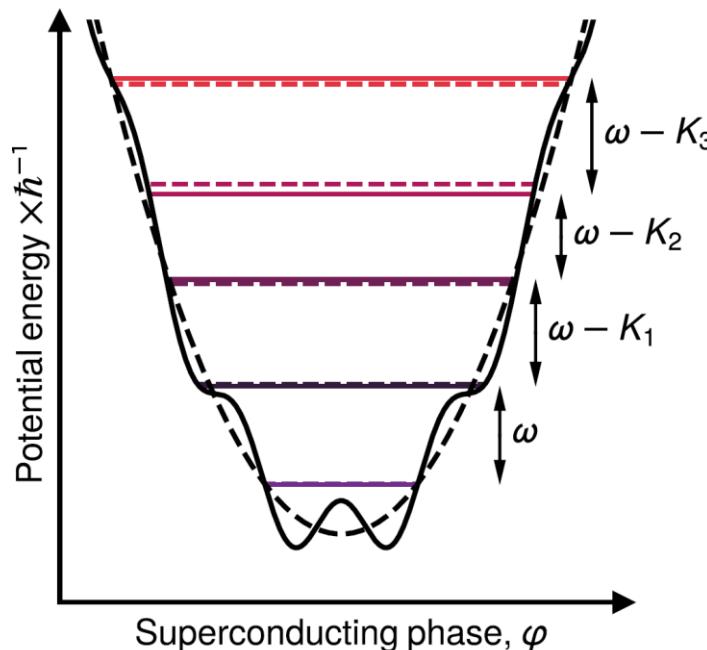
# Nonlinear oscillators in superconducting circuits



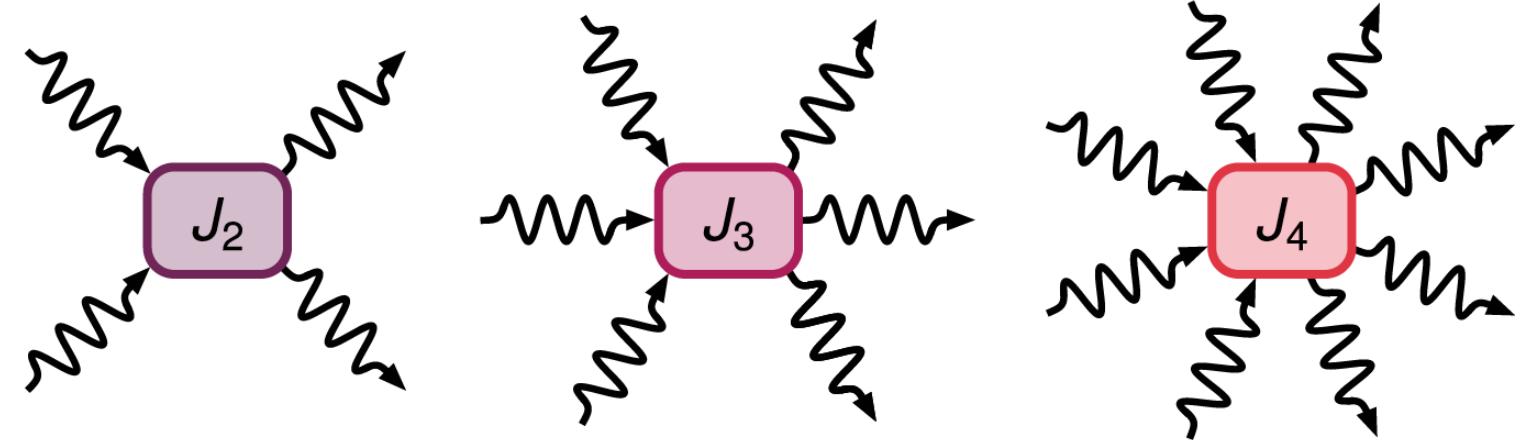
$$H = \hbar\omega_0 a^\dagger a - E_J \cos(\varphi_{\text{zpf}}(a + a^\dagger))$$
$$\approx \hbar\omega a^\dagger a + J_2(a^\dagger)^2 a^2 + J_3(a^\dagger)^3 a^3 + J_4(a^\dagger)^4 a^4 + \dots$$

Small Josephson energy

$$E_J \ll \hbar\omega$$



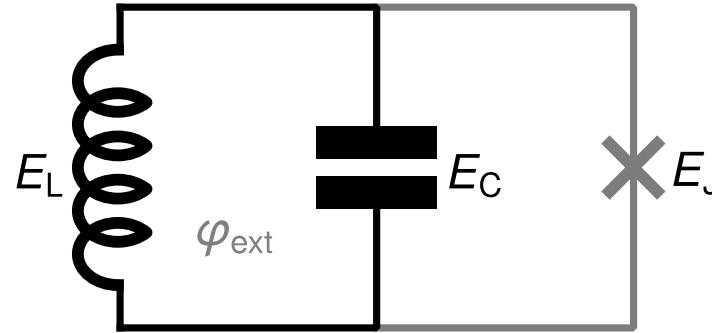
$$J_n \propto \varphi_{\text{zpf}}^{2n}$$



# Nonlinear oscillators in superconducting circuits

Small Josephson energy

$$E_J \ll \hbar\omega$$

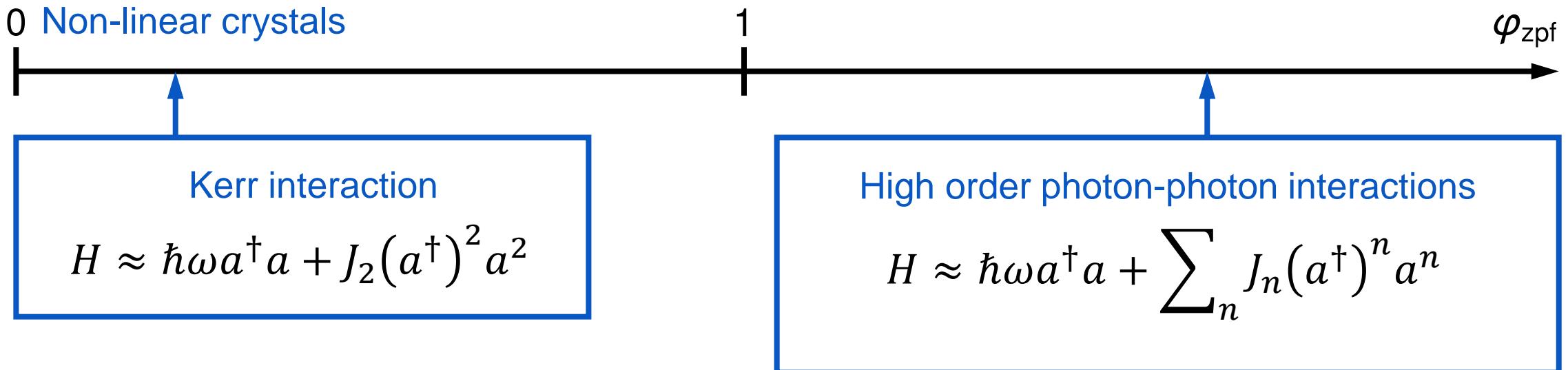


$$\hbar\omega_0 = \sqrt{8E_L E_C}$$

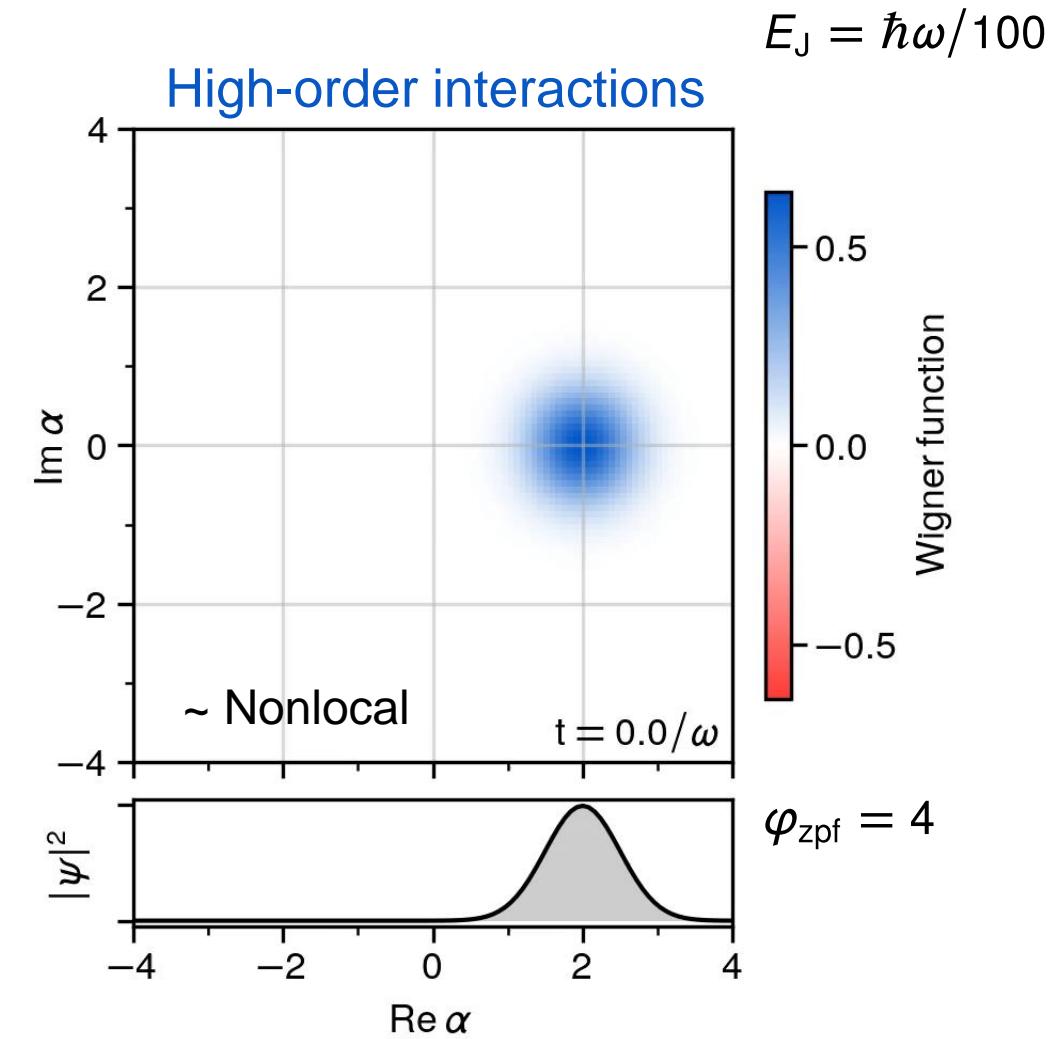
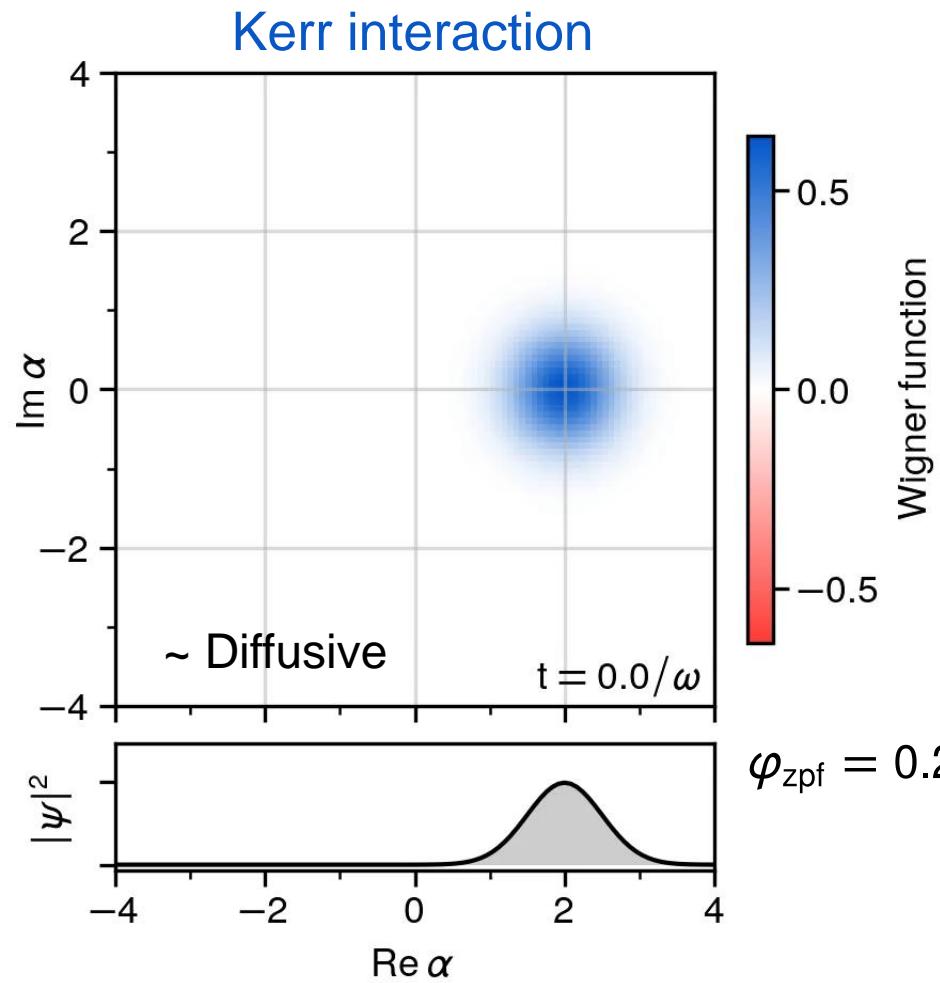
$$\varphi_{\text{zpf}} = \left(\frac{2E_C}{E_L}\right)^{1/4}$$

Transmon  
Amplifiers,  
0 Non-linear crystals

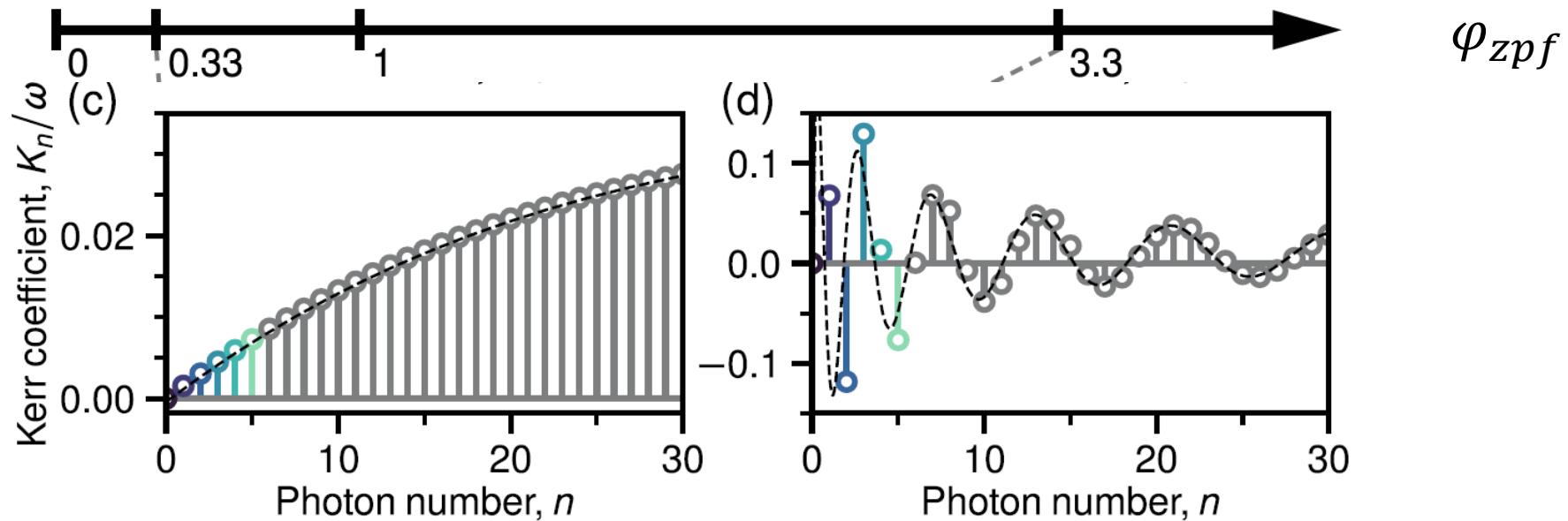
$$H = \hbar\omega_0 a^\dagger a - E_J \cos(\varphi_{\text{zpf}}(a + a^\dagger))$$



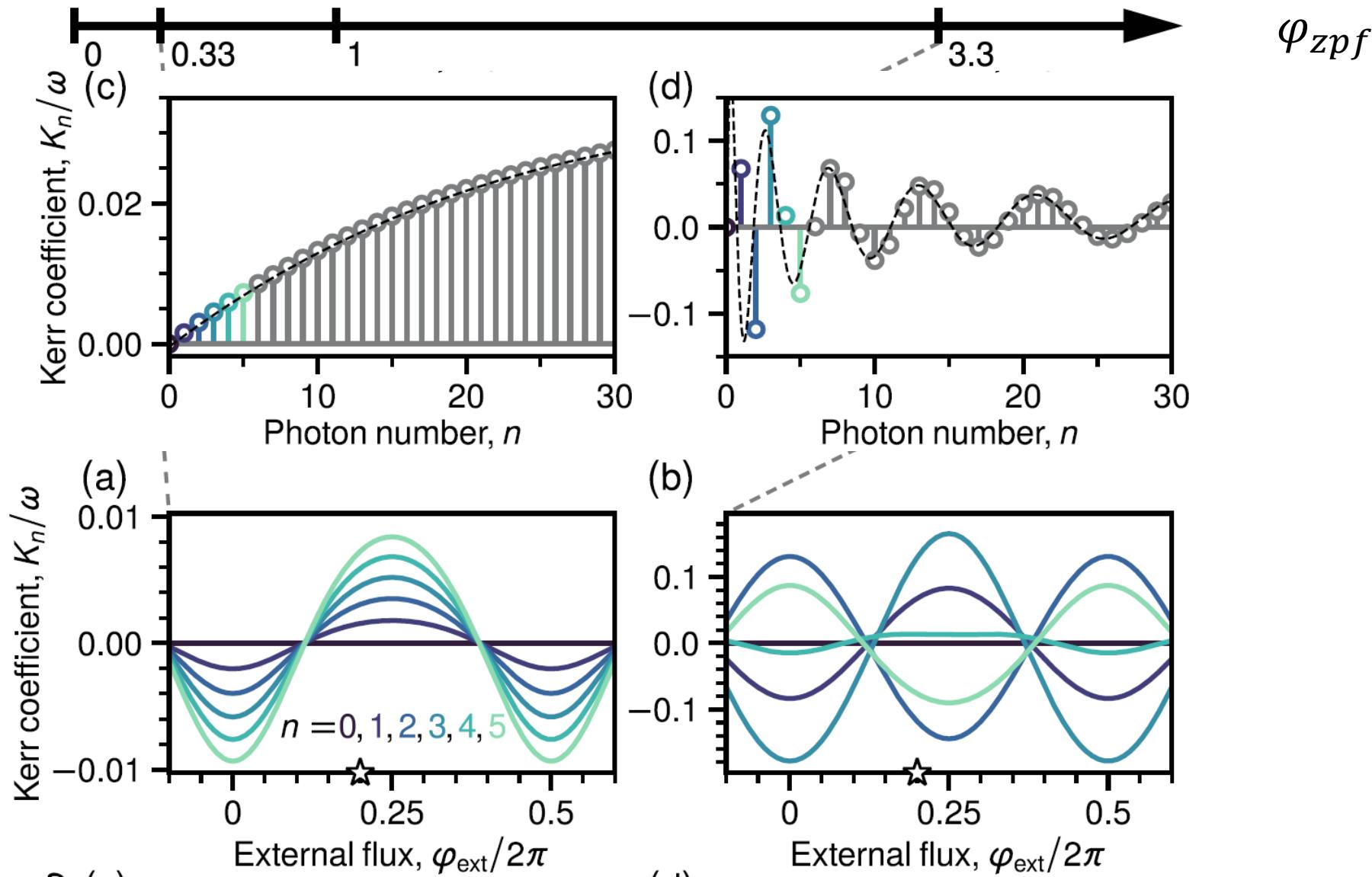
# Time evolution of an initial coherent state



# Spectra of nonlinear oscillators



# Spectra of nonlinear oscillators



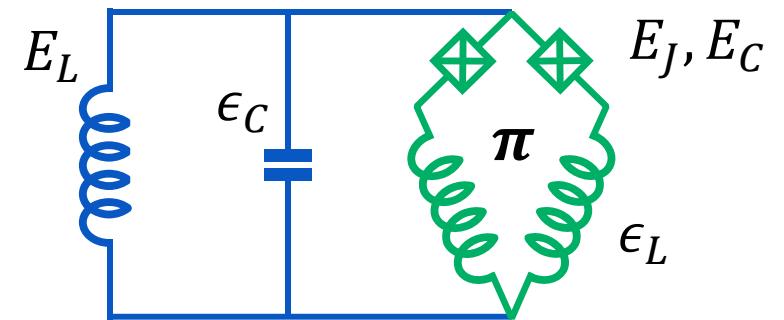
# Experimental realization: two technical challenges

1. Large  $\varphi_{\text{zpf}}$  → ultra-high impedance

KITE in the dc-SQUID-like regime\*  $\epsilon_L \gtrsim E_J$

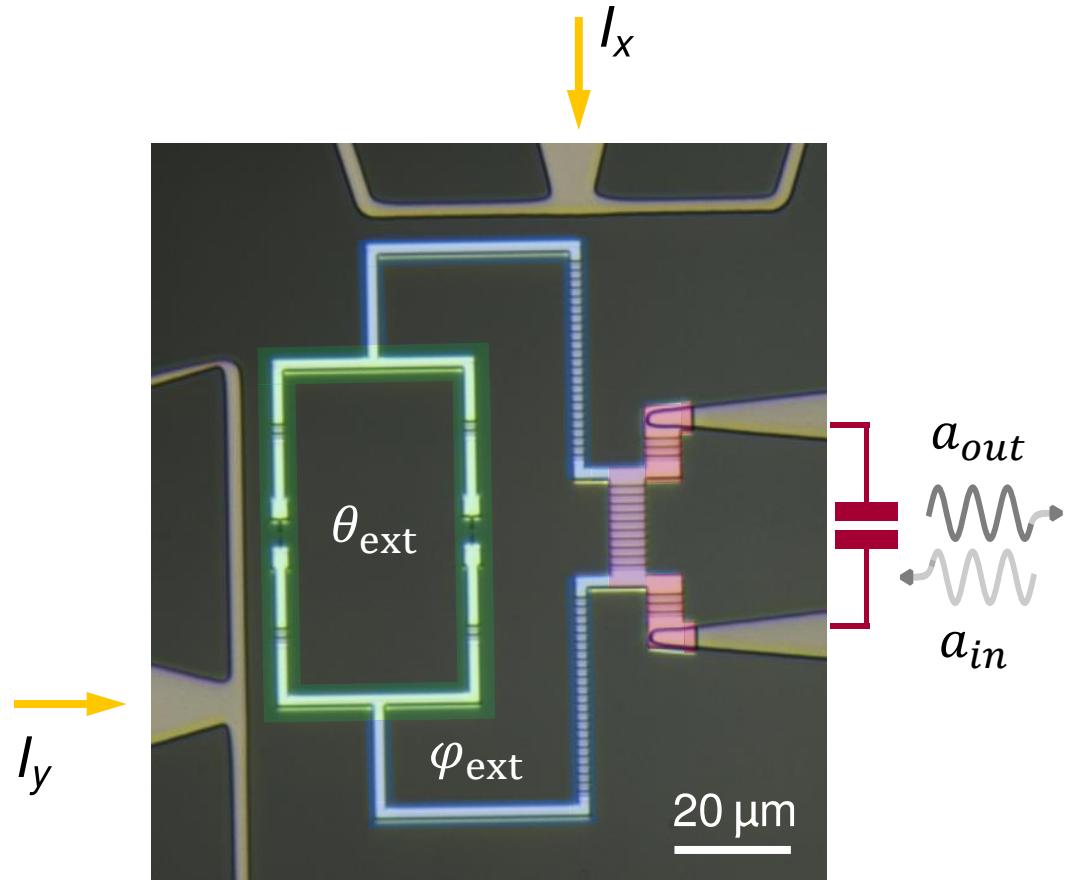
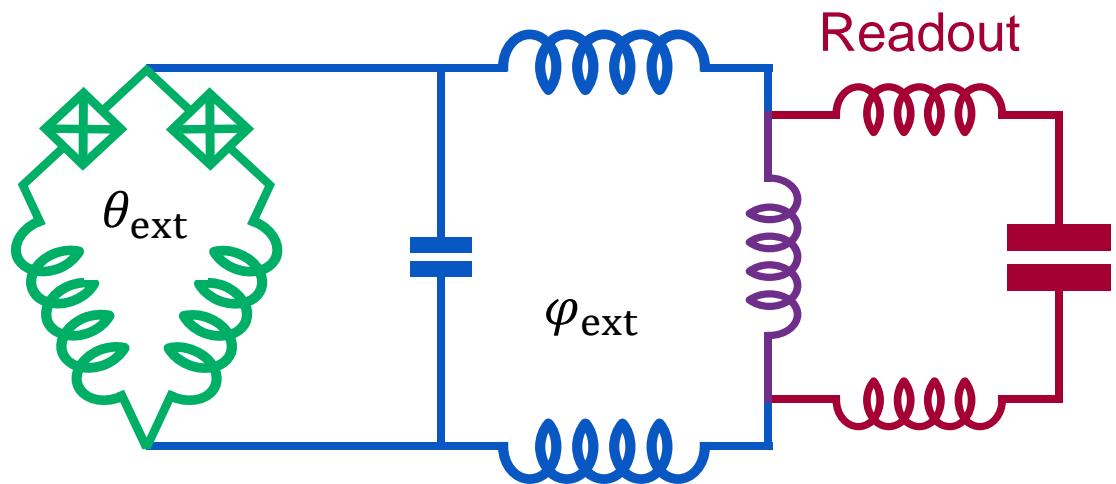
$$\rightarrow \frac{1}{2} \frac{E_J^2}{\epsilon_L} \cos(2\varphi)$$

2. Small  $E_J$  → ultra-small junction



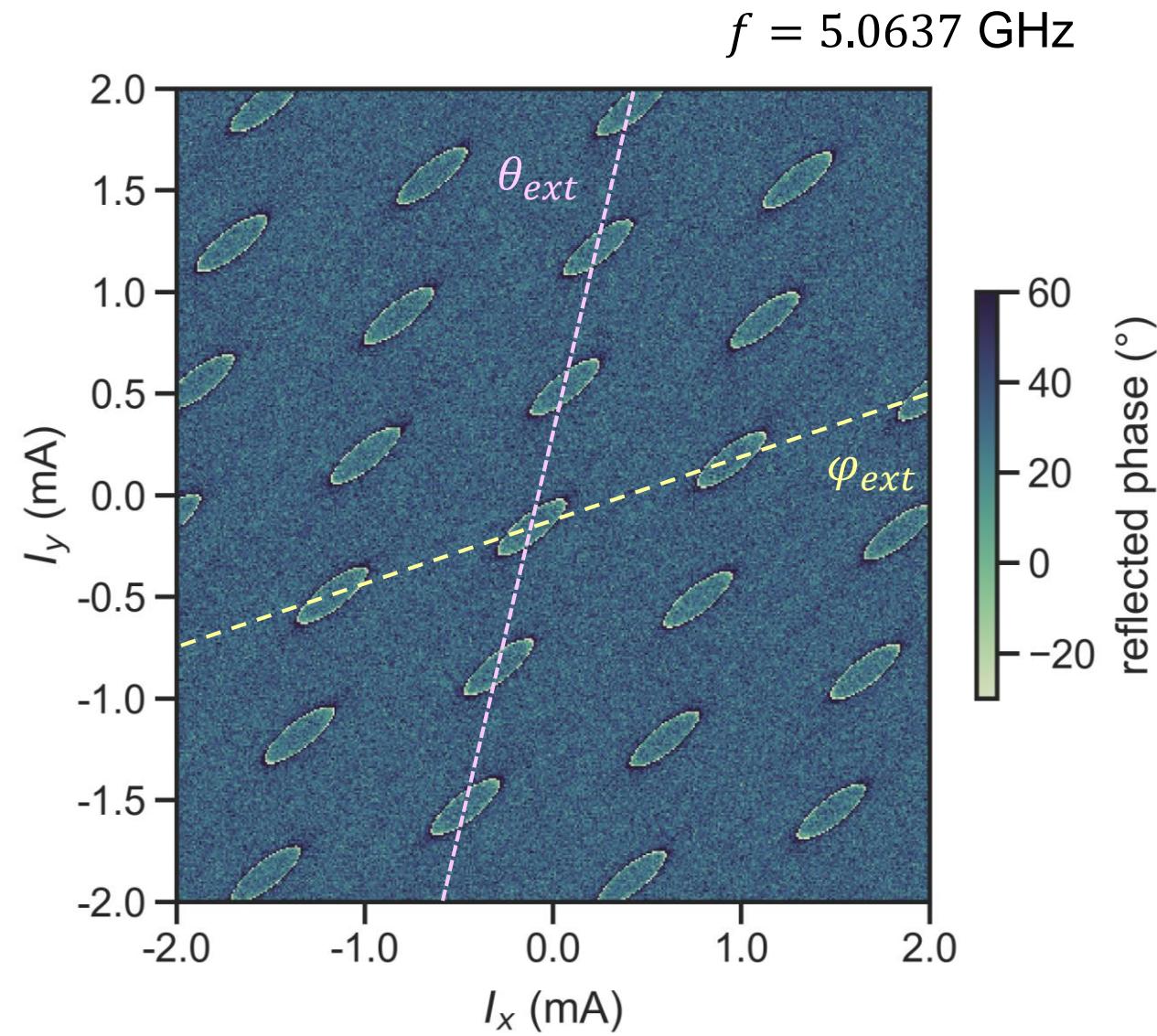
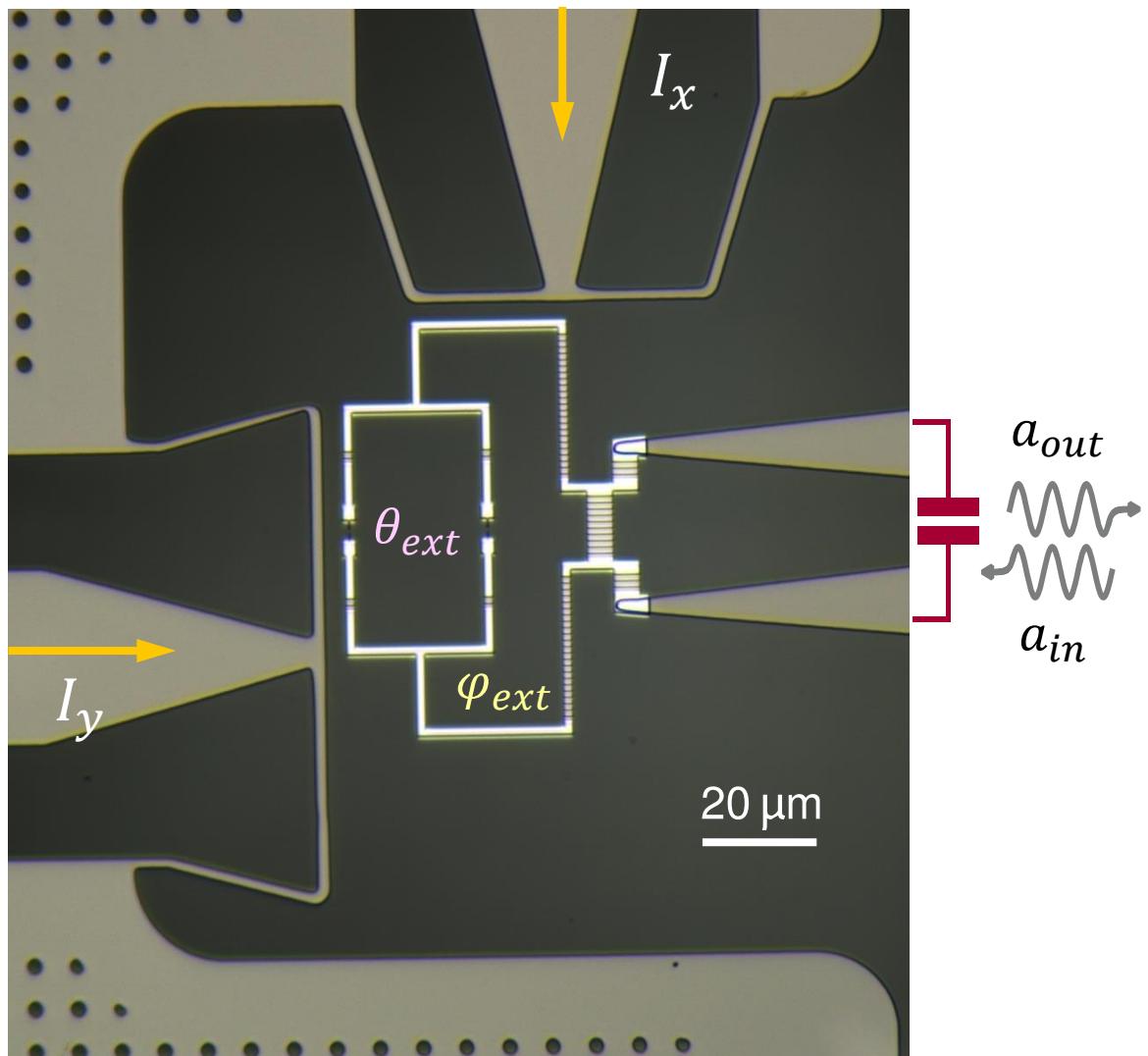
\*opposite regime  $\epsilon_L \ll E_J$  explored in  
Smith et al. PRX (2022)

# Experimental realization: physical device

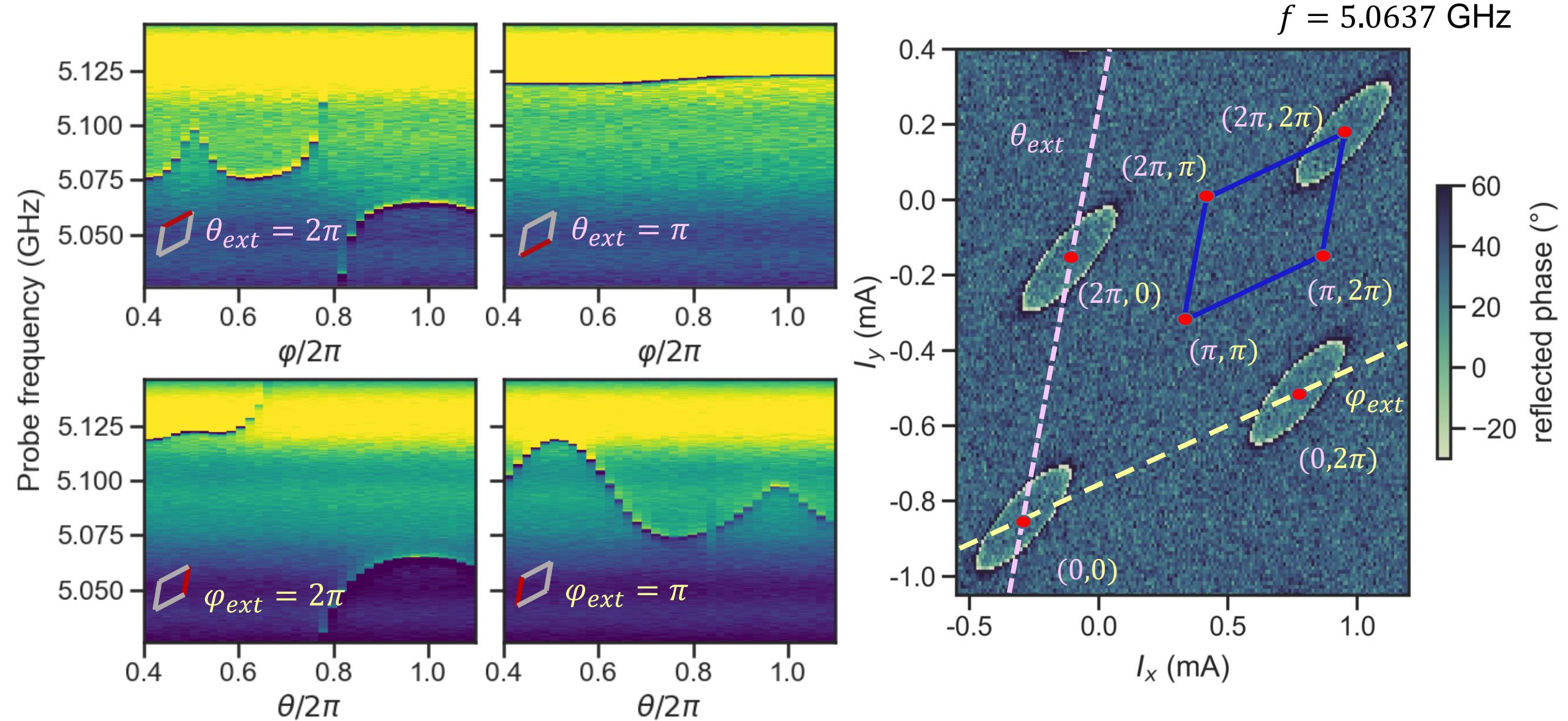


One aluminum double-angle deposition

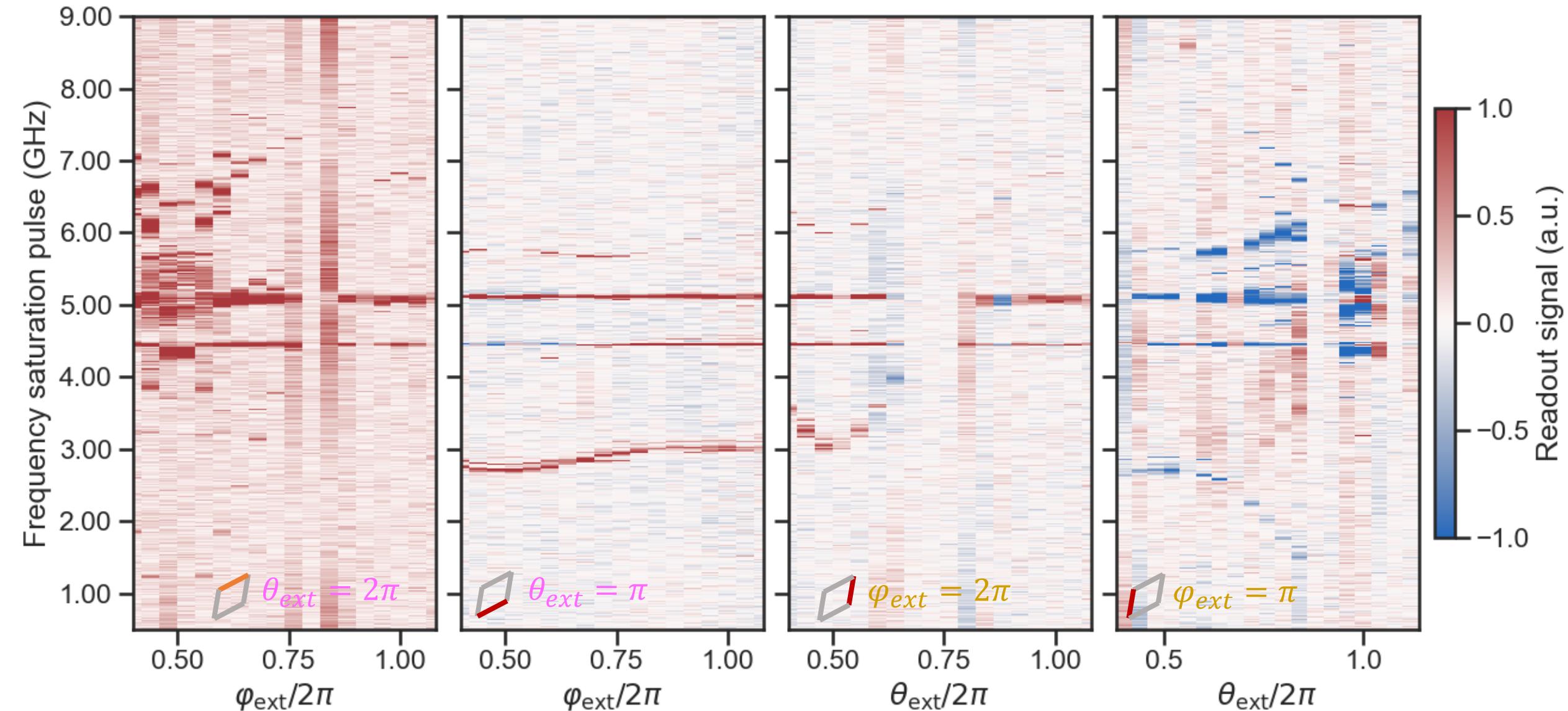
# Readout resonator vs. flux



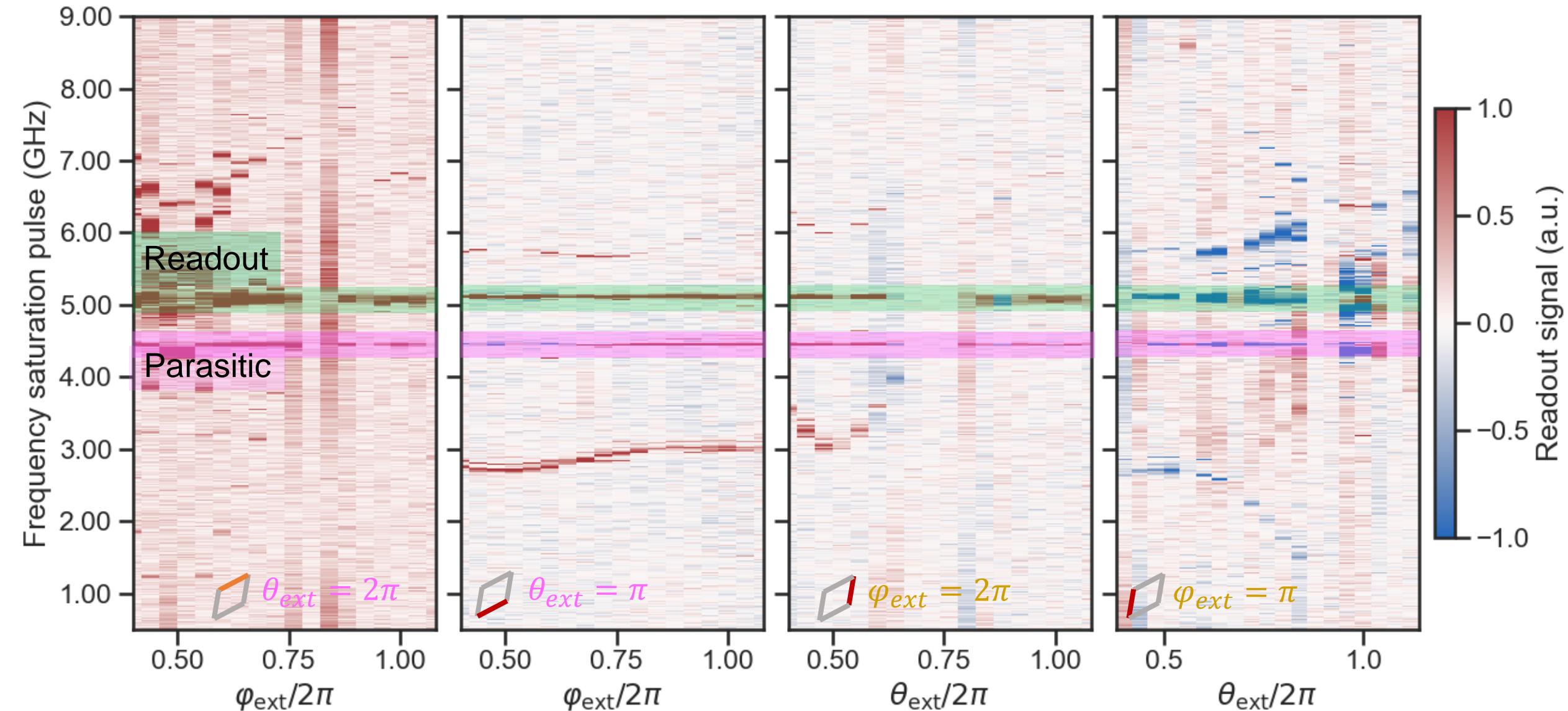
# Readout resonator vs. flux



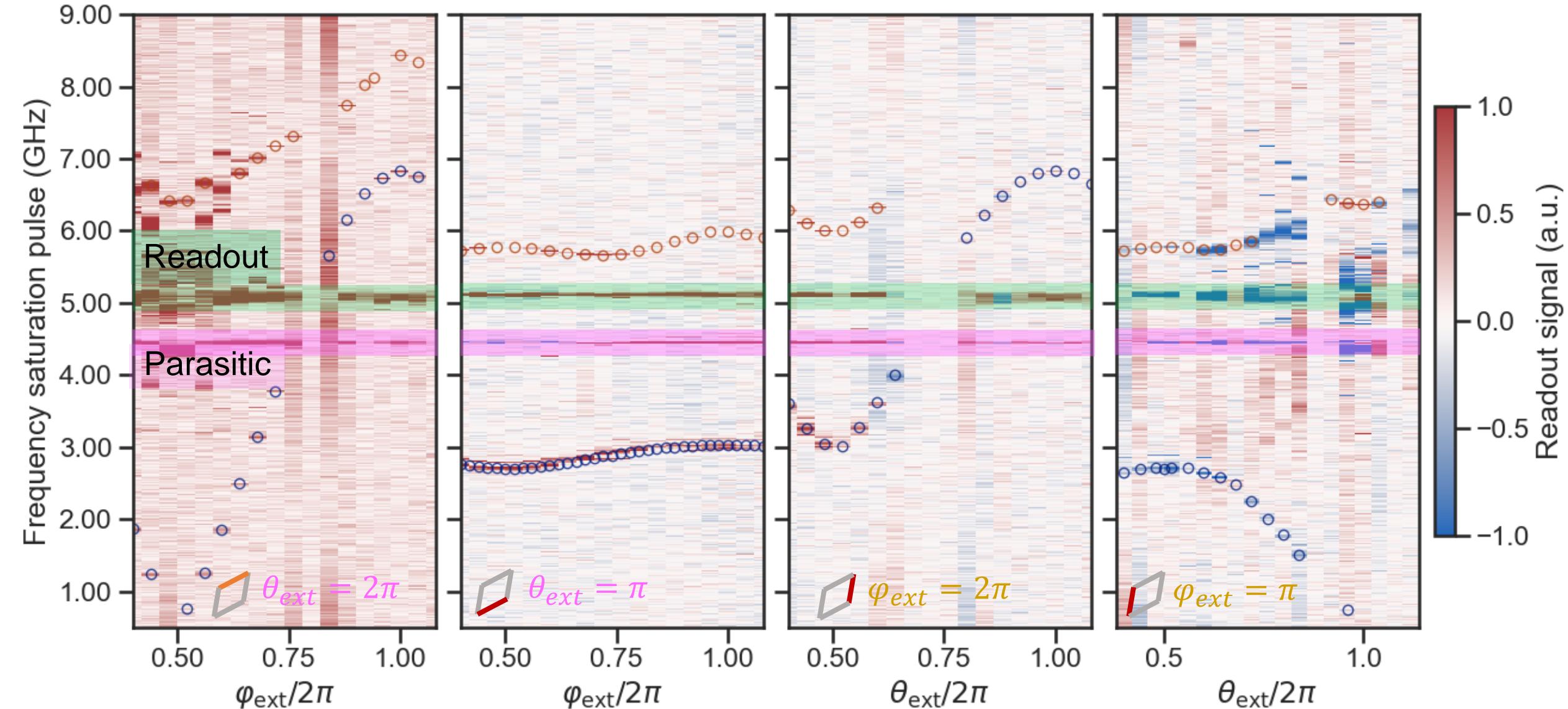
# Transition frequencies vs. flux



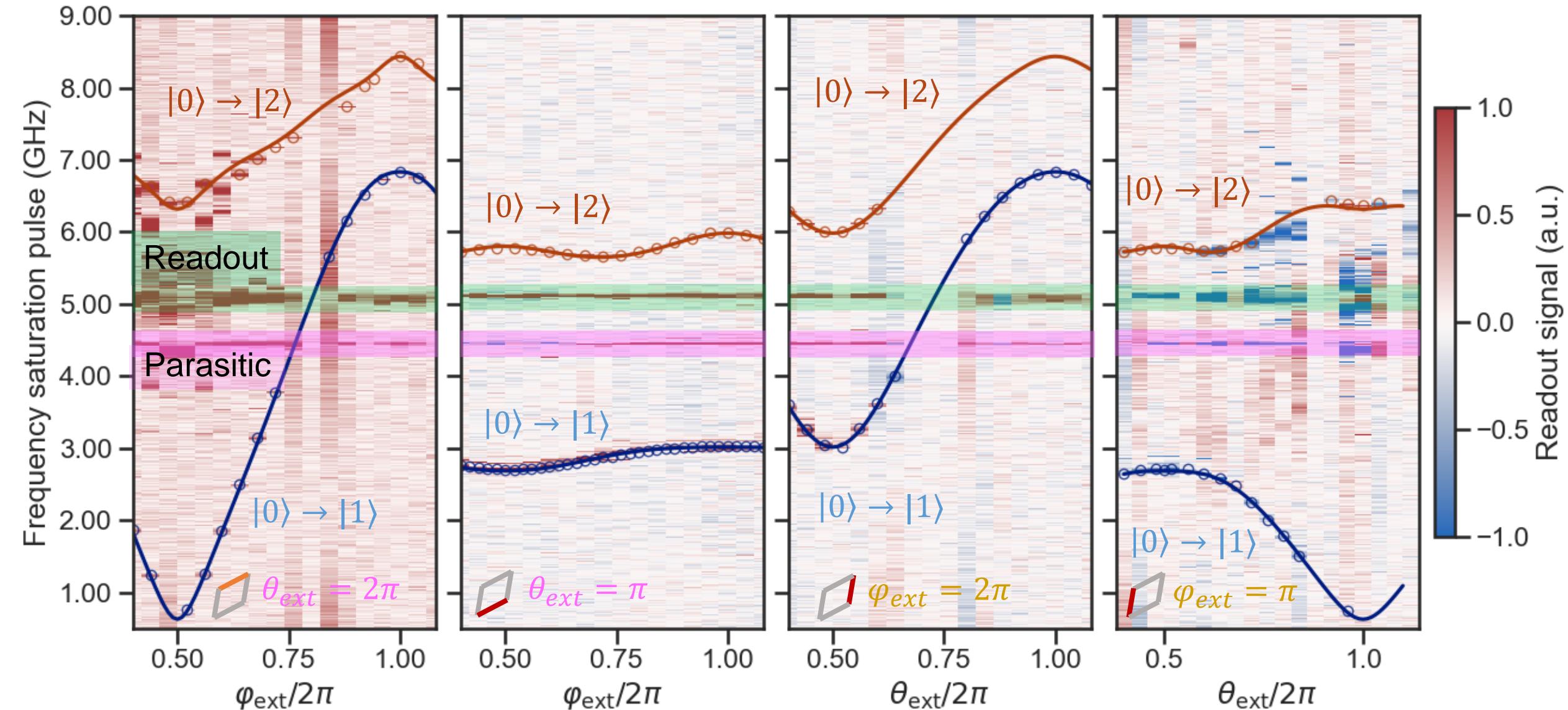
# Transition frequencies vs. flux



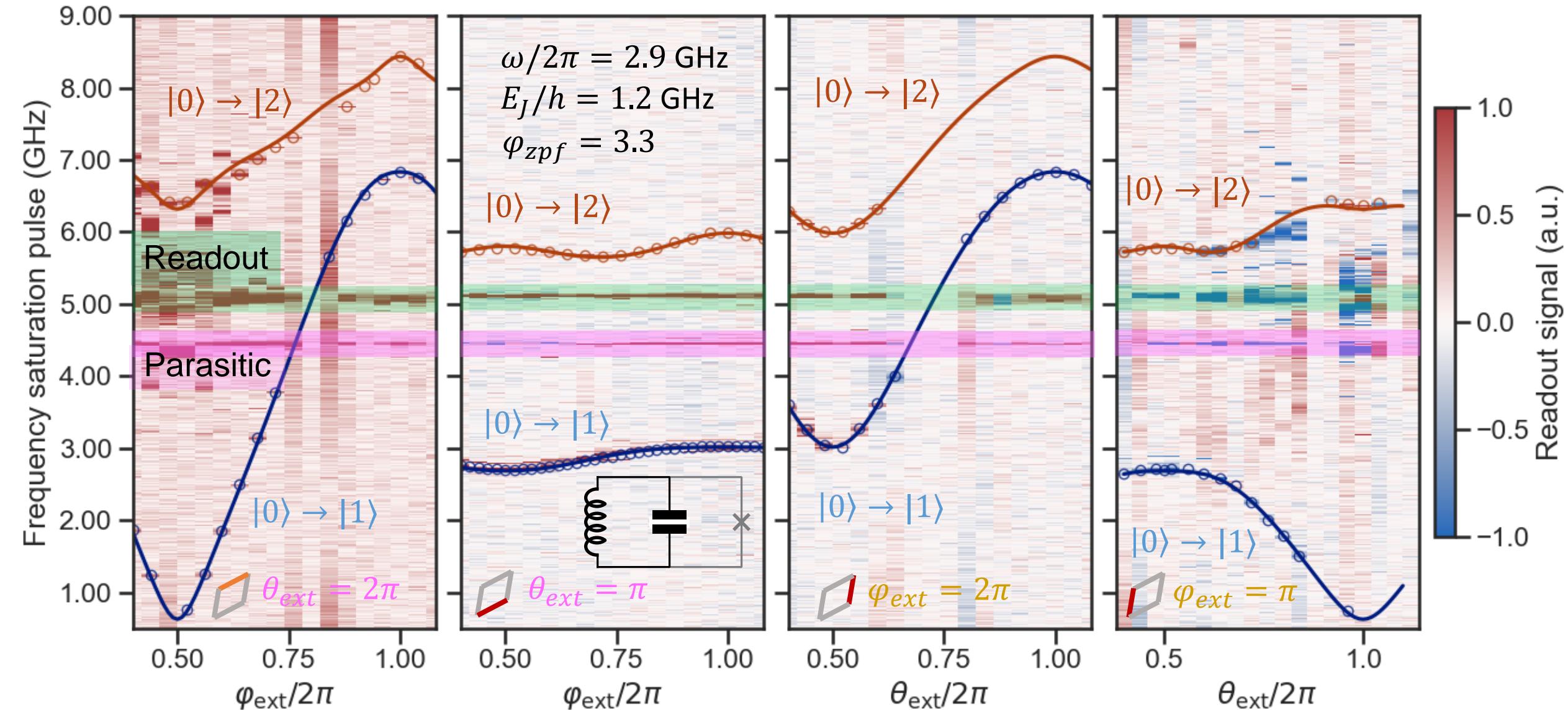
# Transition frequencies vs. flux



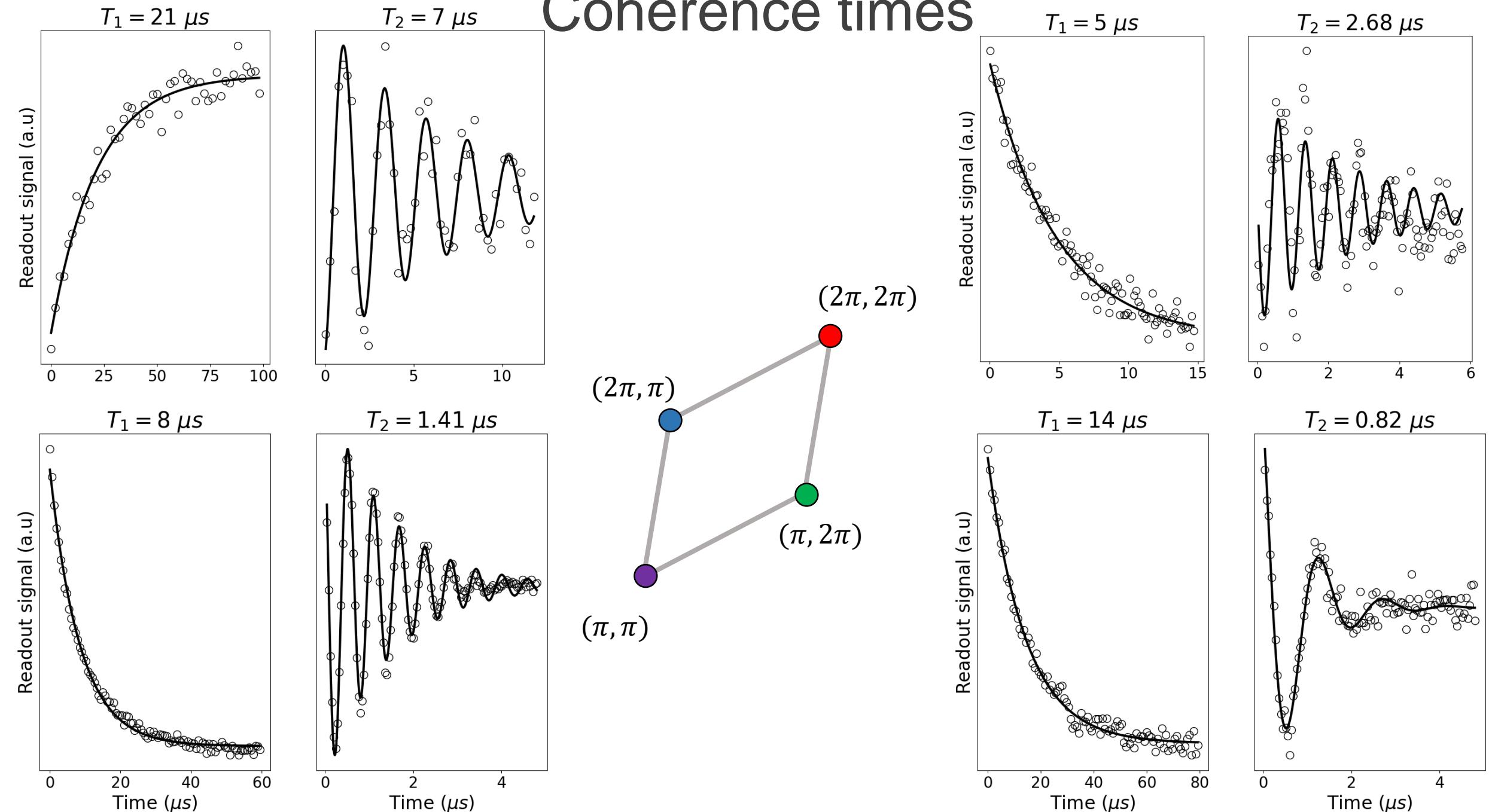
# Transition frequencies vs. flux

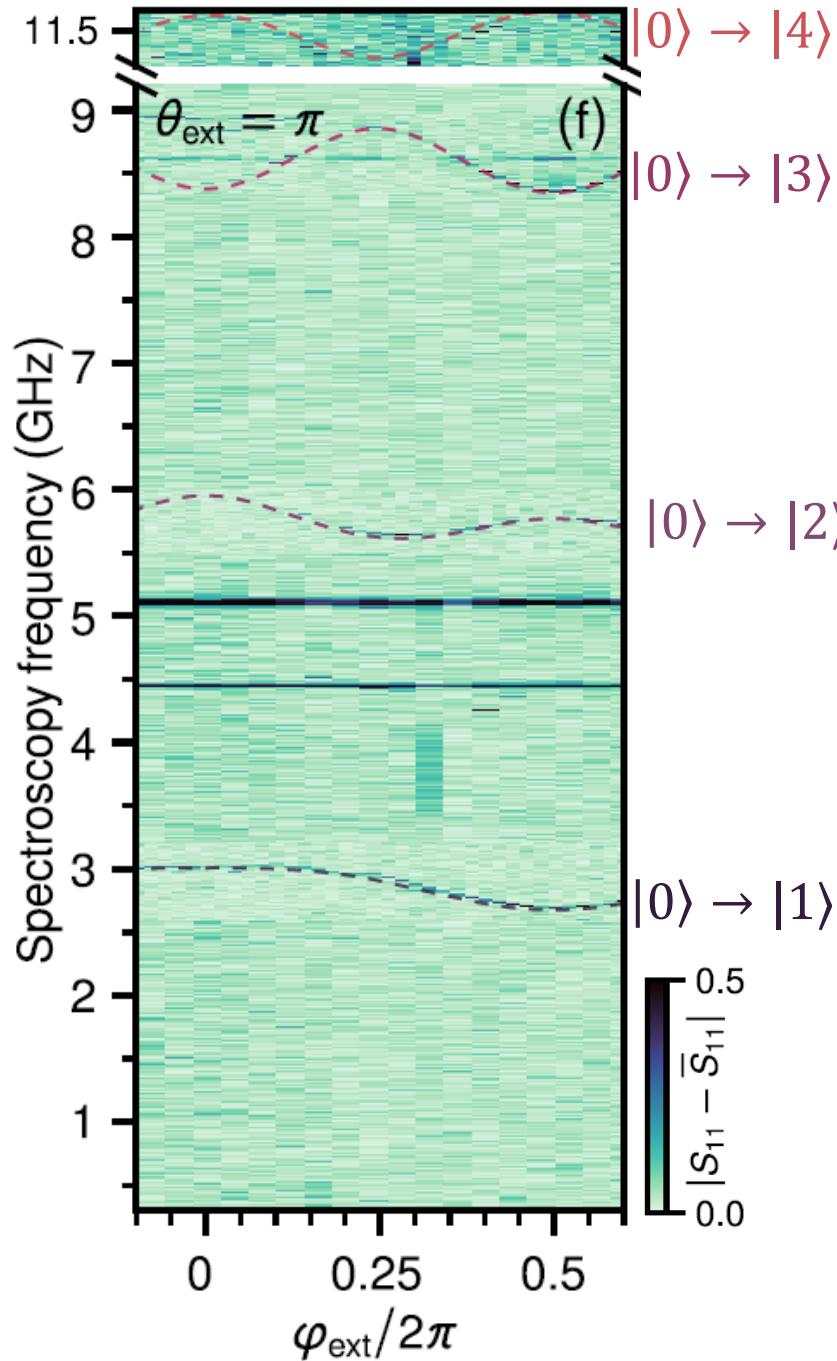


# Transition frequencies vs. flux

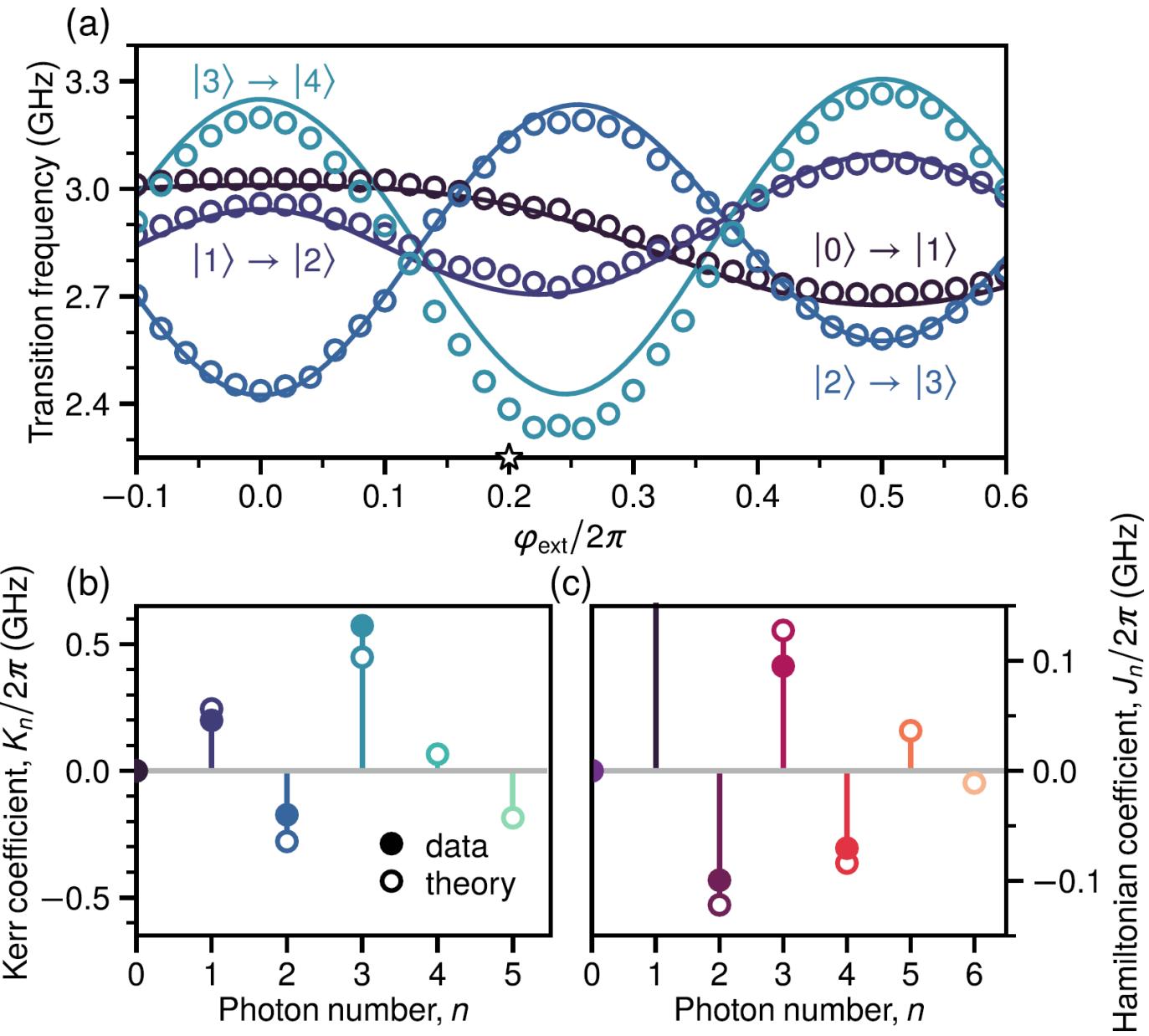


# Coherence times



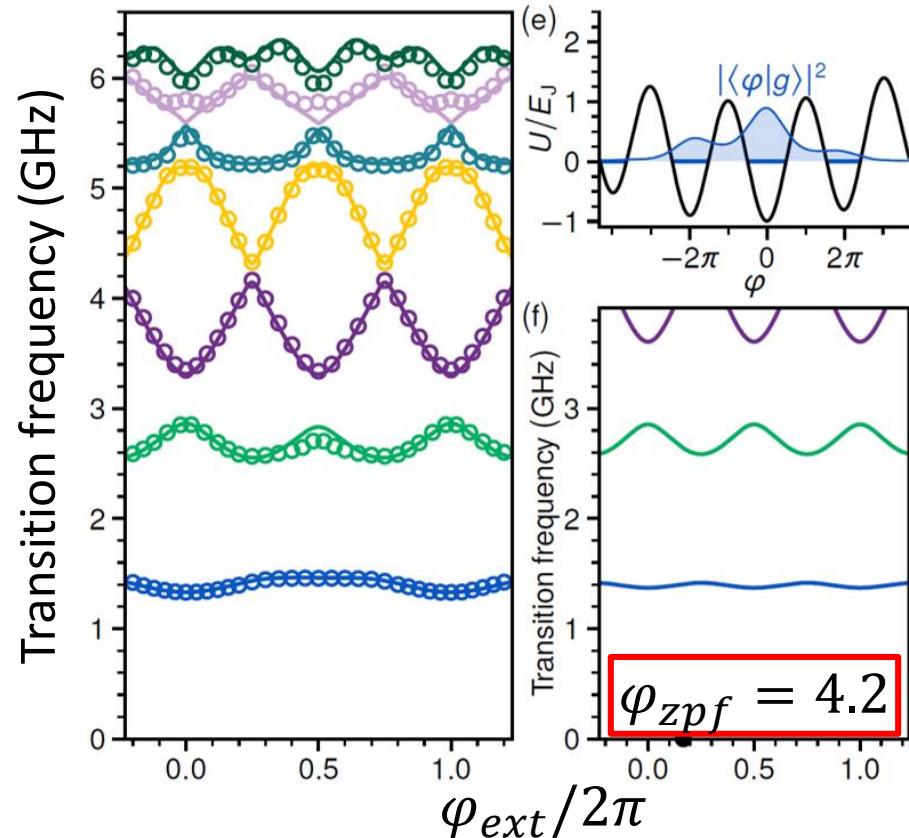


# Flux dependence of $|0\rangle \rightarrow |n\rangle$ at $\theta_{\text{ext}} = \pi$



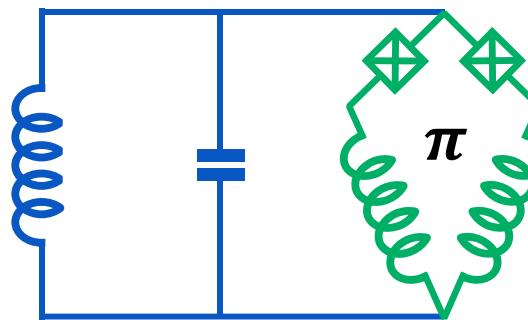
# **Conclusion and perspectives**

# Conclusion

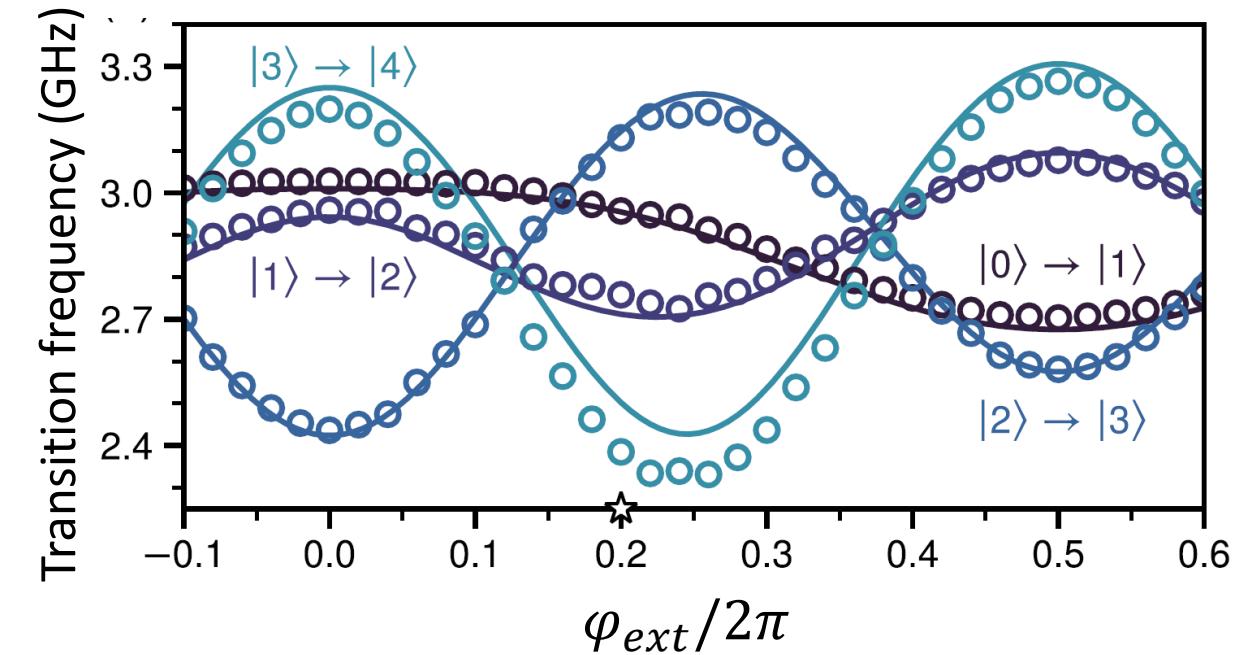
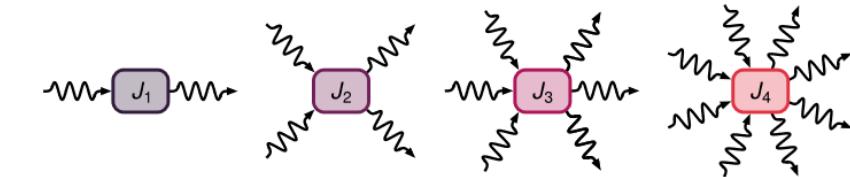


× 10 reduction in flux sensitivity  
× 2 magnification of phase fluctuations

$$\epsilon_L \ll E_J$$

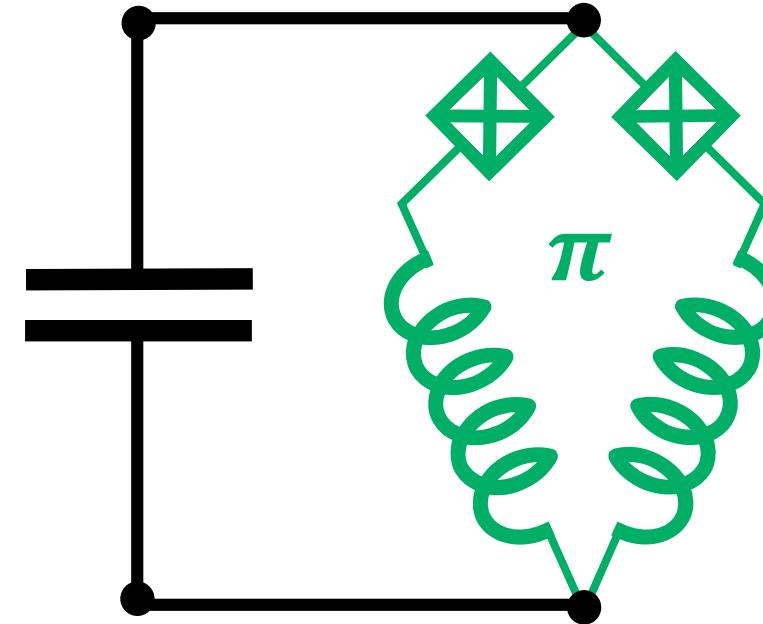
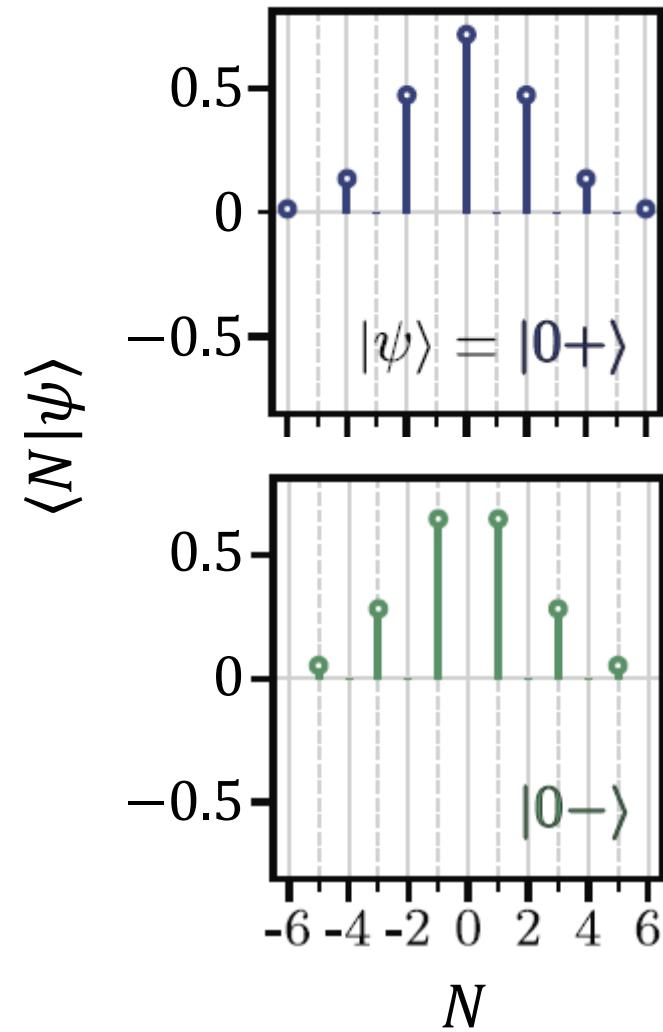


$$\epsilon_L \gtrsim E_J$$



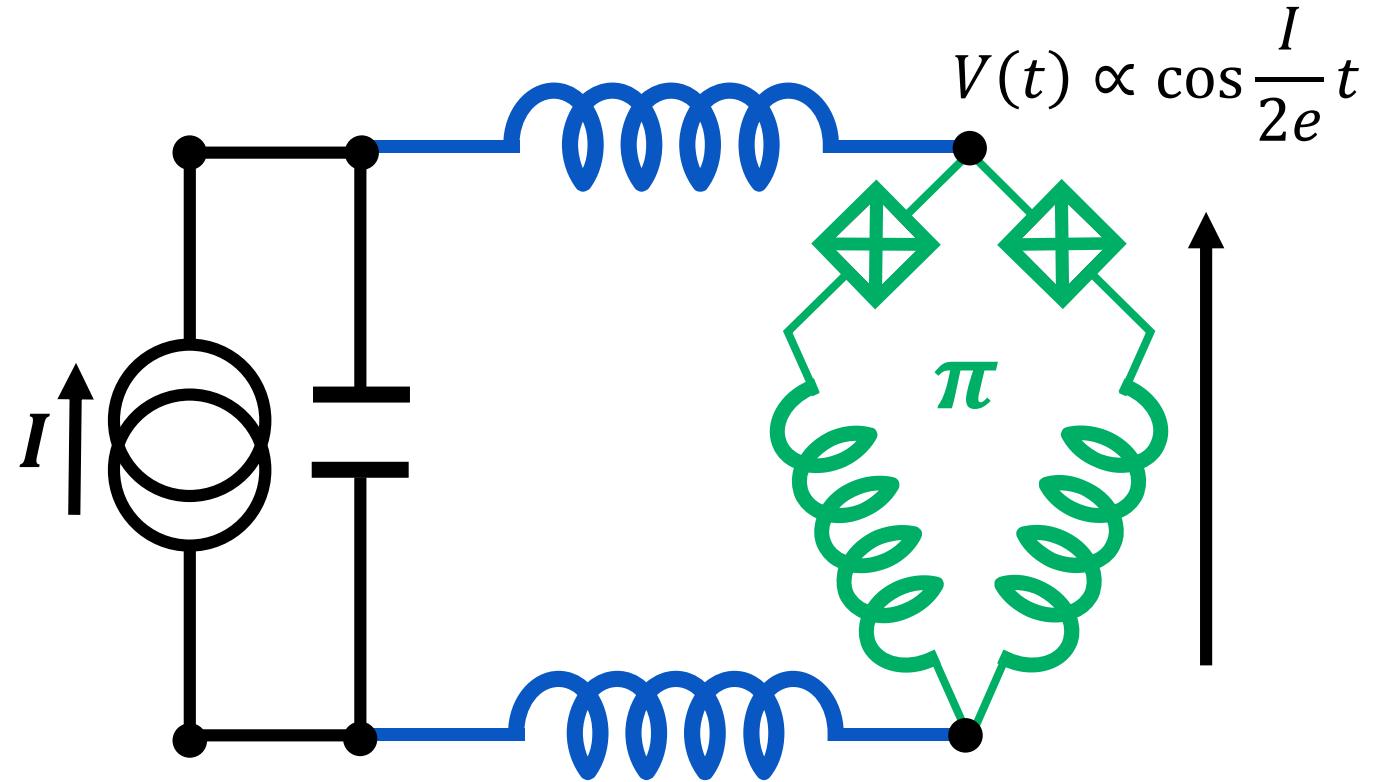
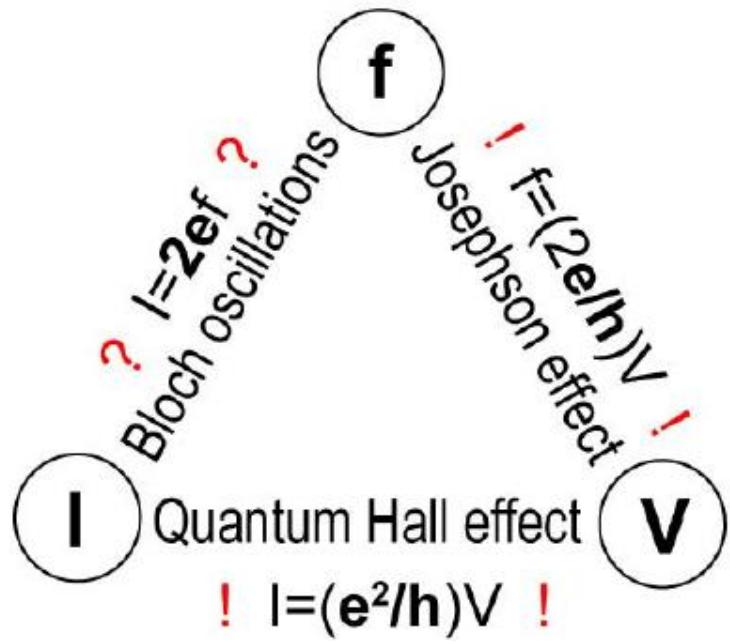
→ Interlacing spectra  
→ High order photon-photon interactions

# Qubit protected by Cooper-pair pairing (**open position**)



Smith *et al.* NPJQI (2020)

# Closing the metrological triangle



# The QUANTIC team

