

First-order quantum breakdown of a superconductor ruled by phase fluctuations

Thibault Charpentier

Néel Institute, Grenoble, France



Les Houches, June 5 2023



In this talk

Study of strongly disordered amorphous indium oxide film (aInO) across the **Superconductor-Insulator Transition** at microwave frequencies.

PhD supervised by



N. Roch



B. Sacépé

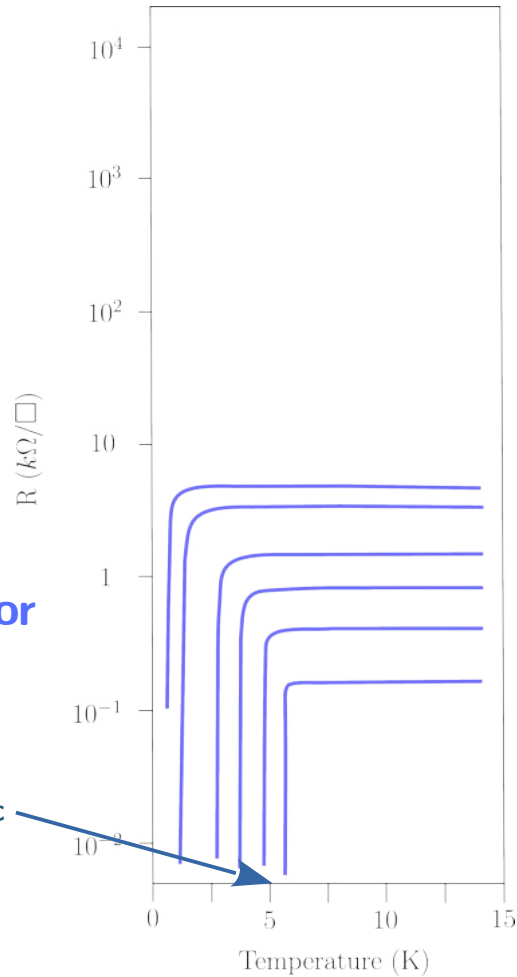


Superconductor-Insulator Transition

Example : Bismuth thin films

Superconductor

Critical temperature T_c



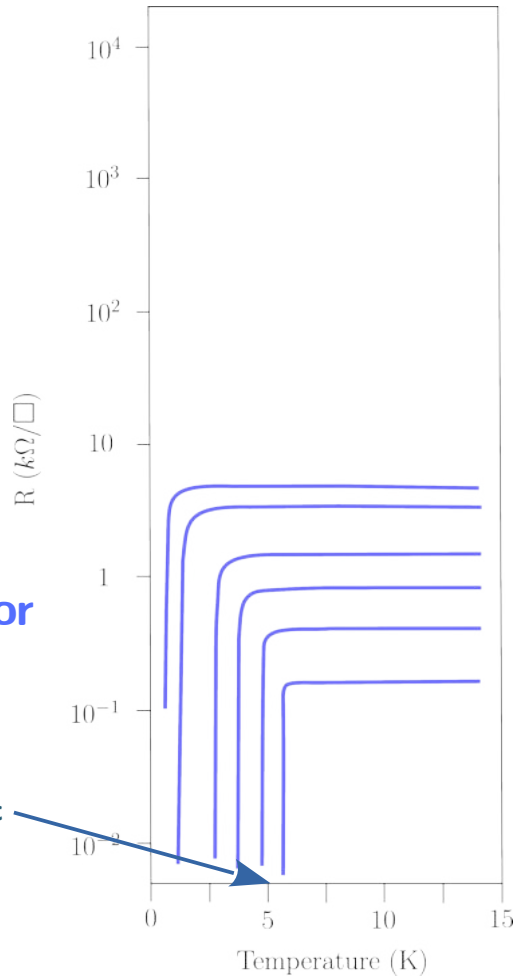
Adapted from Haviland et al, PRL (1989)



Superconductor-Insulator Transition

Superconductor

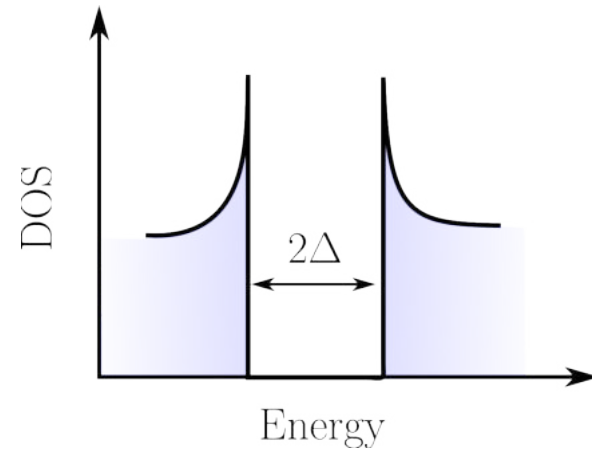
Critical temperature T_c



Example : Bismuth thin films

Superconducting gap Δ

Pairing energy between electrons of a CP



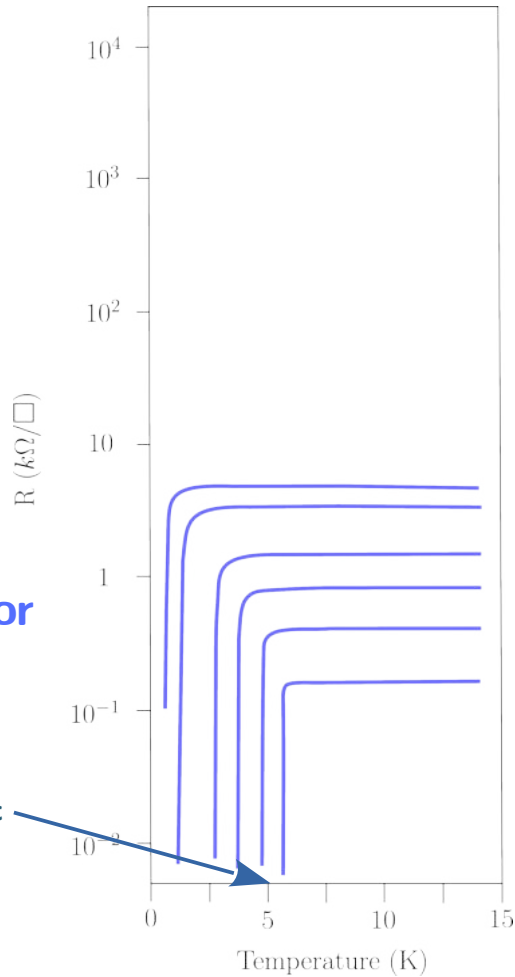
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Superconductor-Insulator Transition

Superconductor

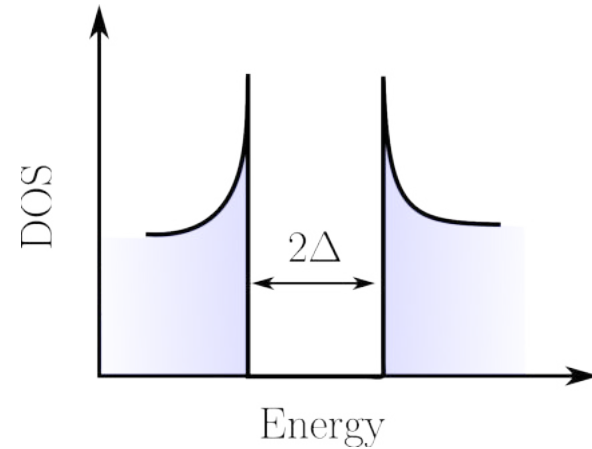
Critical temperature T_c



Example : Bismuth thin films

Superconducting gap $\Delta \sim 1.76 k_B T_c$

Pairing energy between electrons of a CP



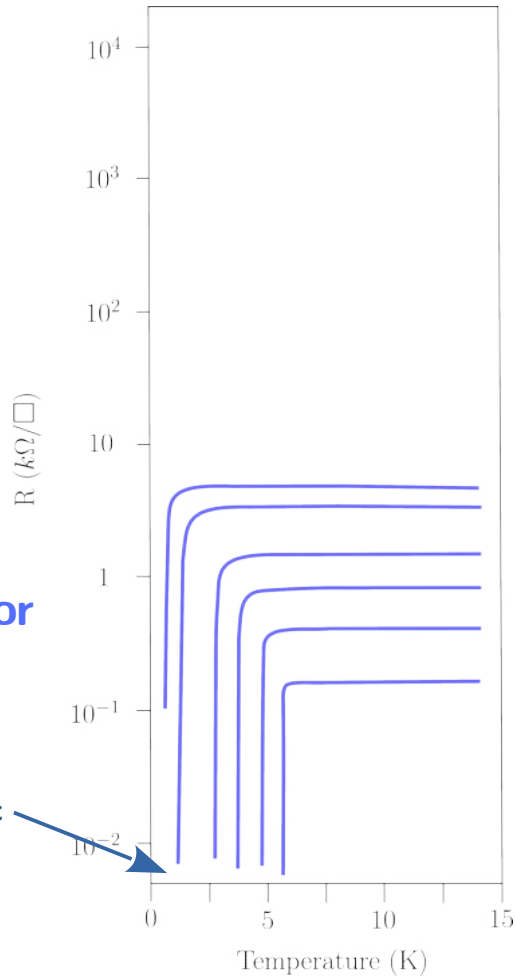
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Superconductor-Insulator Transition

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Example : Bismuth thin films

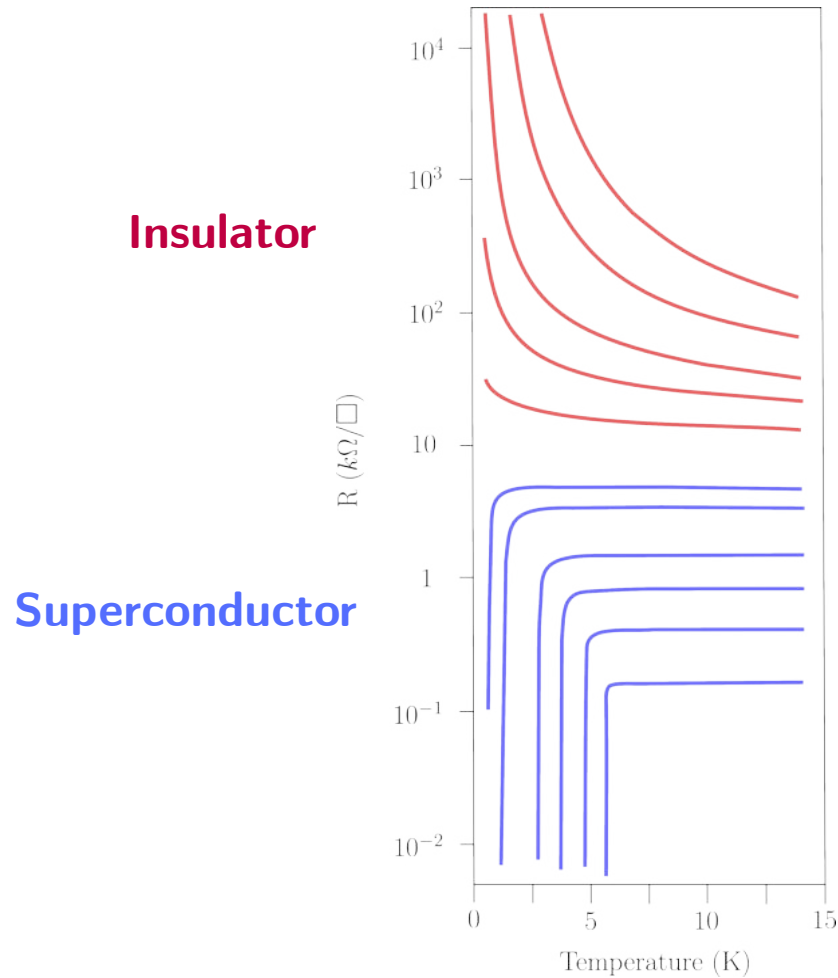
With some driving parameter
(thickness, disorder, B-field ...)

Suppression of T_c

Adapted from Haviland et al, PRL (1989)



Superconductor-Insulator Transition



Example : Bismuth thin films

With some driving parameter
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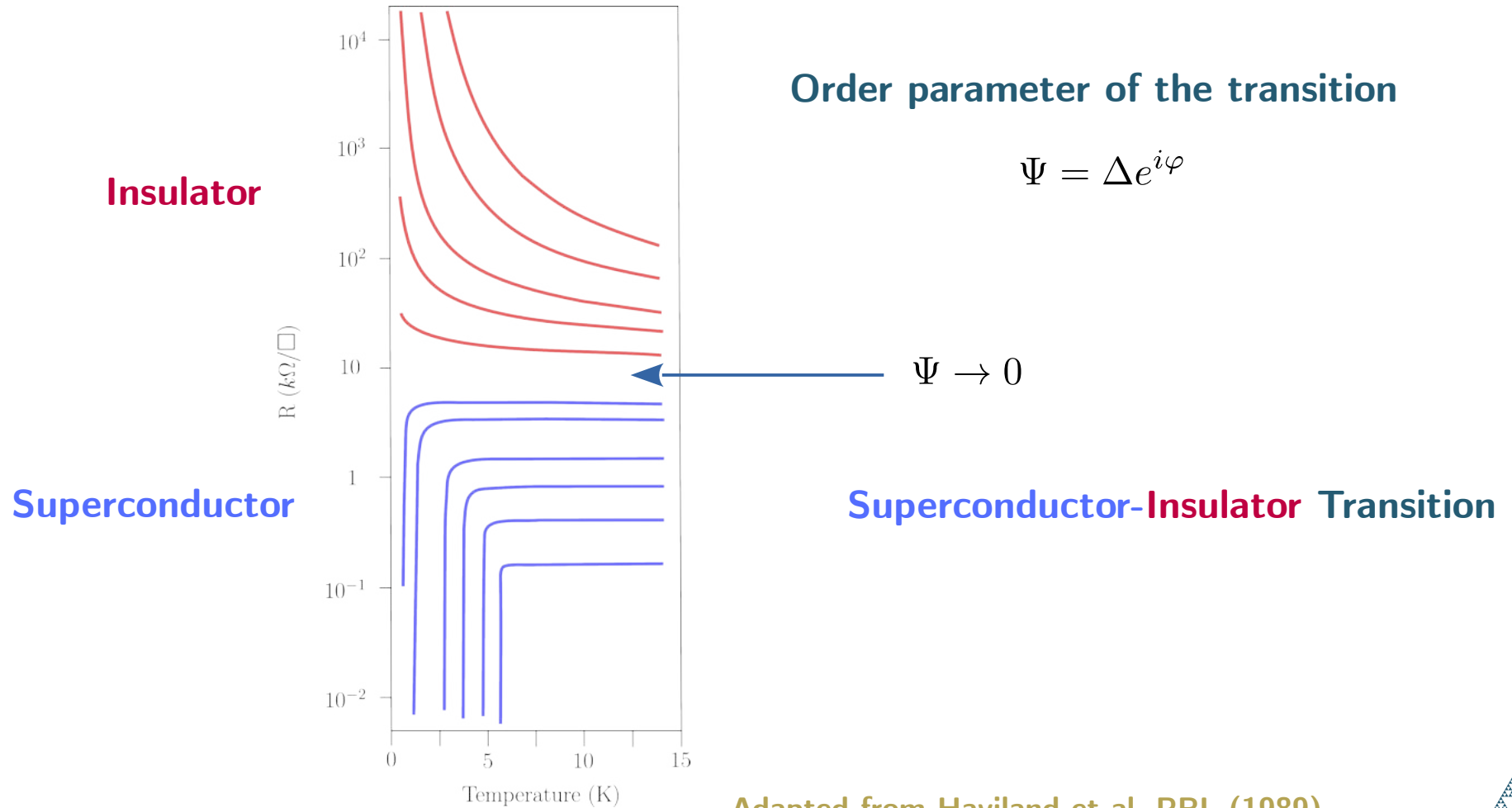
Suppression of T_c

Superconductor-Insulator Transition

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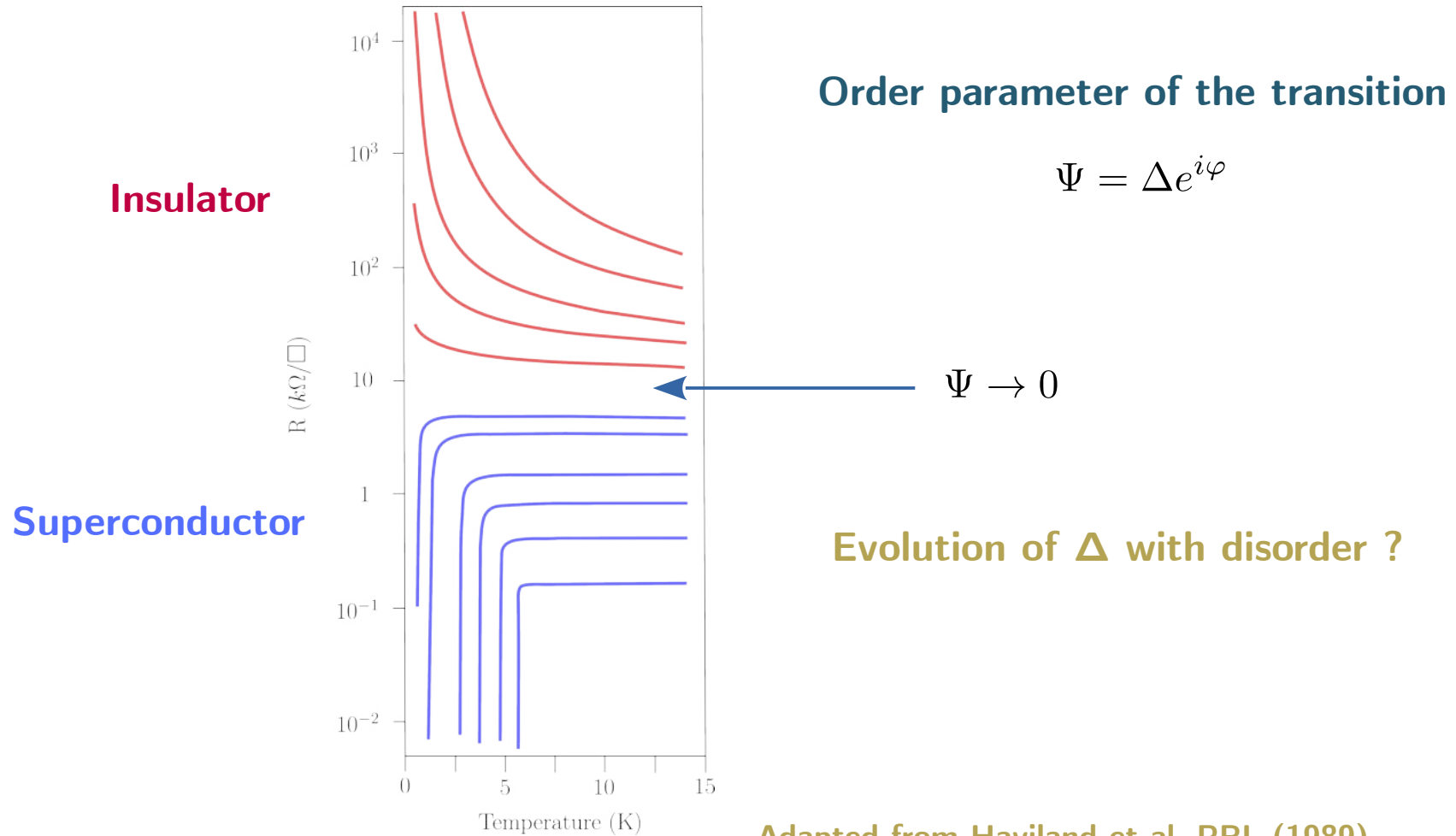
Superconductor-Insulator Transition



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Superconductor-Insulator Transition



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Superconductor-Insulator Transition

Fermionic mechanism

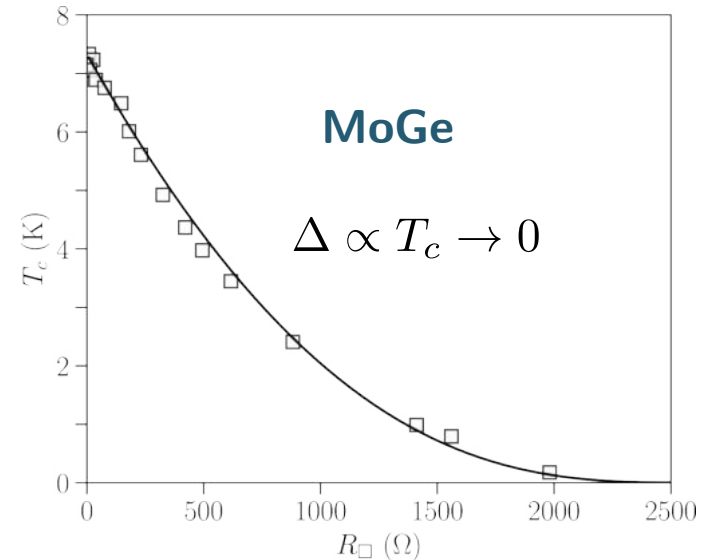
Disorder-enhanced **Coulomb repulsion** between electrons of a Cooper pair opposes to pairing attraction

Cooper pairing dies out at the SIT

$$\Delta \rightarrow 0$$

Order parameter of the transition

$$\Psi = \cancel{\Delta} e^{i\varphi}$$



Finkel'stein, Physica B (1994)



Superconductor-Insulator Transition

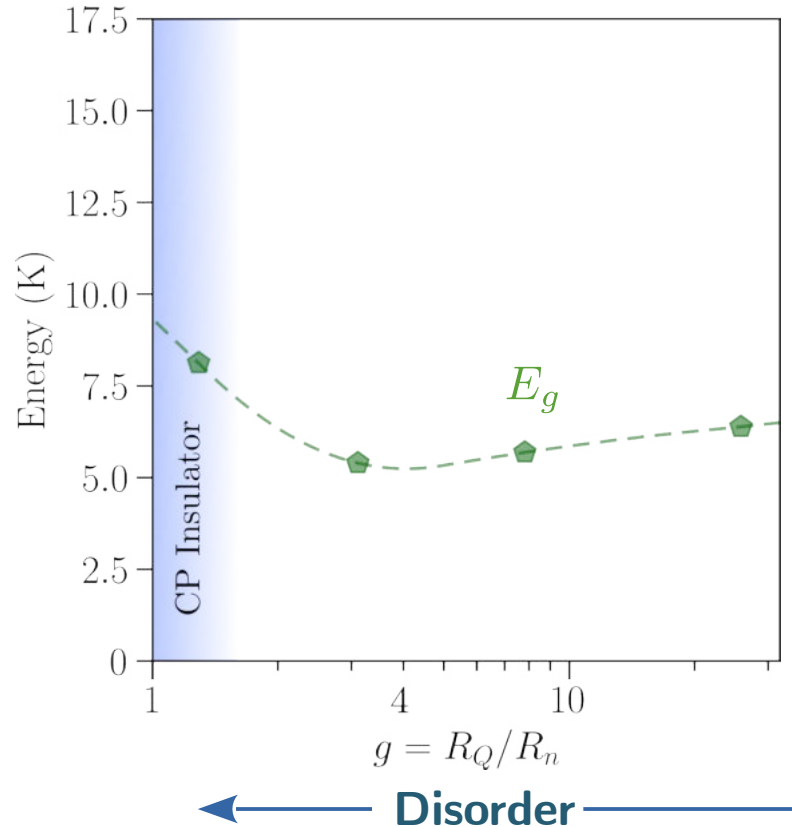
Is it the full picture ?

Let us see indium oxide data



Superconductor-Insulator Transition

Indium oxide



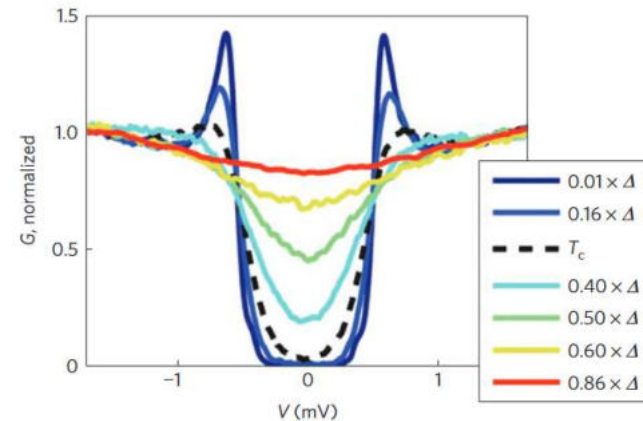
Superconducting gap E_g

Sacépé et al, Nature Physics (2011)

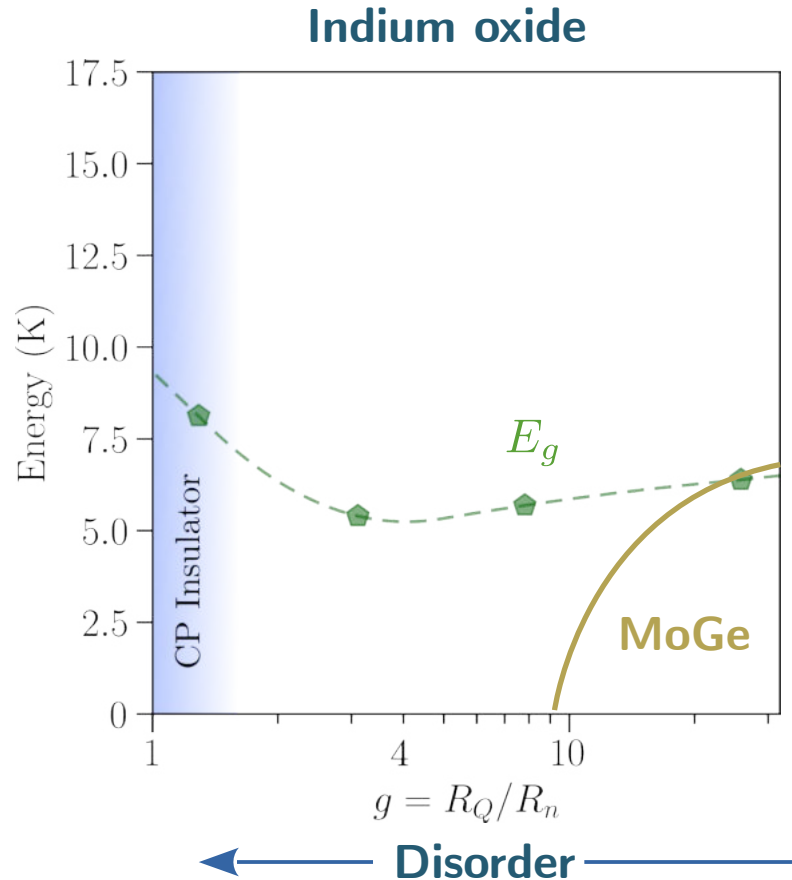
Sacépé et al, PRB (2015)

Sherman et al, PRB (2014)

Tunneling spectroscopy



Superconductor-Insulator Transition



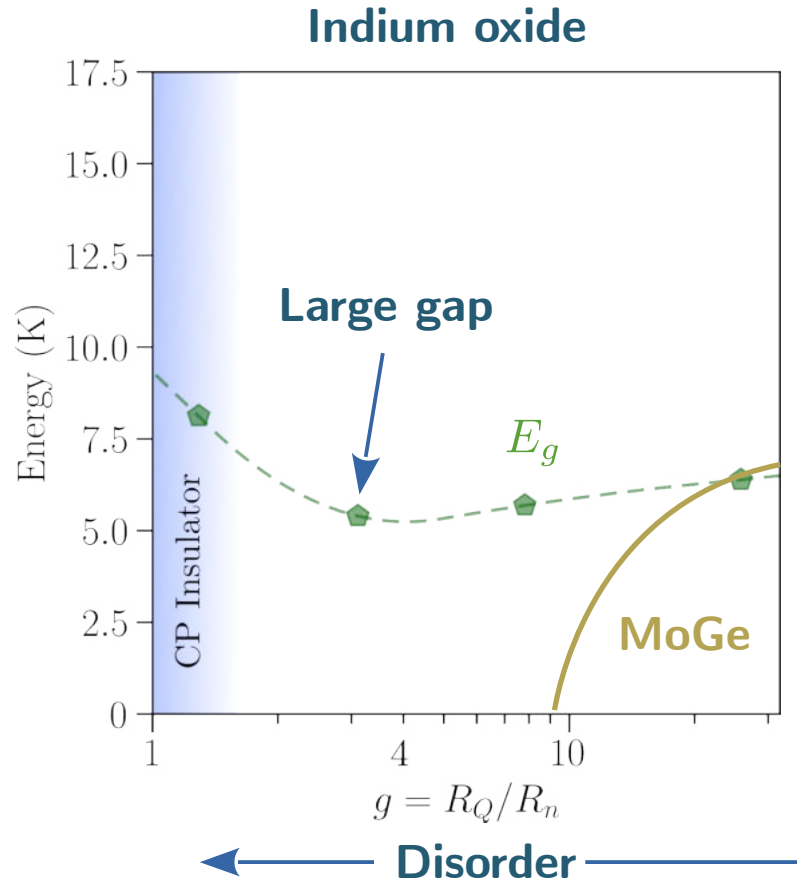
Comparison with fermionic scenario

Gap in MoGe is strongly suppressed

Finkel'stein, Physica B (1994)



Superconductor-Insulator Transition



Comparison with fermionic scenario

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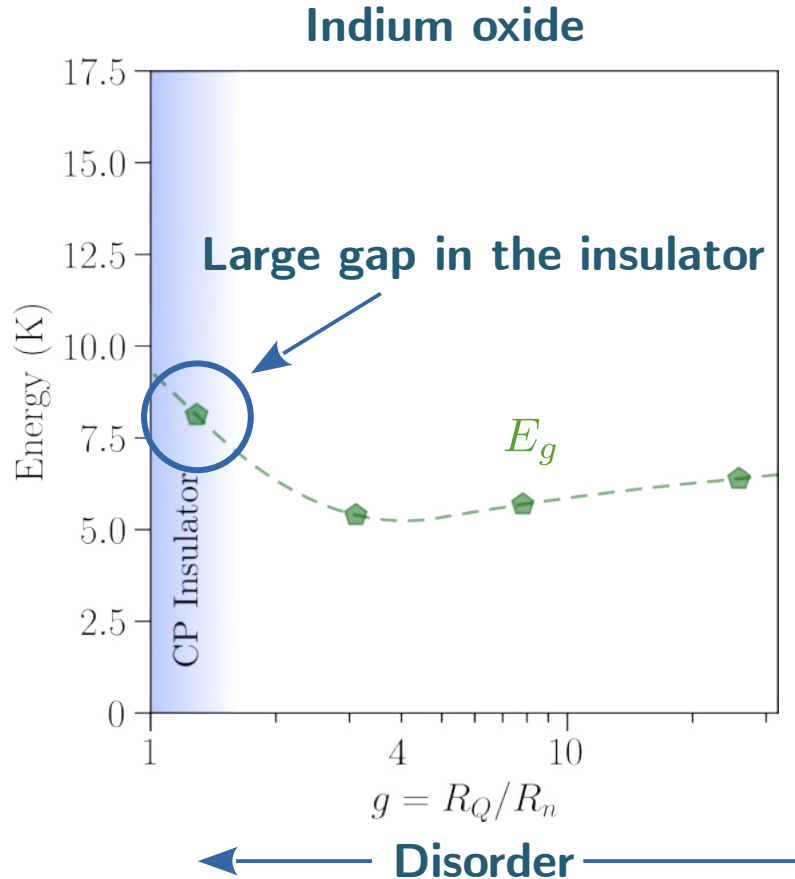
Finkel'stein, Physica B (1994)

But gap in InO remains large

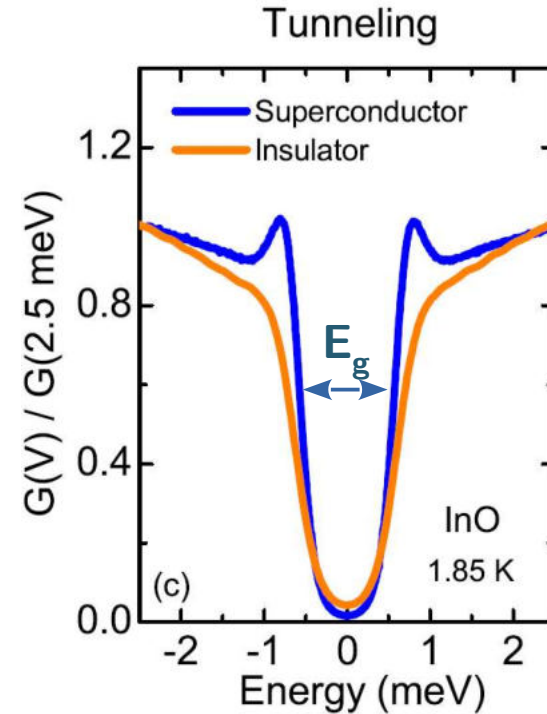
Fermionic scenario does not apply for InO



Pseudogap in indium oxide



Gap remains in insulating state



Sherman et al, PRB (2014)



Pseudogap in indium oxide

Superconducting gap does not vanish in the insulator (pseudogap)

Other mechanism for the breakdown of superconductivity :

Bosonic mechanism

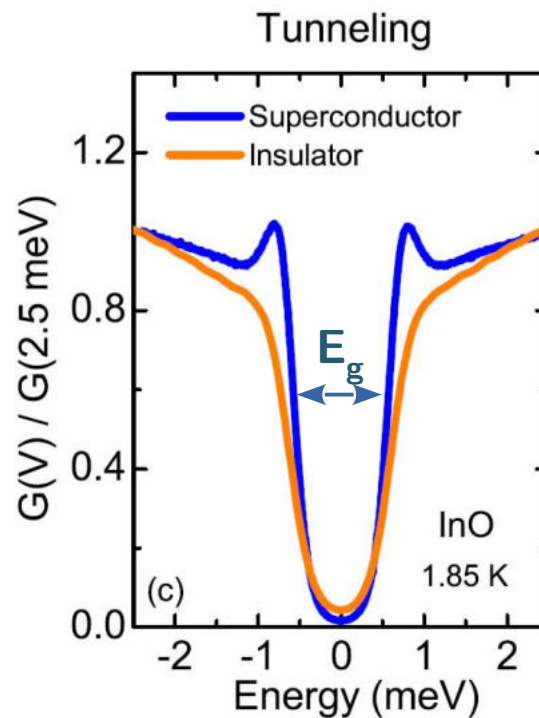
$$\Psi = \Delta e^{i\phi}$$

Phase fluctuations suppress superconductivity

Insulator of incoherent Cooper pairs

Fisher et al, PRB (1989)

Gap remains in insulating state



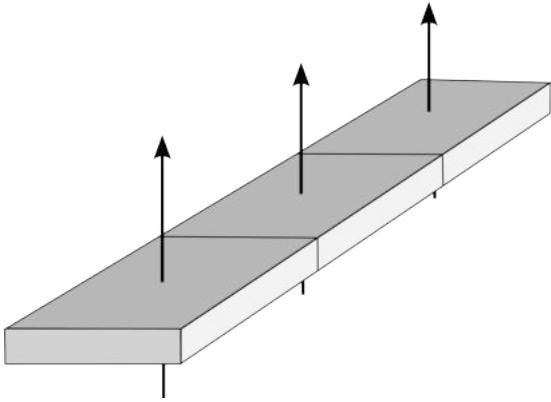
Sherman et al, PRB (2014)



On phase fluctuations

Superconducting order parameter

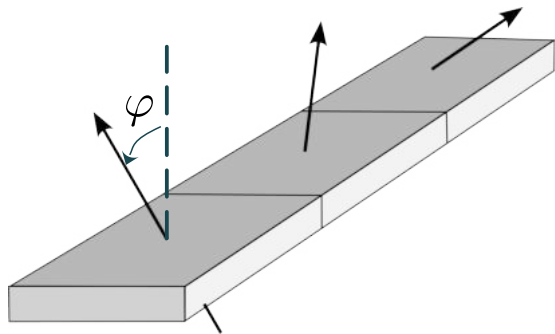
$$\Psi(\mathbf{r}) = \Delta(\mathbf{r})e^{i\varphi(\mathbf{r})}$$



On phase fluctuations

Superconducting order parameter

$$\Psi(\mathbf{r}) = \Delta(\mathbf{r})e^{i\varphi(\mathbf{r})}$$



Elastic energy cost to twist the phase :

$$E = \frac{\Theta}{2} \int (\nabla\varphi)^2 d\mathbf{r}$$

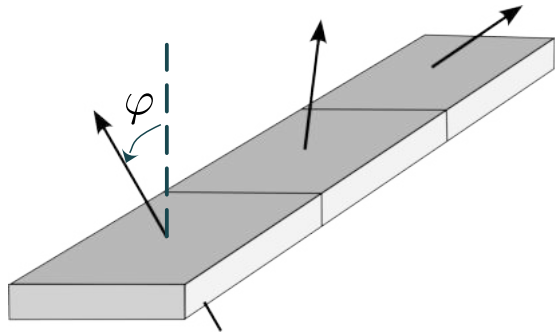
where Θ is the superfluid stiffness $\approx E_J$



On phase fluctuations

Superconducting order parameter

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Elastic energy cost to twist the phase :

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where Θ is the superfluid stiffness $\approx E_J$

Θ describes the resilience of a superconductor against phase fluctuations : SIT for $\Theta \rightarrow 0$



On phase fluctuations

Elastic energy cost to twist the phase

$$E = \frac{\Theta}{2} \int (\nabla\varphi)^2 d\mathbf{r}$$

Kinetic energy of the condensate

$$E = \int \frac{1}{2} n_s m v_s^2 d\mathbf{r} \text{ where } v_s = \frac{\hbar}{m} \nabla\varphi$$
$$= \frac{1}{2} L_K I^2$$

L_K is the kinetic inductance



On phase fluctuations

Elastic energy cost to twist the phase

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$$\Theta = \left(\frac{\hbar}{2e} \right)^2 \frac{1}{L_K}$$

L_K is the kinetic inductance

Θ can be obtained experimentally through the measurement of L_K



Phase stiffness versus gap

Elastic energy cost to twist the phase

$$E = \frac{\Theta}{2} \int (\nabla\varphi)^2 d\mathbf{r}$$

Amplitude of pairing strength E_g

Two possibilities

$\Theta \gg E_g$ Phase fluctuations do not affect superconductivity



Phase stiffness versus gap

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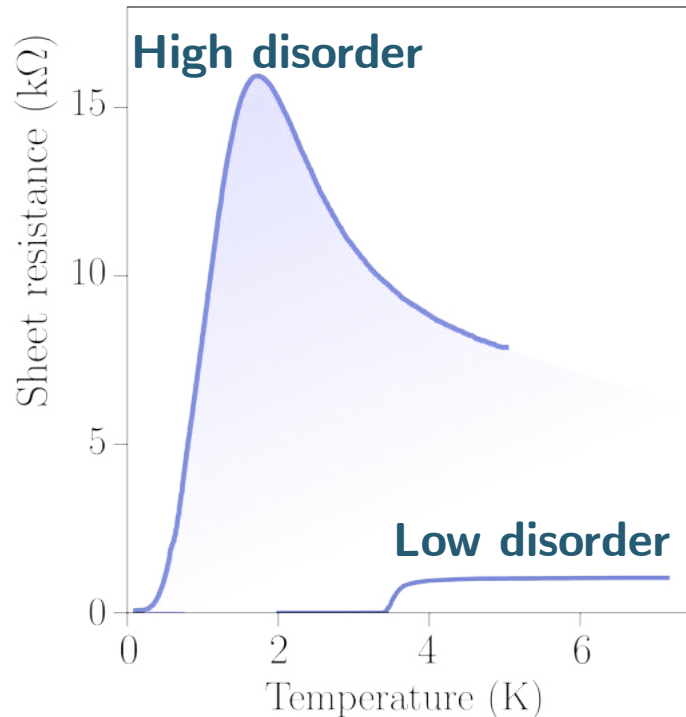
$\Theta \gg E_g$ Phase fluctuations do not affect superconductivity

$\Theta \leq E_g$ Phase fluctuations suppress superconductivity (bosonic scenario)



In which system ?

$\Theta \leq E_g$ can be achieved in **strongly disordered superconductors**



Strong electron scattering $k_F l \sim 1$

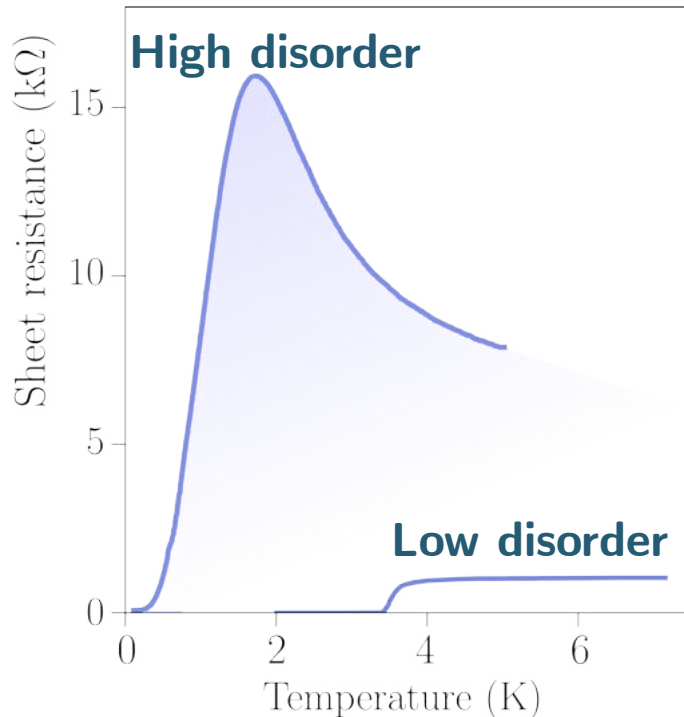
Enhanced normal state resistance R_n

Low superfluid density



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$\Theta \leq E_g$ can be achieved in **strongly disordered superconductors**



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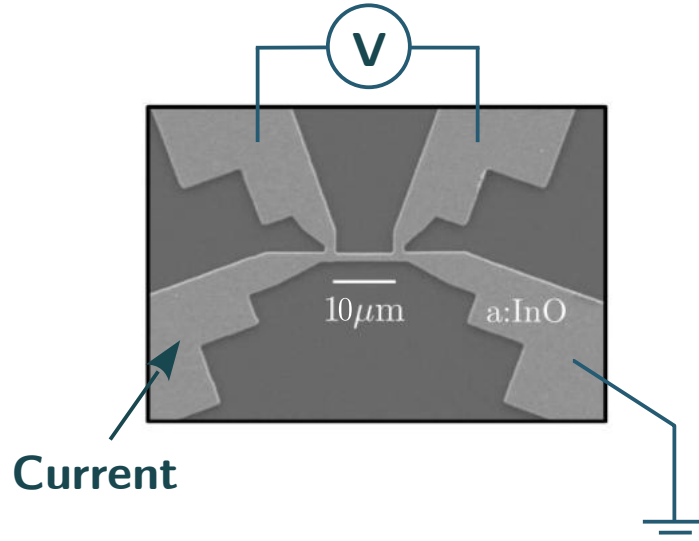
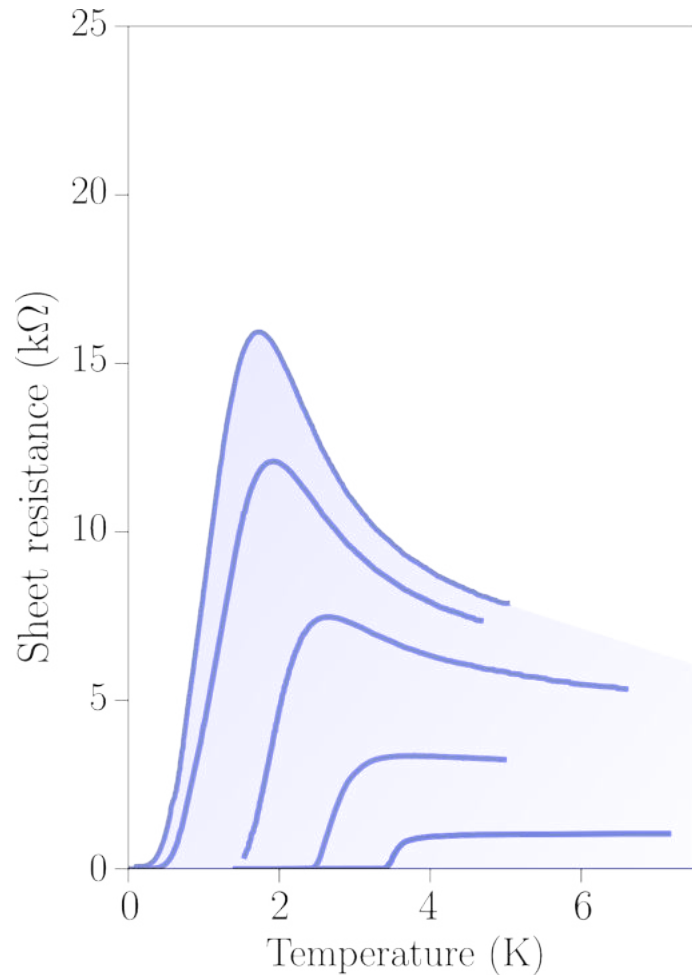
Low superfluid density

$$L_K = \frac{\hbar R_n}{\pi \Delta} \longrightarrow \Theta \propto \frac{1}{R_n} \text{ is small}$$

large phase fluctuations



Amorphous indium oxide

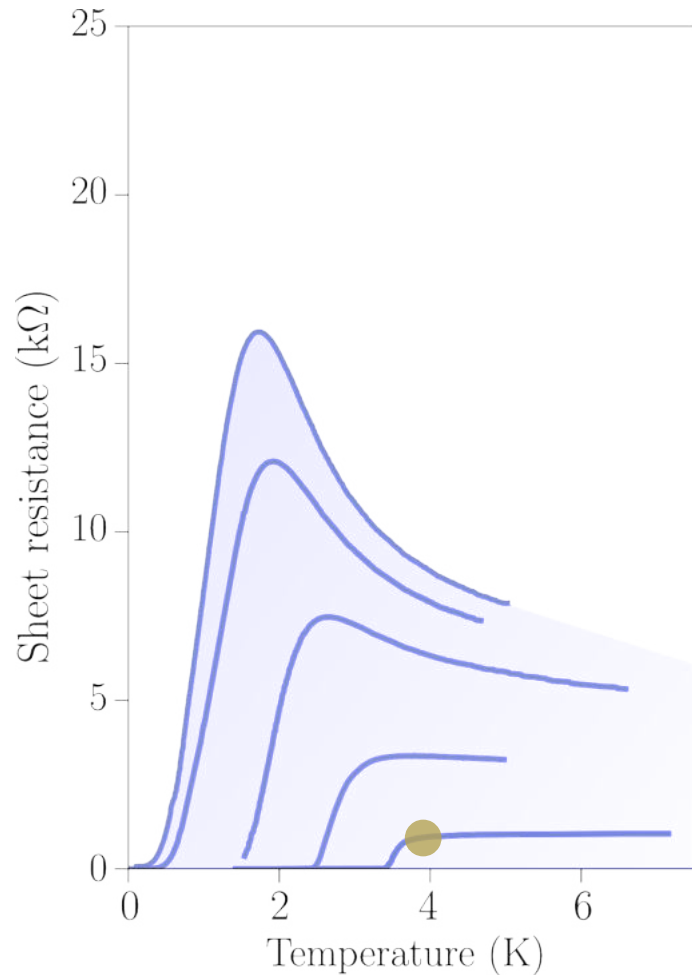


Sheet resistance $R_{\square} = \frac{\rho}{d}$

Thickness $d = 40 \text{ nm}$

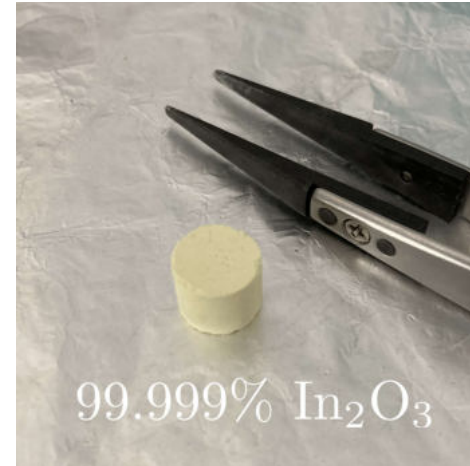


Amorphous indium oxide

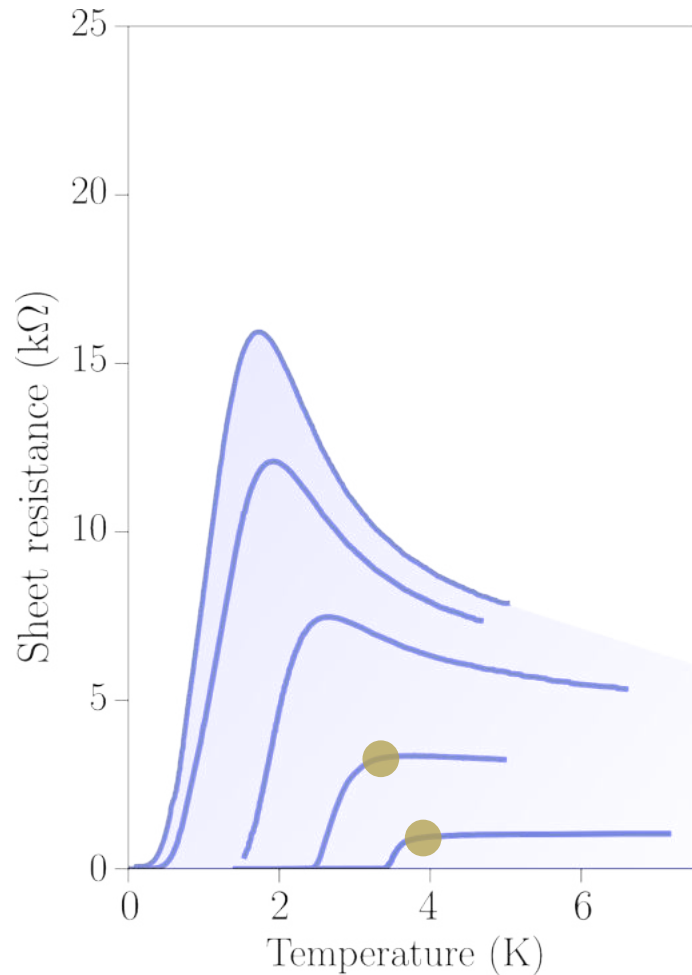


Resistance increases with disorder

Disorder tuned by oxygen pressure during evaporation

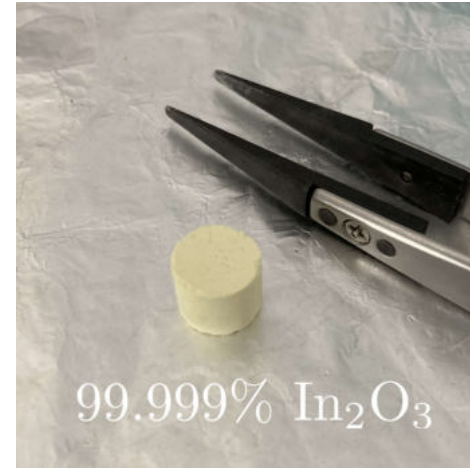


Amorphous indium oxide

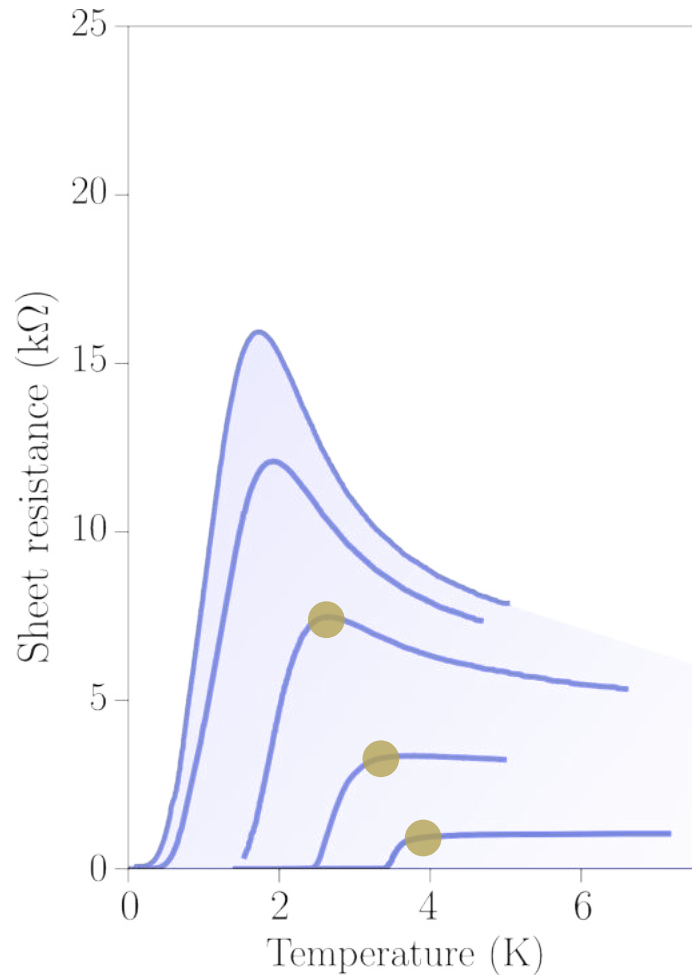


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Amorphous indium oxide

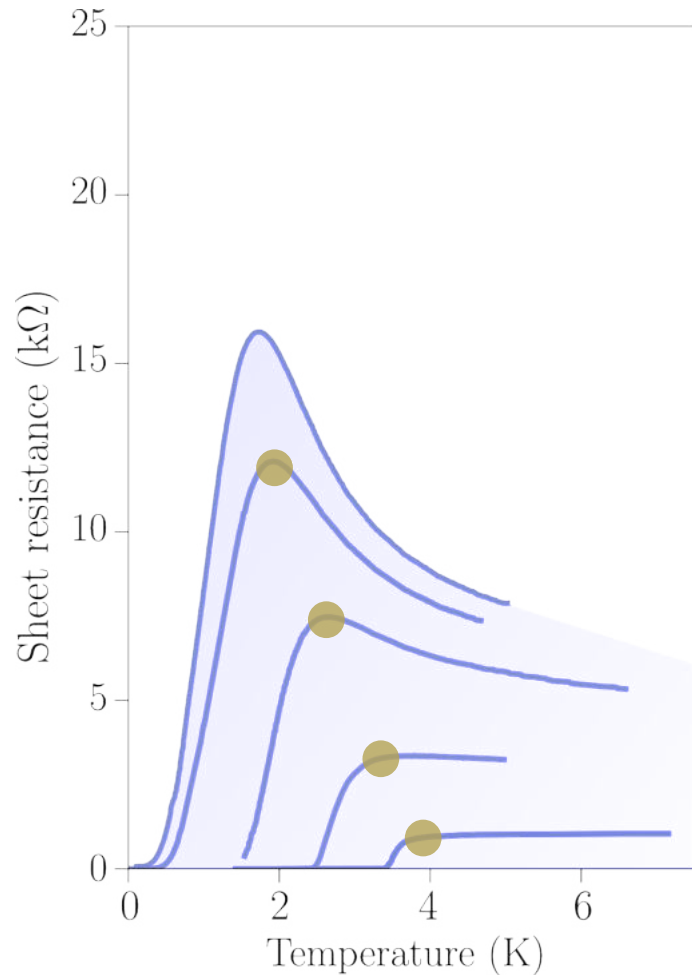


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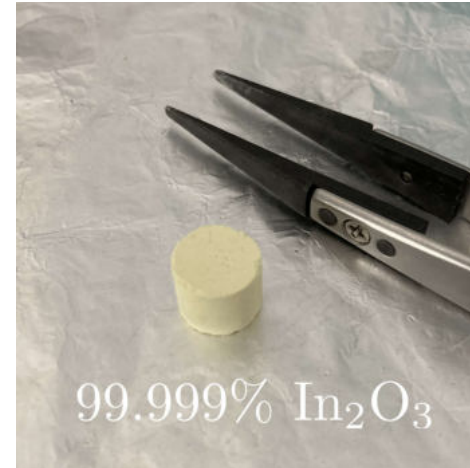


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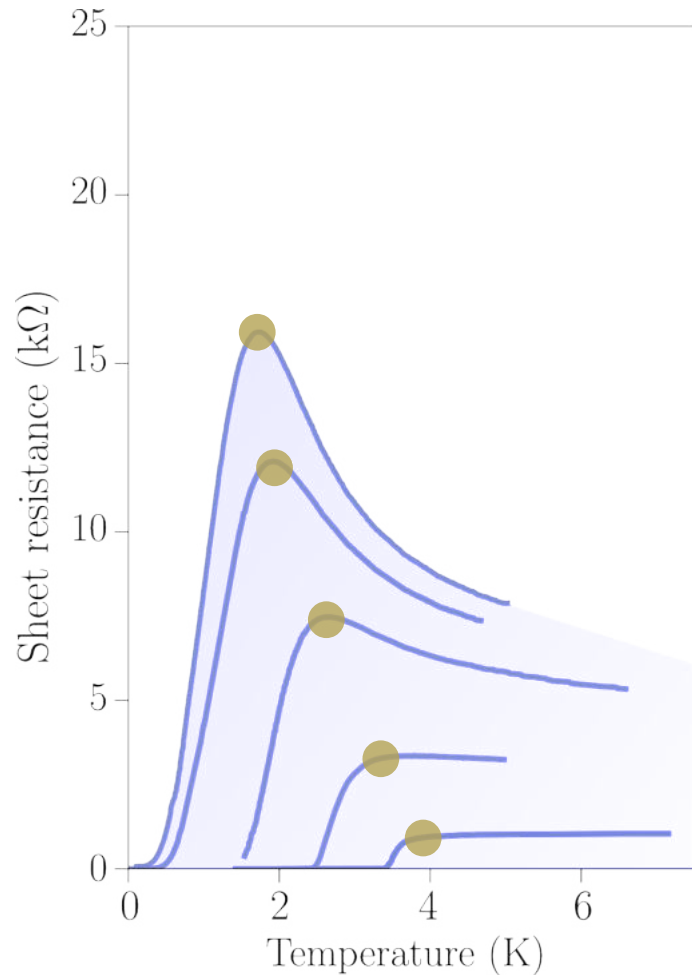


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Amorphous indium oxide



Resistance increases with disorder

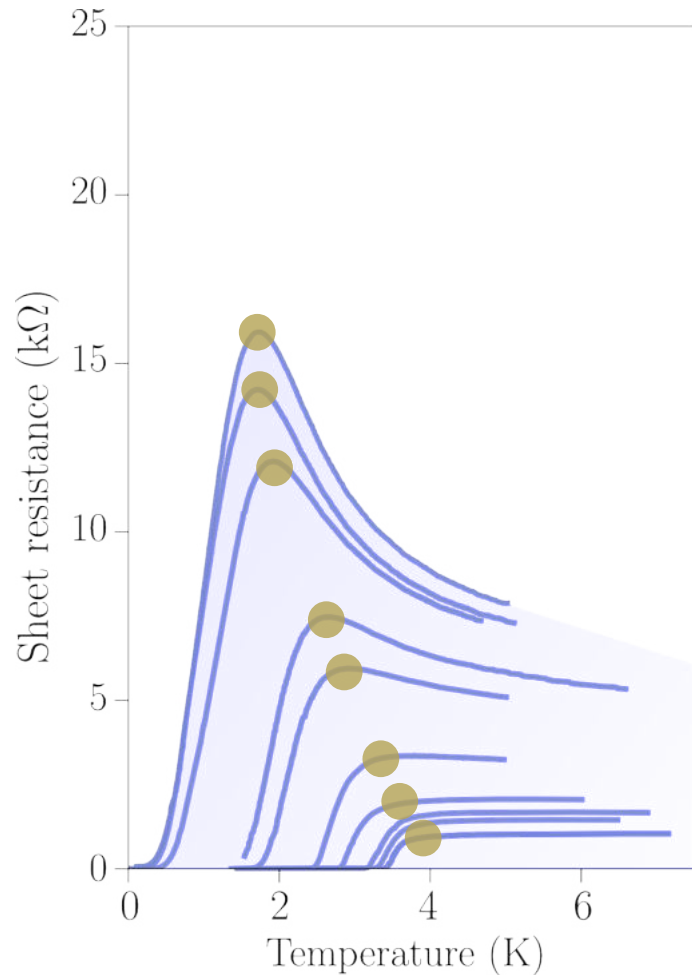
Strongly disordered superconductor :

Short coherence length $\xi \sim 5$ nm

Strong electron localization $k_F l < 1$



Amorphous indium oxide

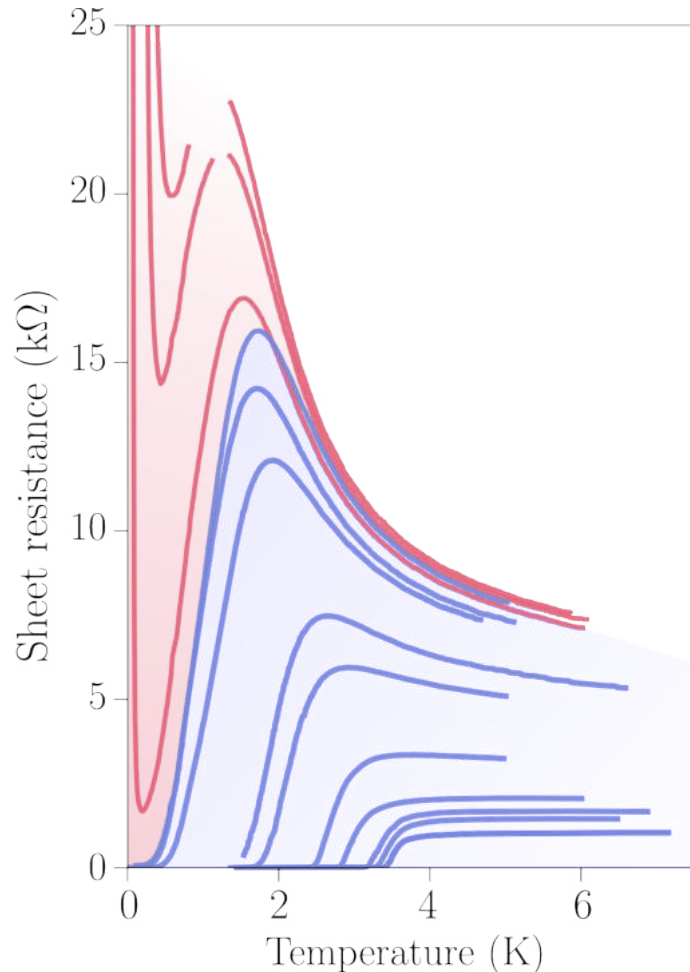


Anderson's theorem (conventional SCs are robust against disorder) **does not apply here**

Superconductivity is weakened by strong disorder
 T_c decreases



Amorphous indium oxide



Anderson's theorem (conventional SCs are robust against disorder) **does not apply here**

Superconductivity is weakened by strong disorder

Above a critical disorder :
Superconductor-Insulator Transition

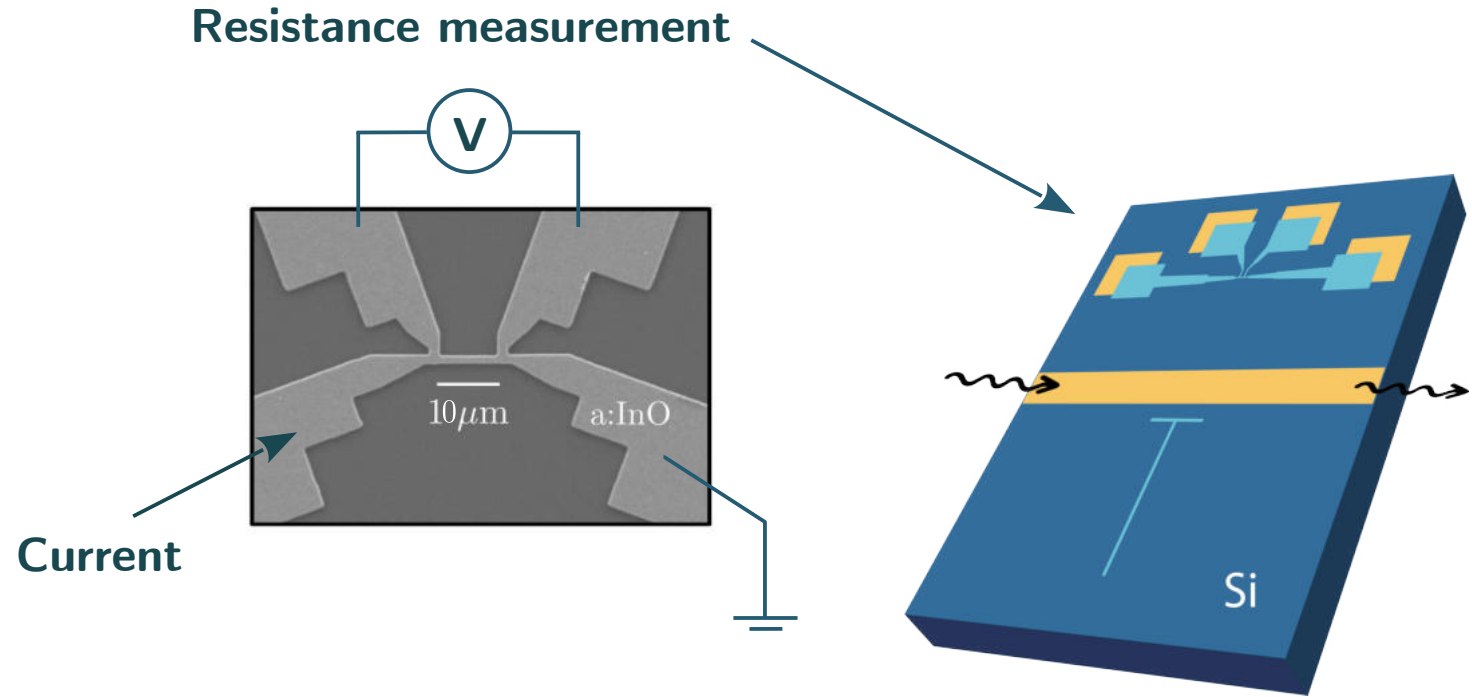
Review article : Sacépé, Feigel'man and Klapwijk, Nature Physics (2020)



The sample

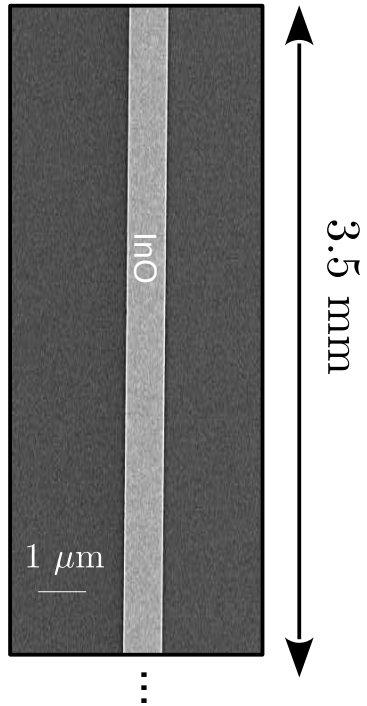


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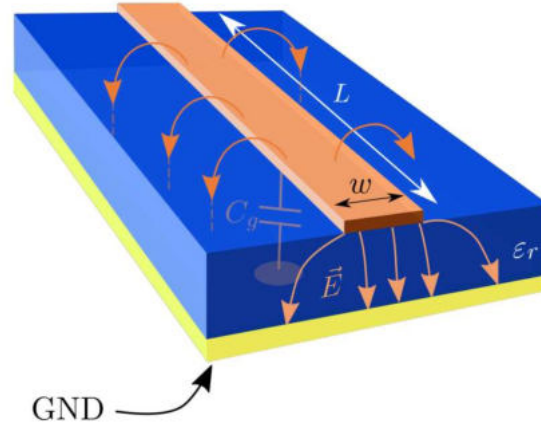
Microwave resonator

Long AlN resonator

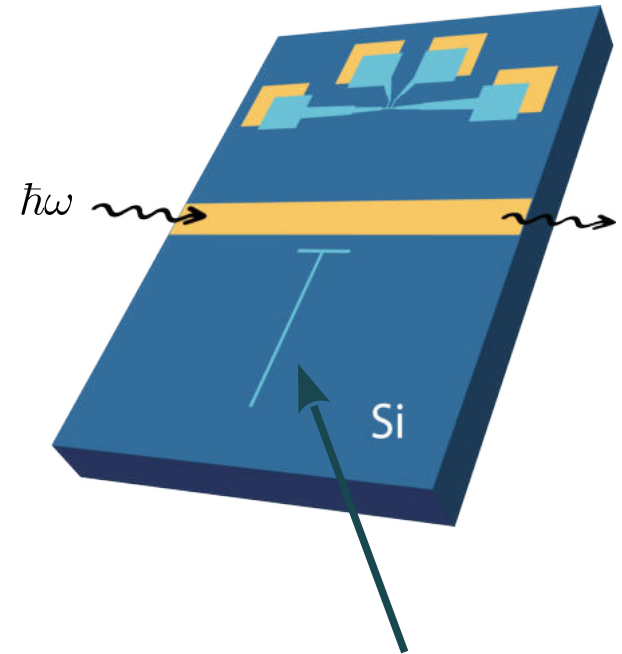


Kinetic inductance L_K

Microstrip geometry



Capacitance to ground C

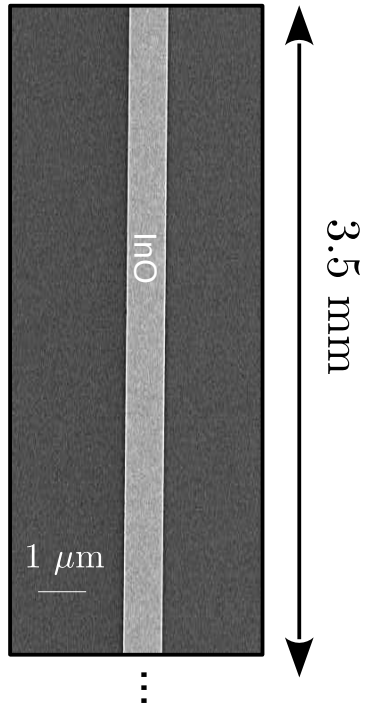


Resonator



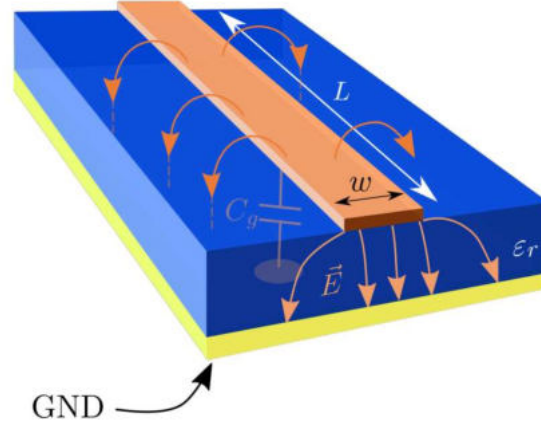
Microwave resonator

Long AlN resonator



Kinetic inductance L_K

Microstrip geometry



Capacitance to ground C

Plasmon standing wave resonances given by

$$\omega_n = v|k_n| = \frac{|k_n|}{\sqrt{L_K C}}$$

Kulik, ZETF (1973)

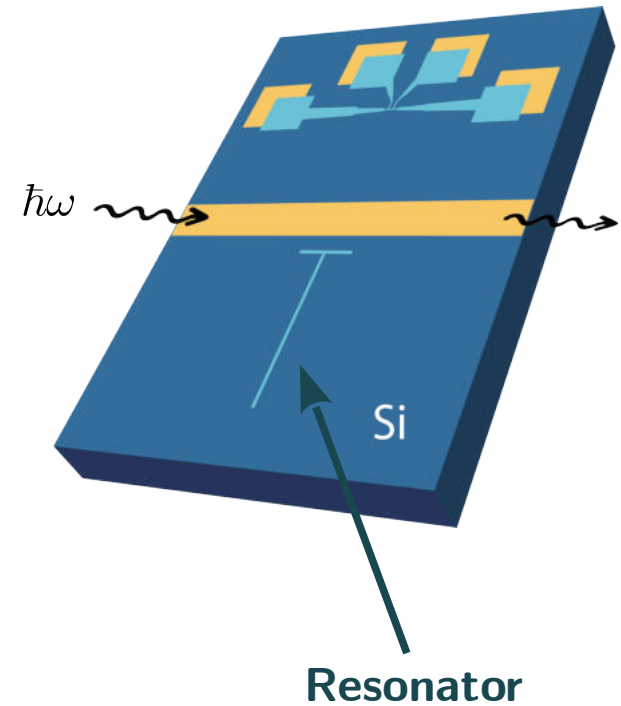
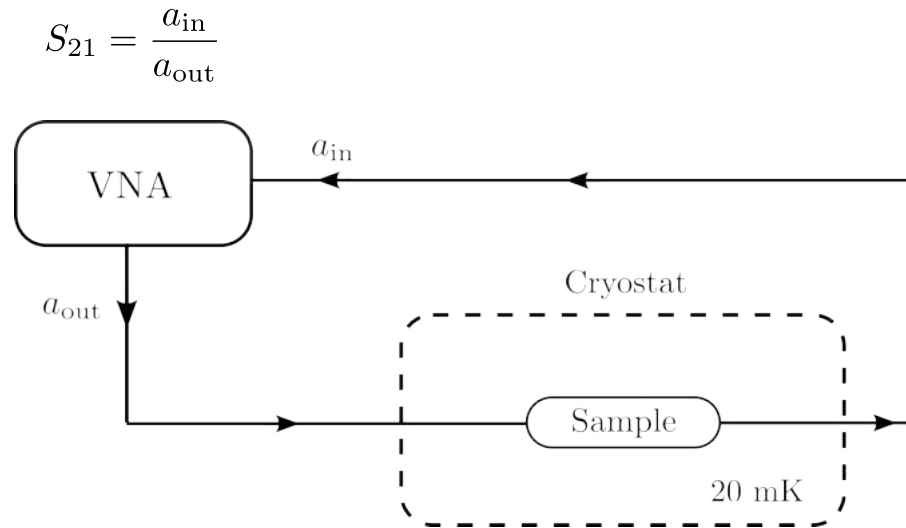
Mooij and Schön, PRL (1985)

Camarota et al, PRL (2001)



Microwave spectroscopy

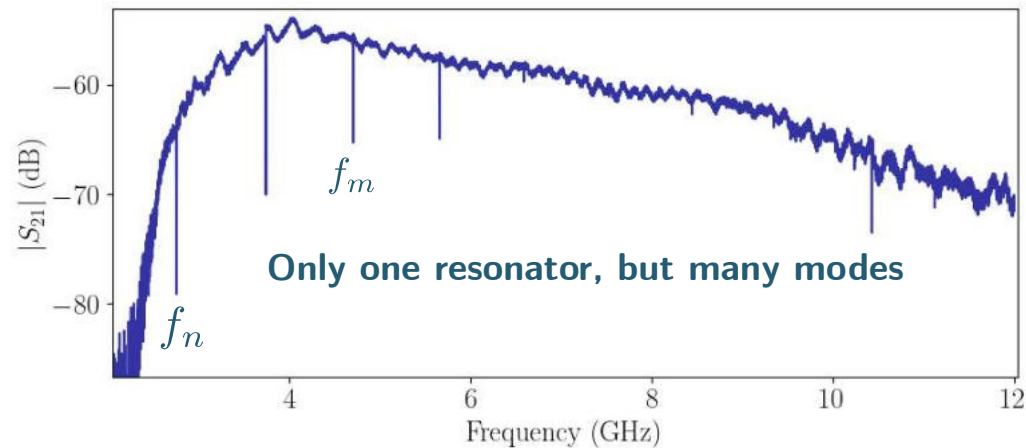
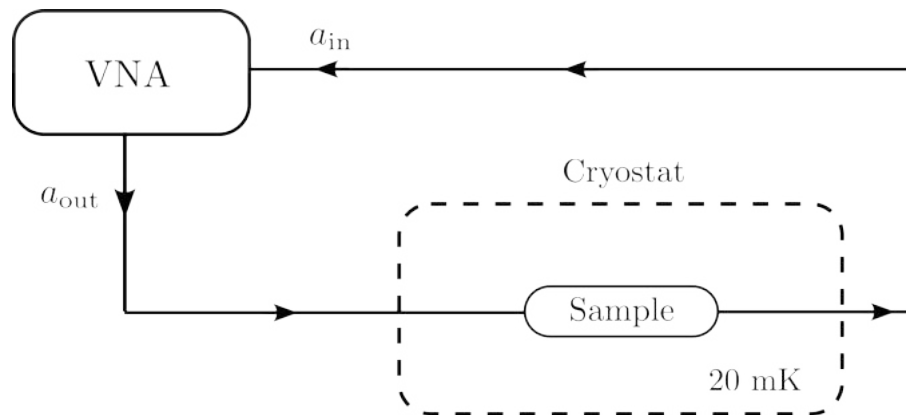
Single-tone measurement (at $T = 20$ mK)



Microwave spectroscopy

Single-tone measurement
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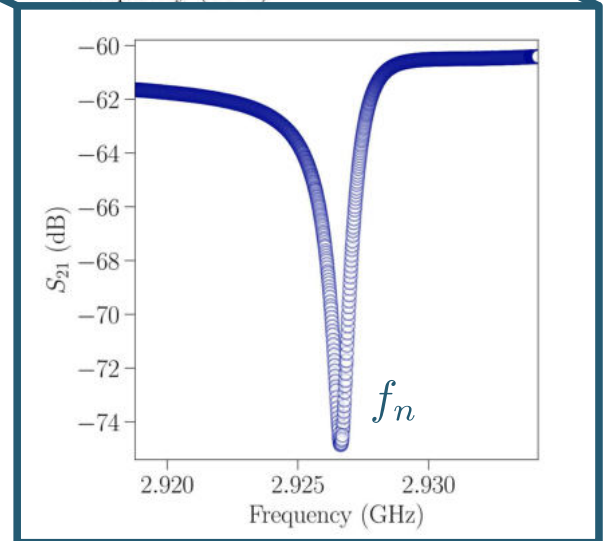
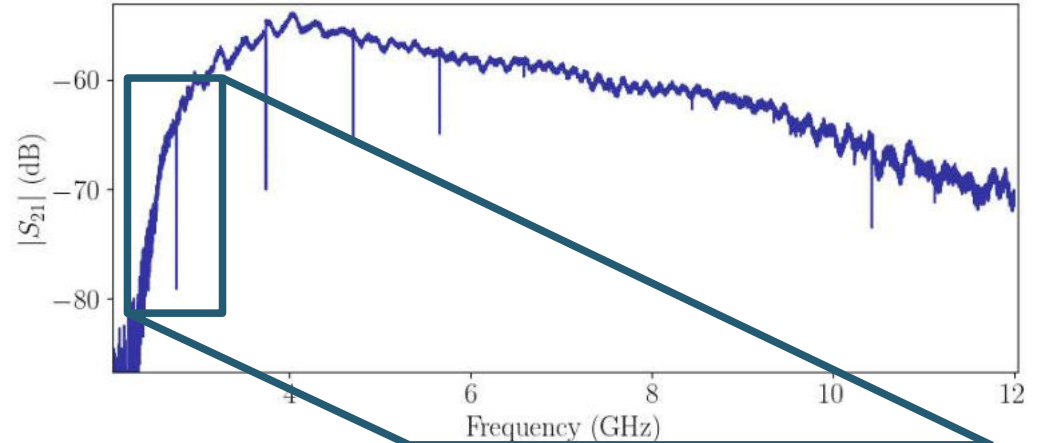
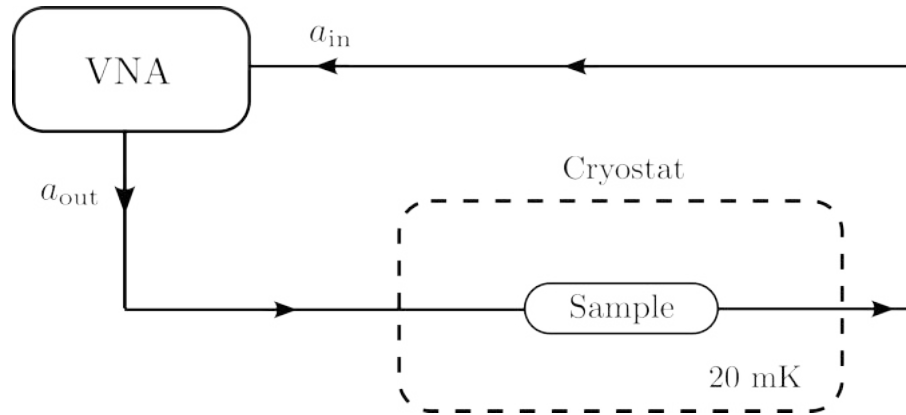
$$S_{21} = \frac{a_{\text{in}}}{a_{\text{out}}}$$



Microwave spectroscopy

Single-tone measurement
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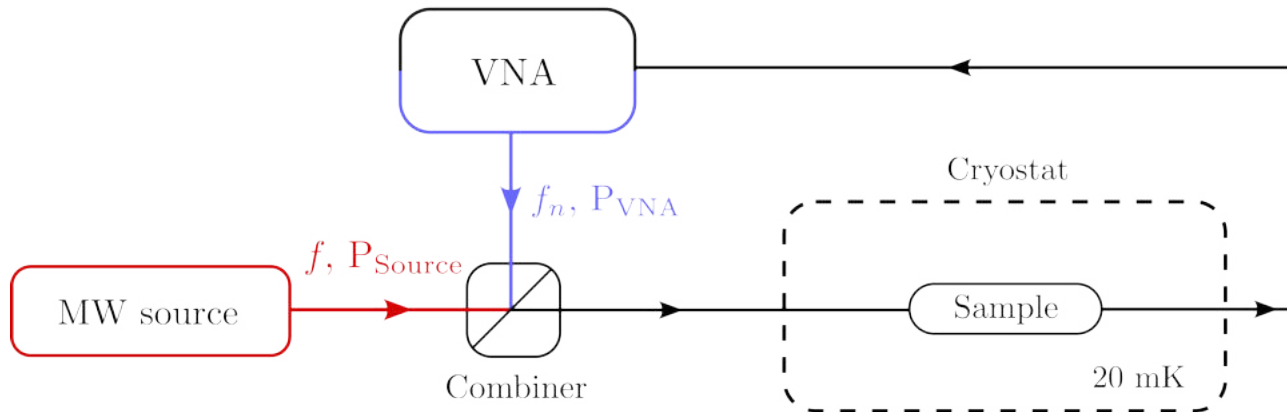
$$S_{21} = \frac{a_{in}}{a_{out}}$$



Two-tones spectroscopy

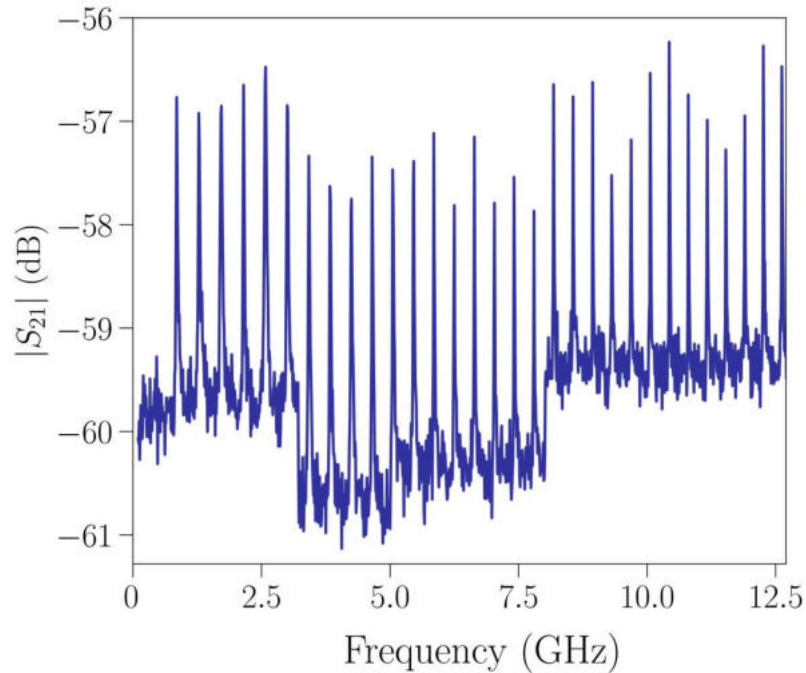
To measure modes between 0-30 GHz we perform a two-tones spectroscopy

We add a second tone to the VNA signal and exploit the resonator's non-linearities



Two-tones spectroscopy

To measure modes between 0-30 GHz we perform a two-tones spectroscopy



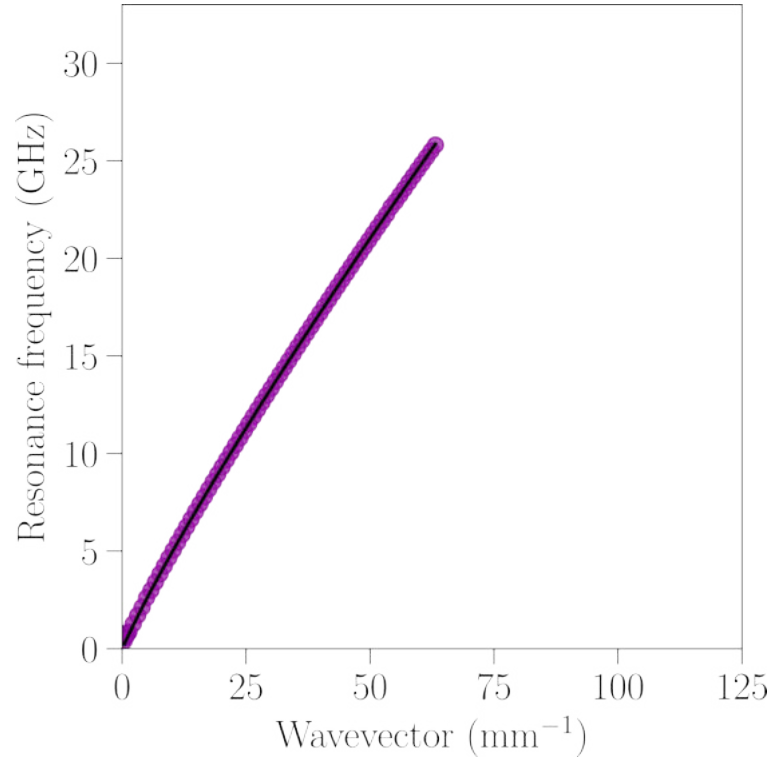
Each peak corresponds to a resonant mode of the Indium oxide resonator

$$\omega_n = \frac{|k_n|}{\sqrt{L_K C}}, n \in \mathbb{N}$$



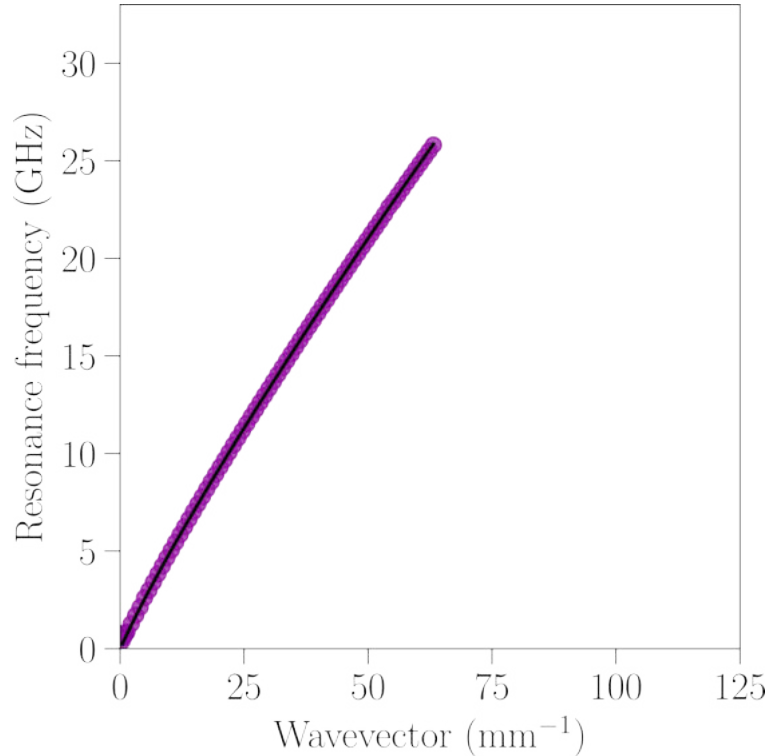
Plasmon dispersion relation

Dispersion relation $\omega(k)$



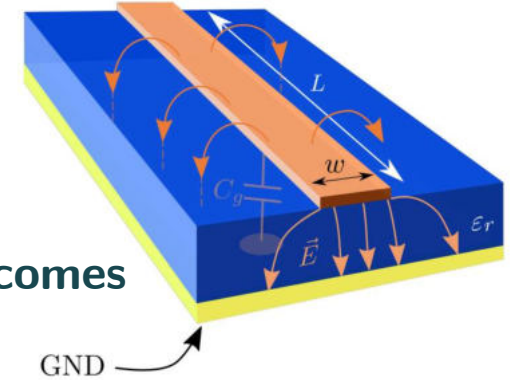
Plasmon dispersion relation

Dispersion relation $\omega(k)$



Remote ground plane :

Capacitance to ground becomes
frequency-dependent $C(k)$

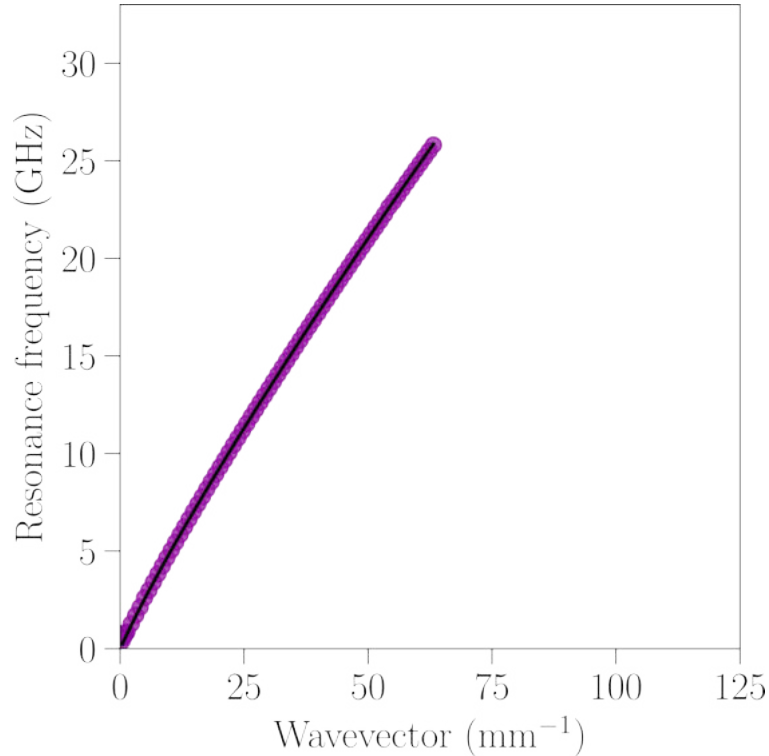


D. Basko, Private communications



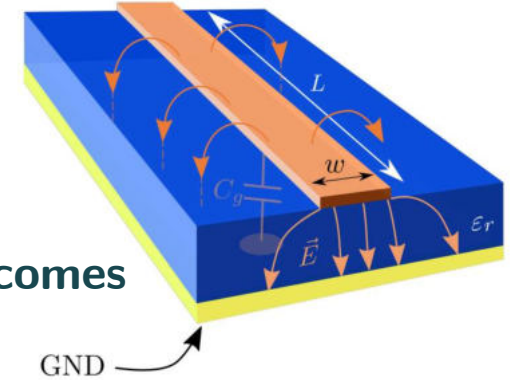
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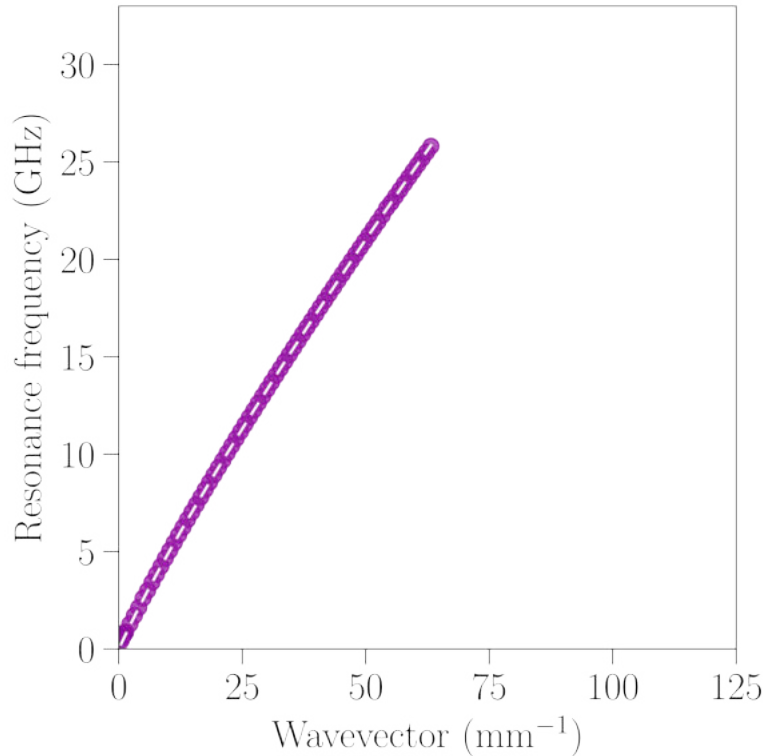
Plasmon velocity slightly k -dependent

$$\omega(k) = \frac{|k|}{\sqrt{L_K C(k)}} = v(k)|k|$$



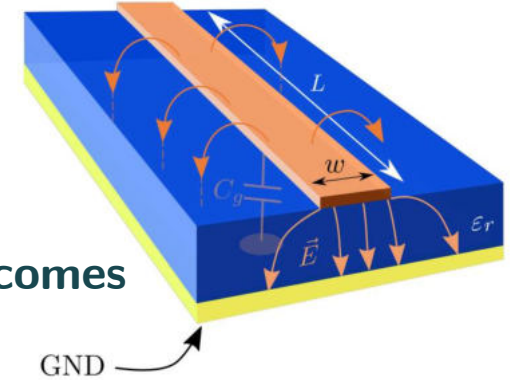
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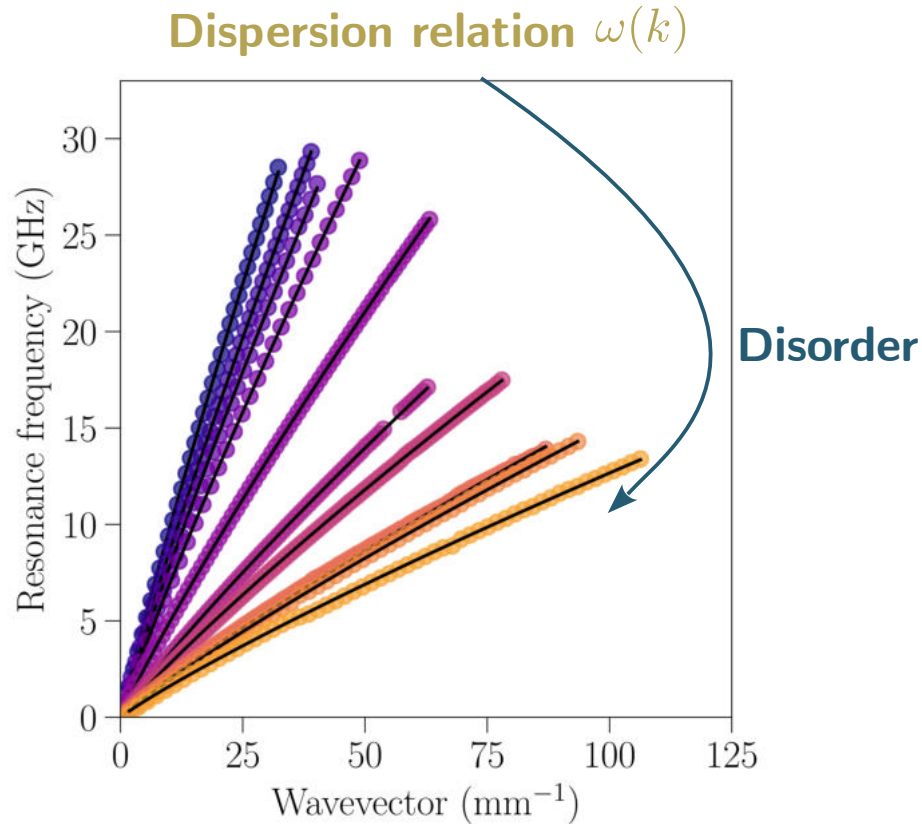
$$\omega(k) = \frac{|k|}{\sqrt{L_K C(k)}} = v(k)|k|$$

Only fitting parameter is L_K

Accurate determination of kinetic inductance



Plasmon dispersion relation



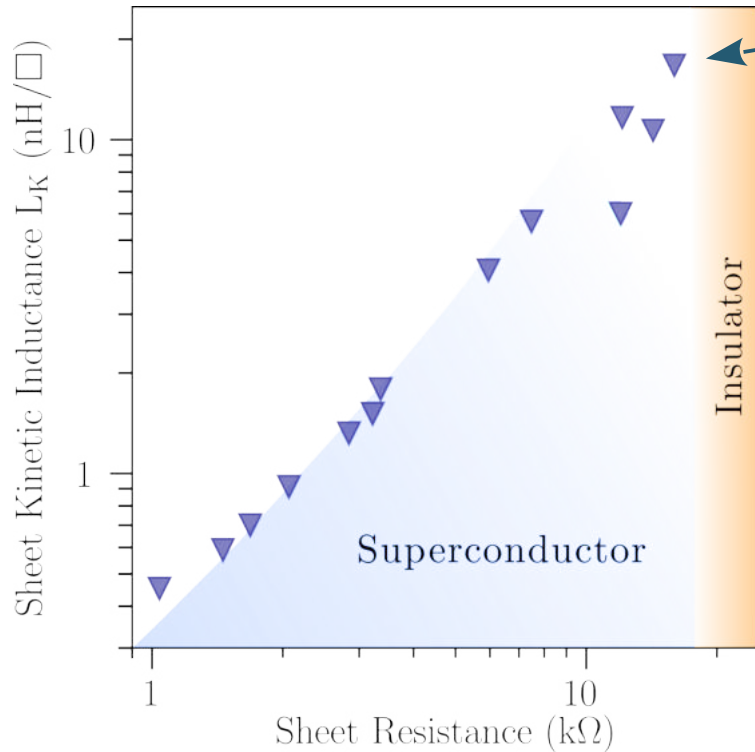
Extraction of kinetic inductance
for increasing disorder

$$\omega(k) \propto \frac{1}{\sqrt{L_K}}$$

Slope decreases with disorder



Kinetic inductance



17 nH/ \square

Qualitatively $L_K \approx \frac{\hbar R_n}{\pi \Delta}$

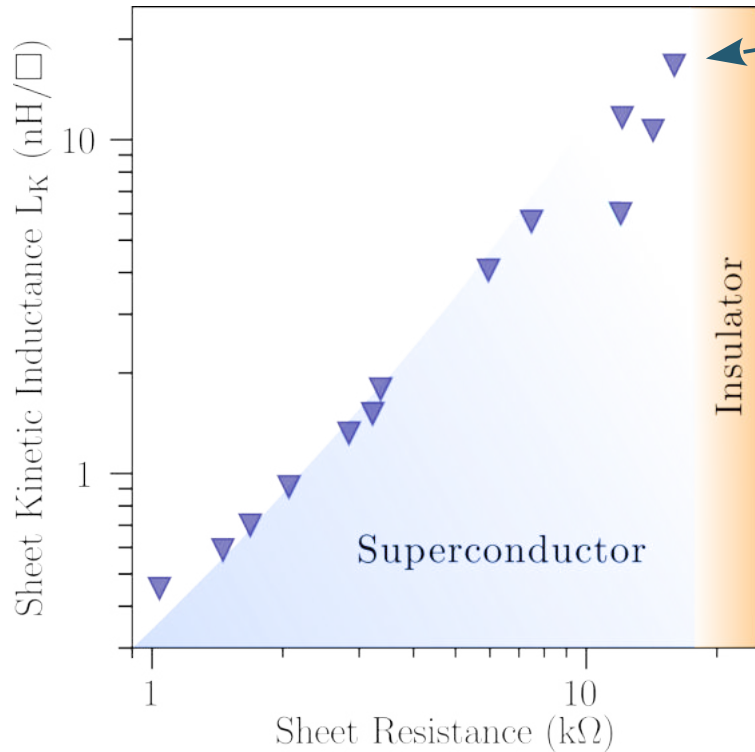
$L_K < \text{pH}/\square$: clean Aluminum films

$L_K = 1 - 4 \text{ nH}/\square$: typical granular Al used for cQED

Very large inductance : potential applications to cQED



Kinetic inductance



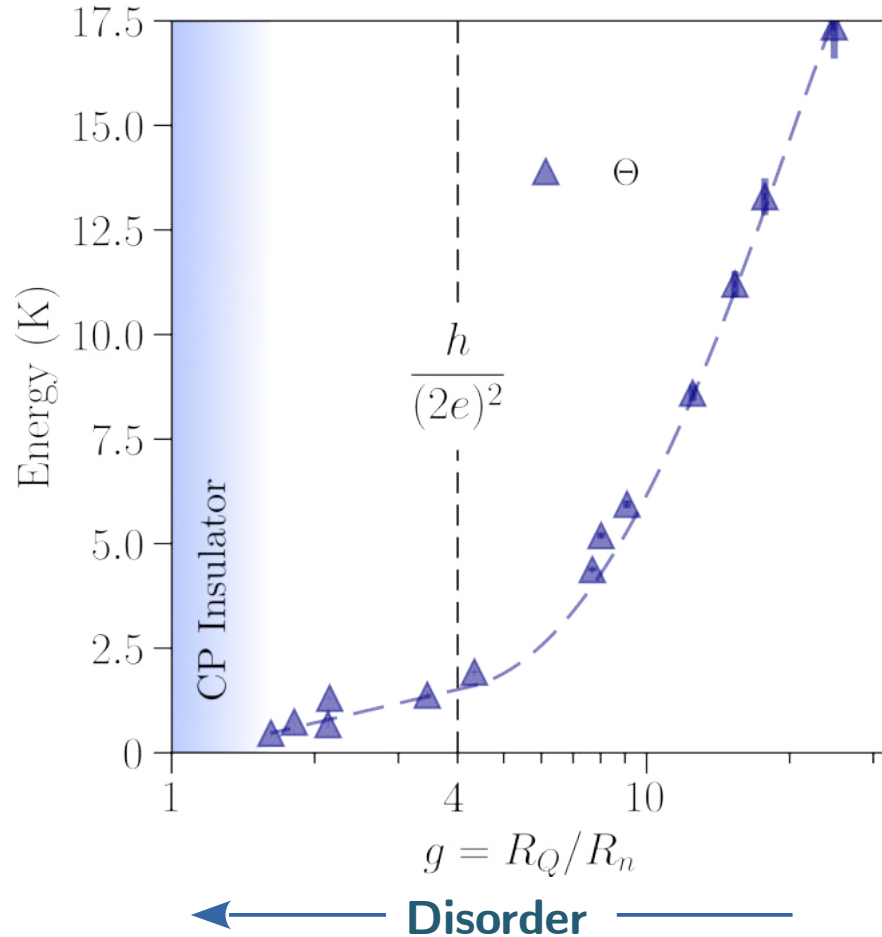
Qualitatively $L_K \approx \frac{\hbar R_n}{\pi \Delta}$

We obtain a measurement of the superfluid stiffness

$$\Theta = \left(\frac{\hbar}{2e} \right)^2 \frac{1}{L_K}$$



Superconductor ruled by phase fluctuations



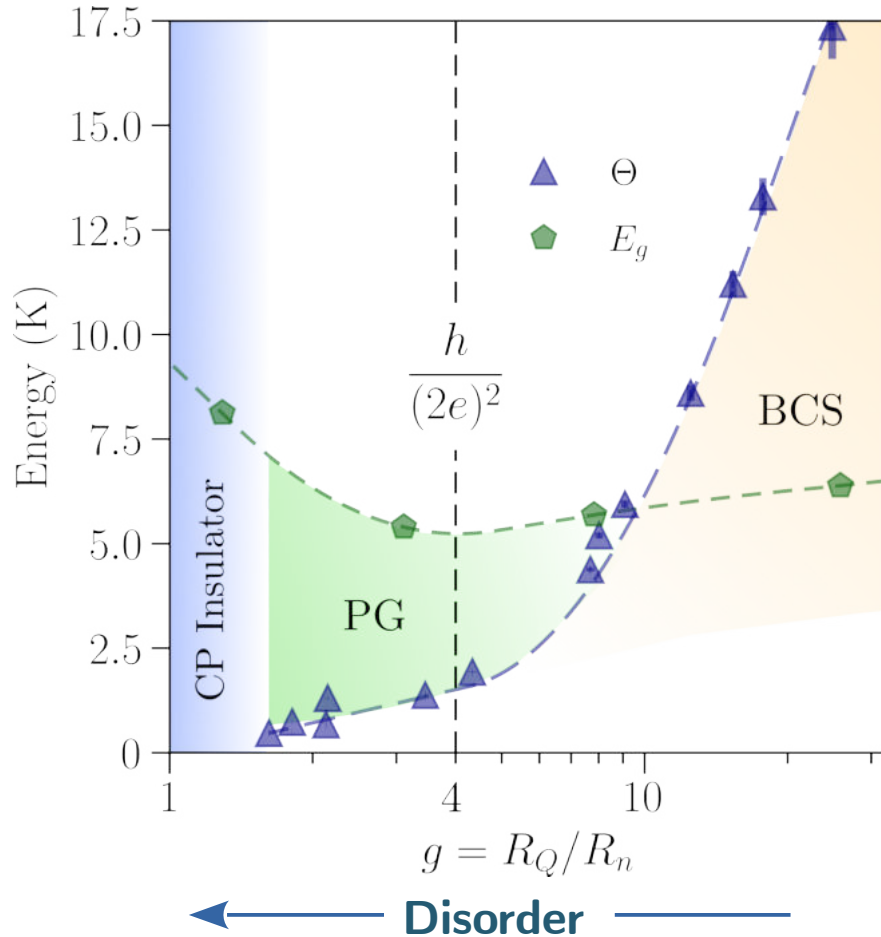
2D Superfluid stiffness

$$\Theta = \left(\frac{\hbar}{2e} \right)^2 \frac{1}{L_K} \approx E_J$$

BCS theory : $\Theta = \frac{1}{8} g \Delta$

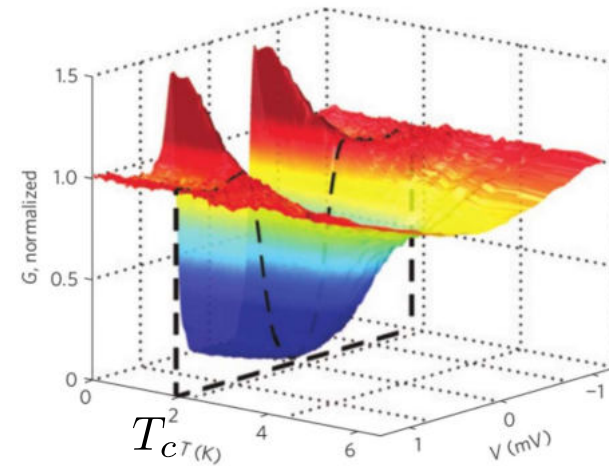


Superconductor ruled by phase fluctuations

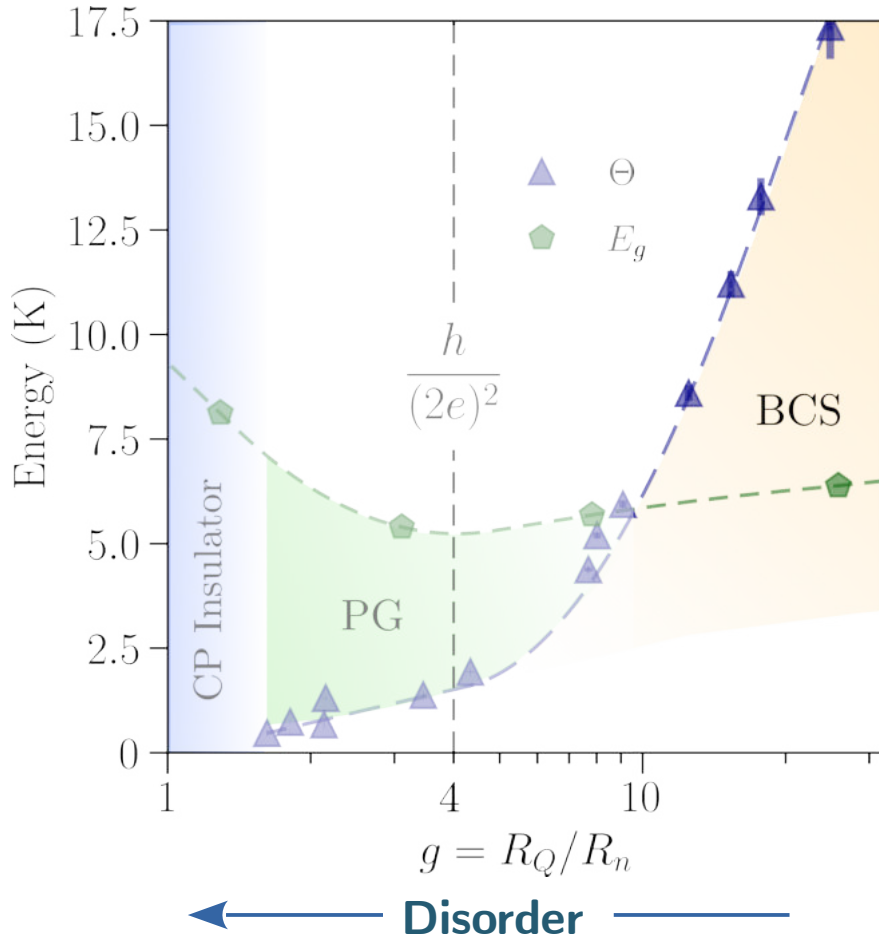


E_g = single particle gap
from tunneling measurement

Sacépé et al, Nature Physics (2011)
Sherman et al, PRB (2014)
Sacépé et al, PRB (2015)



Superconductor ruled by phase fluctuations



E_g = single particle gap
from tunneling measurement

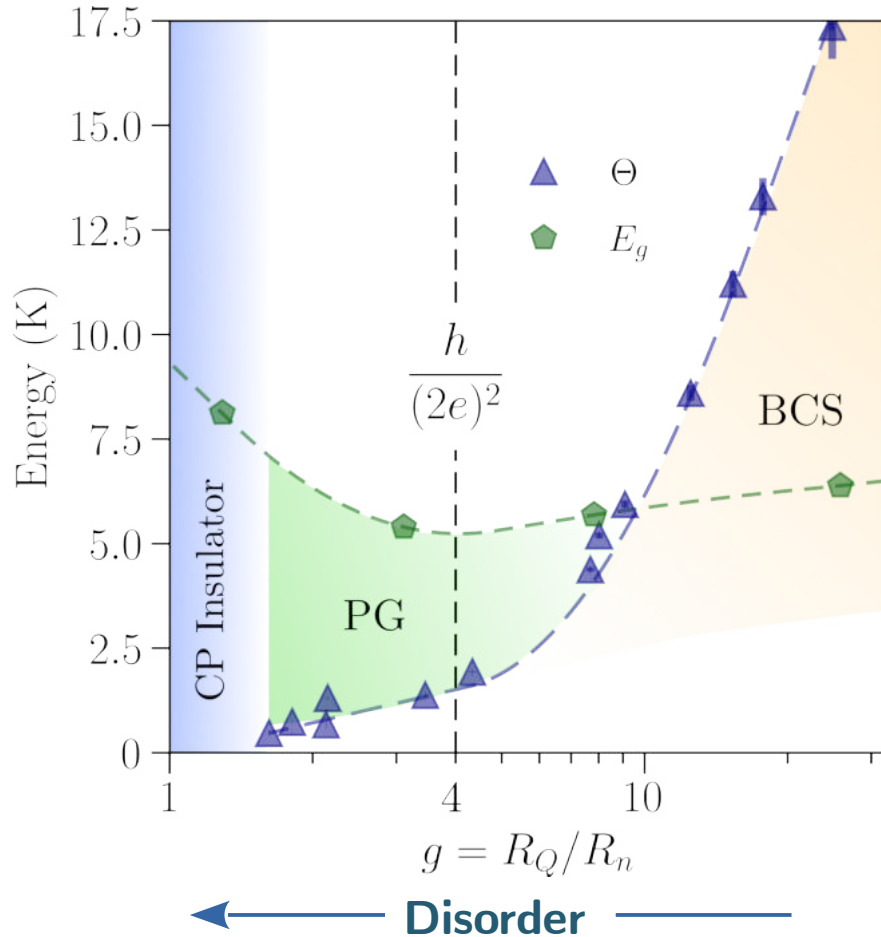
Sacépé et al, Nature Physics (2011)
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Sacépé et al, PRB (2015)

$\Theta \gg E_g = \Delta$: BCS superconductor

Phase fluctuations can be neglected



Superconductor ruled by phase fluctuations



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$\Theta \gg E_g = \Delta$: BCS superconductor

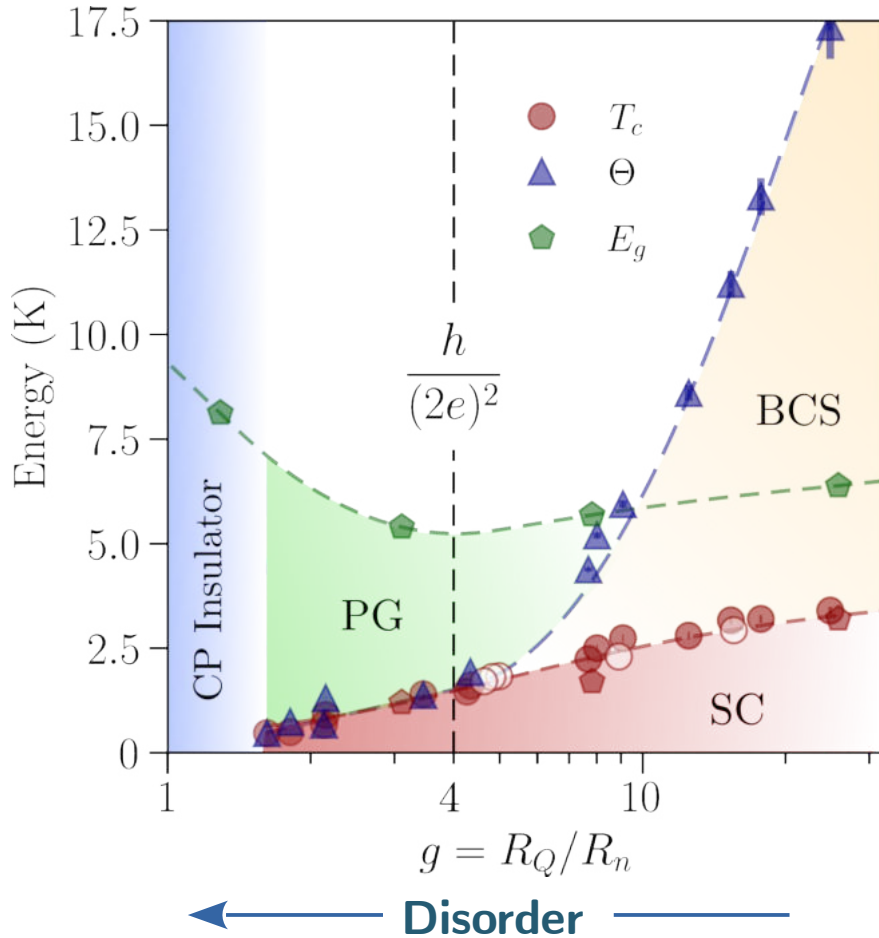
Phase fluctuations can be neglected

$\Theta \leq E_g$: Pseudo-gap superconductor

Phase fluctuations become predominant



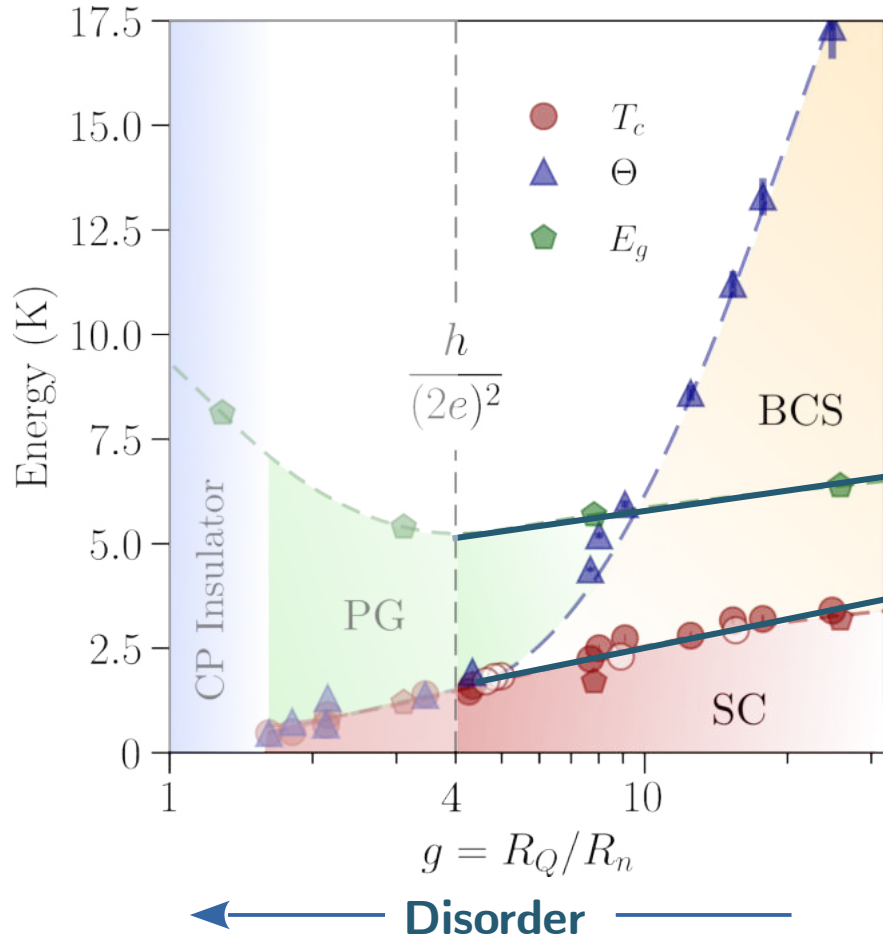
Superconductor ruled by phase fluctuations



Critical temperature T_c from DC measurements



Superconductor ruled by phase fluctuations



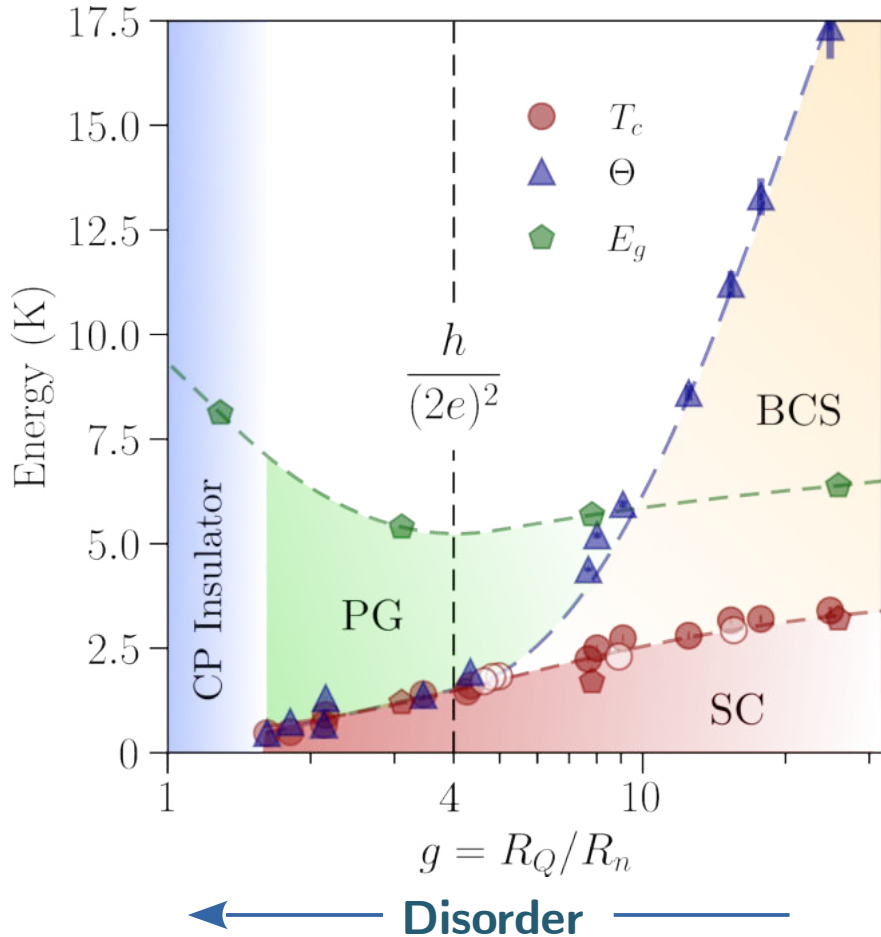
Critical temperature T_c from DC measurements

BCS region : T_c defined by pairing $E_g \sim 2k_B T_c$

$$E_g \propto T_c$$



Superconductor ruled by phase fluctuations



Critical temperature T_c from DC measurements

BCS region : T_c defined by pairing $E_g \sim 2k_B T_c$

Pseudo-gap region : T_c defined by Θ

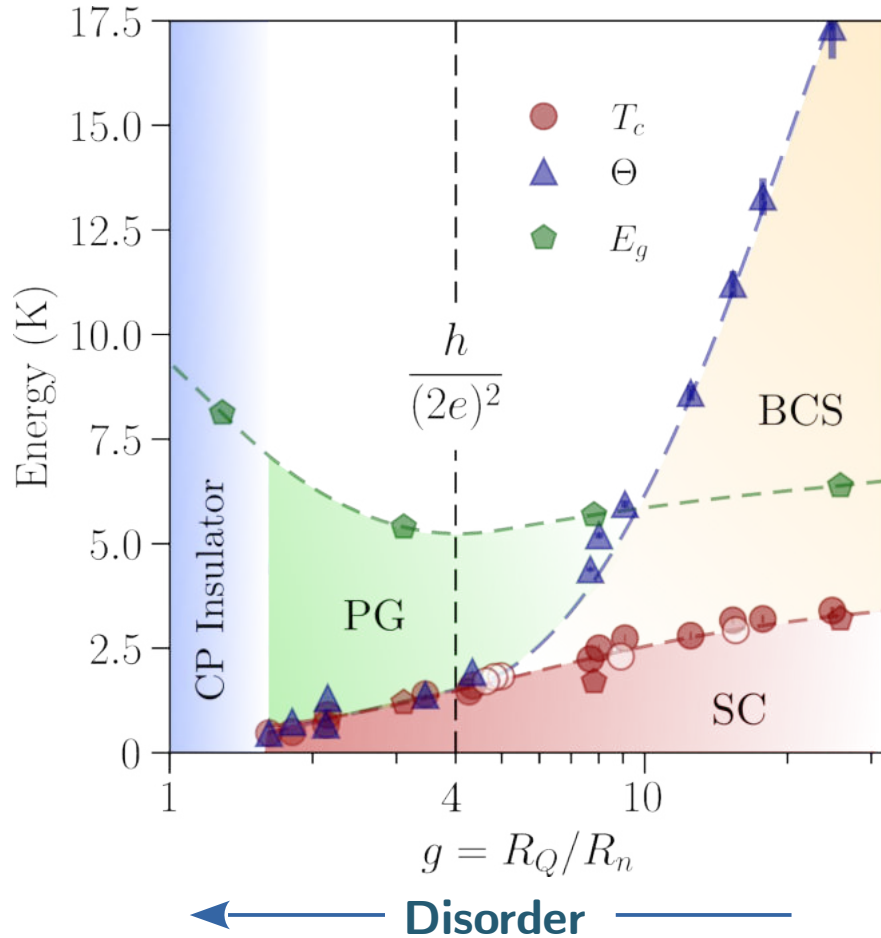
$$T_c = \Theta$$

Superconductivity ruled by phase fluctuations

Emery and Kivelson, Nature (1995)



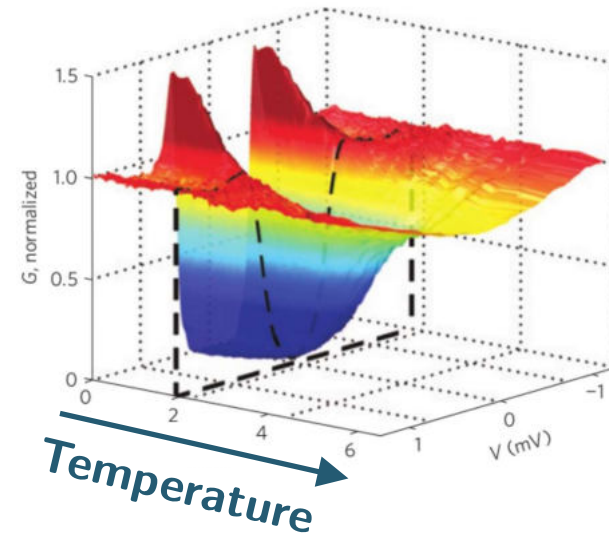
Superconductor ruled by phase fluctuations



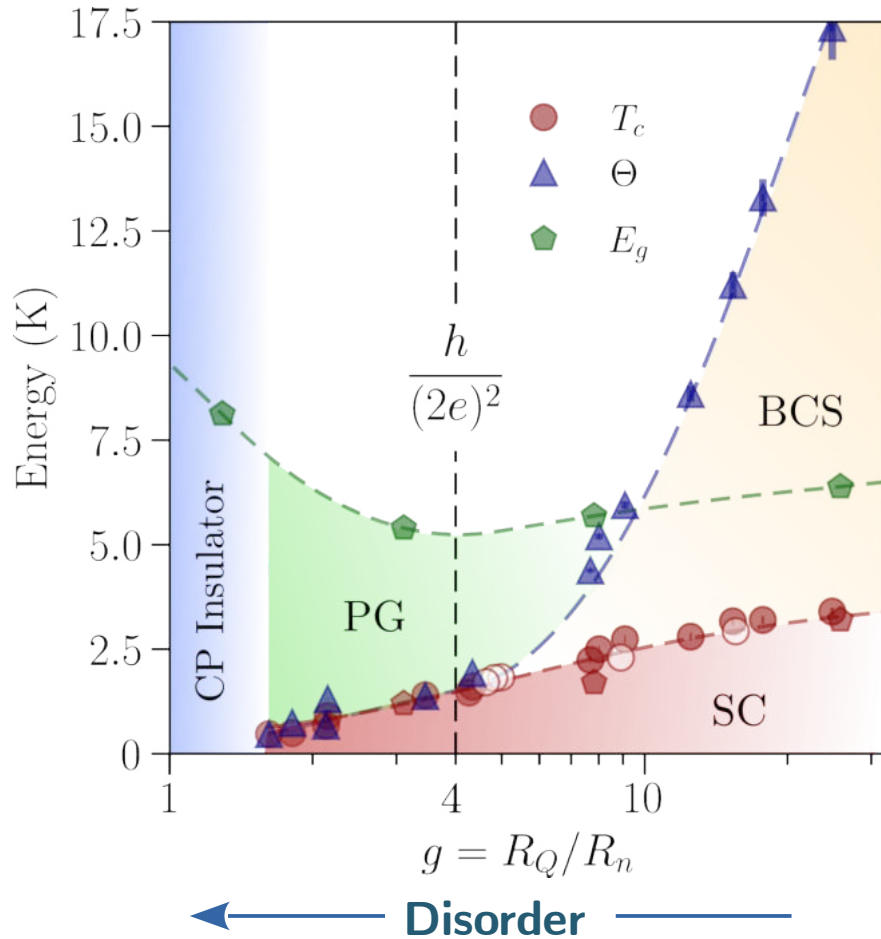
In the pseudo-gap region

$$T_c = \Theta$$

DOS versus temperature



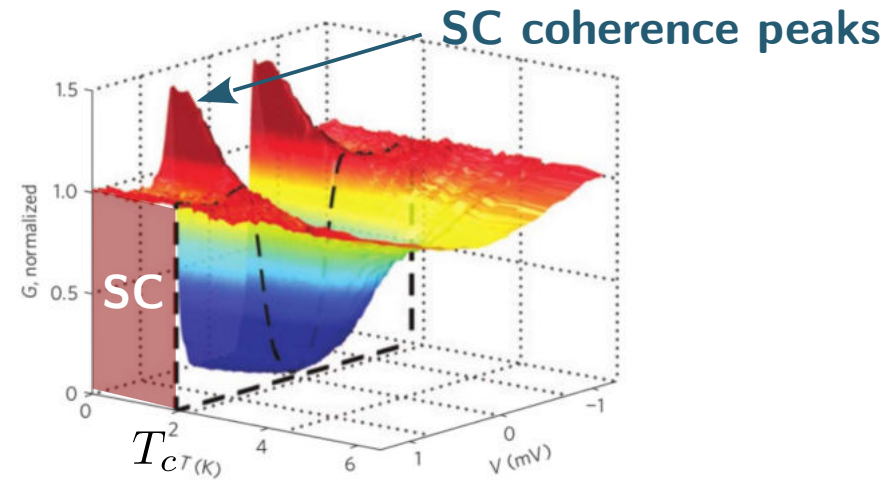
Superconductor ruled by phase fluctuations



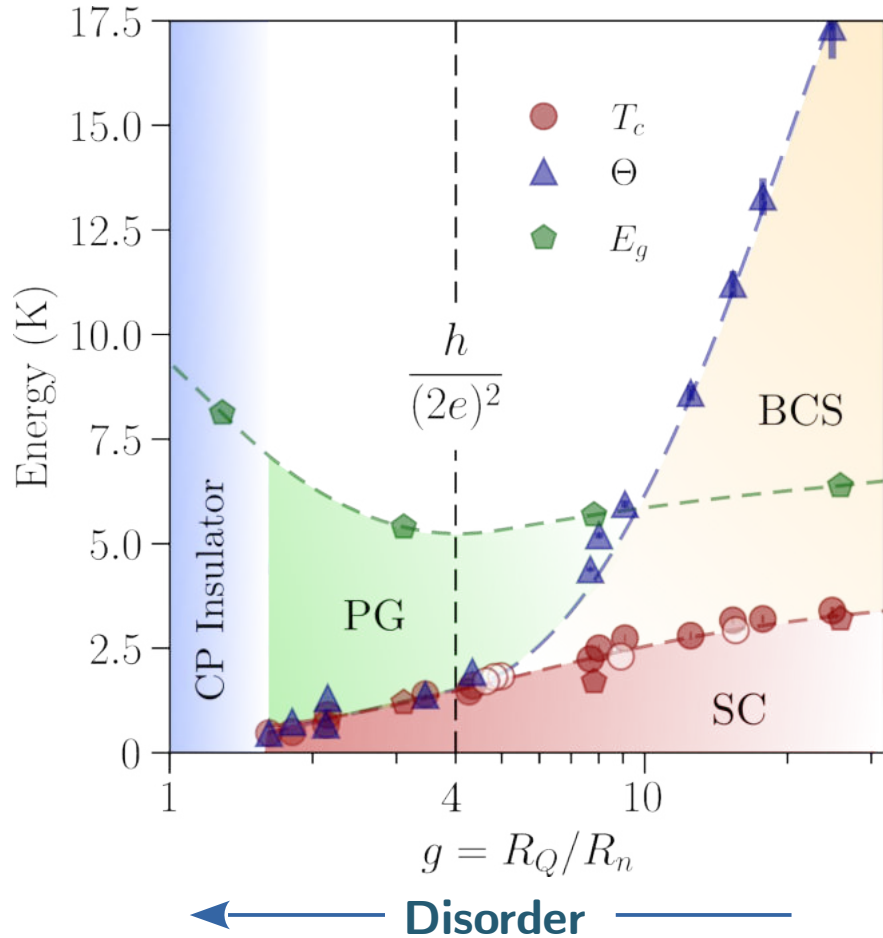
In the pseudo-gap region

$$T_c = \Theta$$

DOS versus temperature



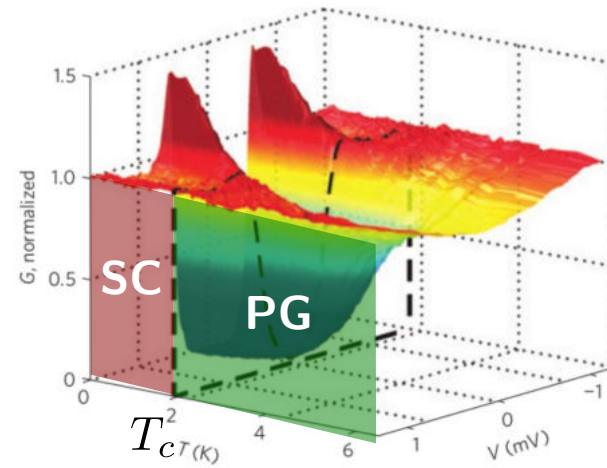
Superconductor ruled by phase fluctuations



In the pseudo-gap region

$$T_c = \Theta$$

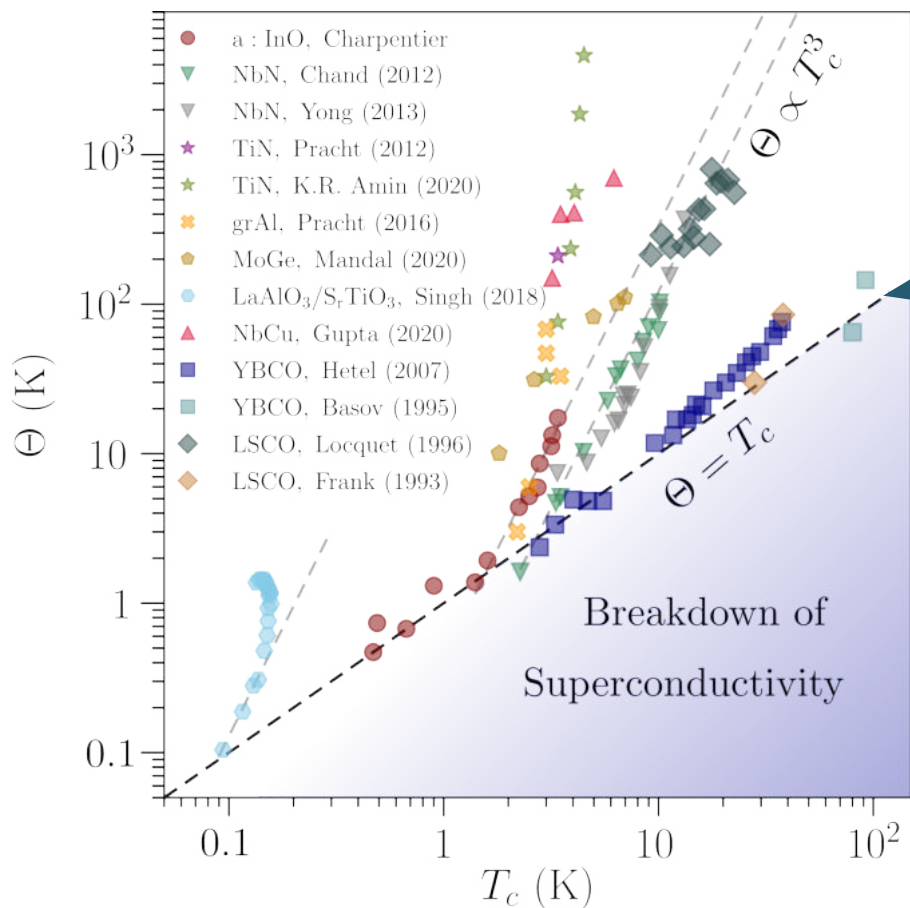
DOS versus temperature



Pseudogap



Role of phase fluctuations in low-density SCs



Critical line $\Theta = T_c$

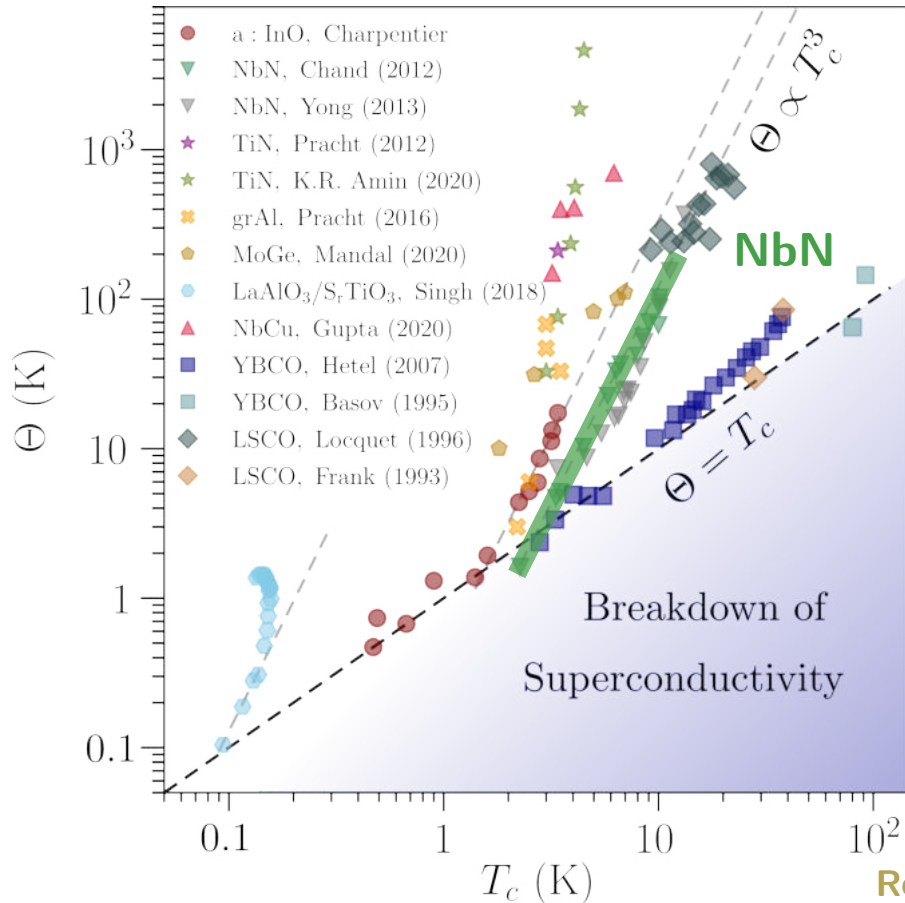
Emery and Kivelson, Nature (1995)

Review article :

Raychaudhuri and Dutta, Journal of Physics: Cond. Mat. (2021)



Role of phase fluctuations in low-density SCs



PHYSICAL REVIEW B **85**, 014508 (2012)

NbN

Phase diagram of the strongly disordered *s*-wave superconductor NbN close to the metal-insulator transition

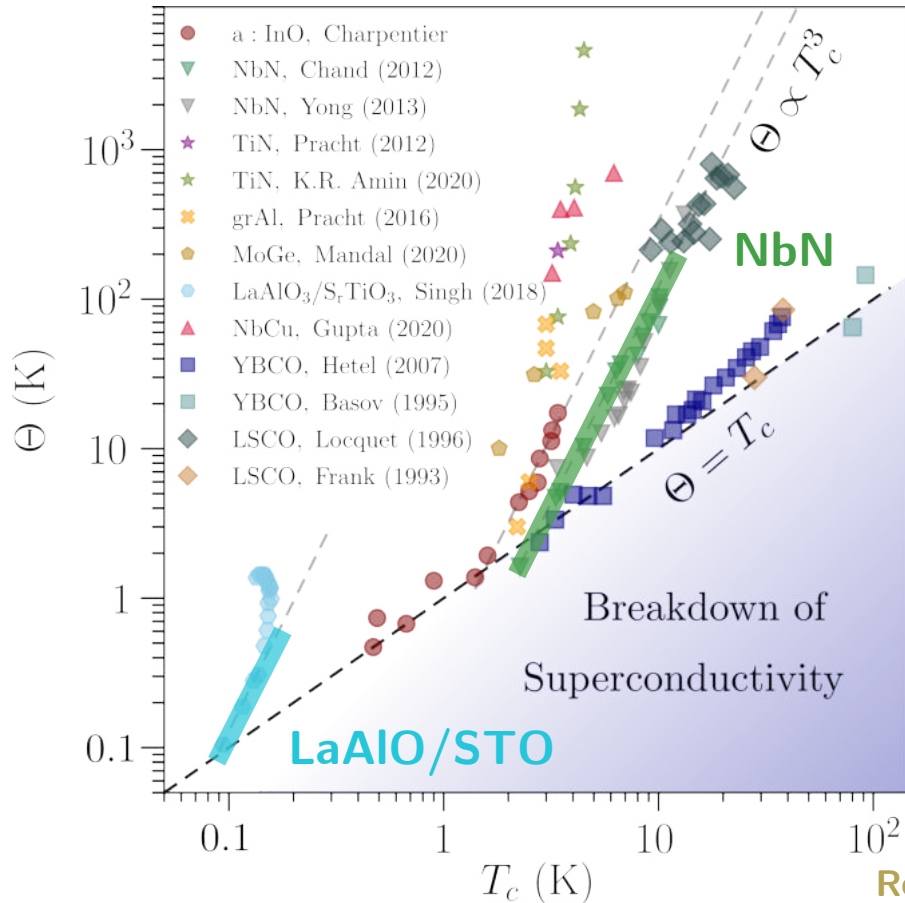
Madhavi Chand,¹ Garima Saraswat,¹ Anand Kamlapure,¹ Mintu Mondal,¹ Sanjeev Kumar,¹ John Jesudasan,¹ Vivas Bagwe,¹ Lara Benfatto,² Vikram Tripathi,¹ and Pratap Raychaudhuri^{1,*}

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Raychaudhuri and Dutta, *Journal of Physics: Cond. Mat.* (2021)



Role of phase fluctuations in low-density SCs



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LaAlO/STO

ARTICLE

DOI: 10.1038/ncomms41467-018-02907-8 OPEN

Competition between electron pairing and phase coherence in superconducting interfaces

G. Singh^{1,2}, A. Jouan^{1,2}, L. Benfatto^{3,4}, F. Couëdo^{1,2}, P. Kumar⁵, A. Dogra⁵, R.C. Budhani⁶, S. Caprara^{3,4}, M. Grilli^{3,4}, E. Lesne⁷, A. Barthélémy⁷, M. Bibes⁷, C. Feuillet-Palma^{1,2}, J. Lesueur^{1,2} & N. Bergeal^{1,2}

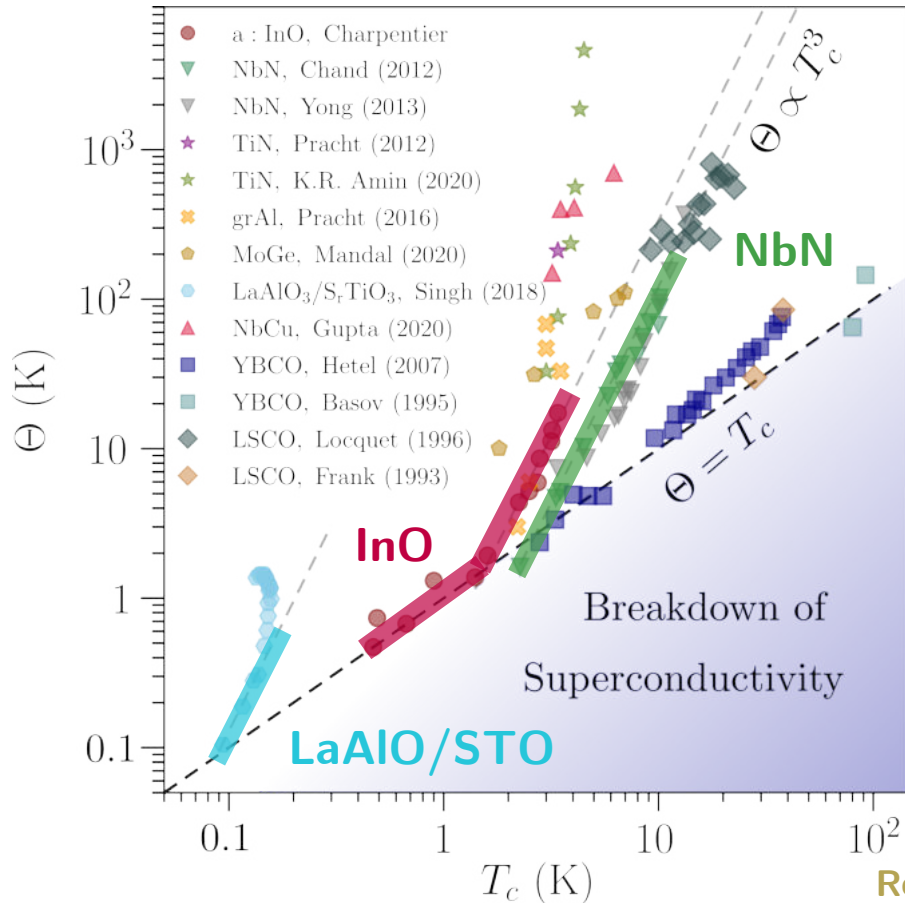
But also grAl, high- T_c superconductors ...

Review article :

Raychaudhuri and Dutta, Journal of Physics: Cond. Mat. (2021)



Role of phase fluctuations in low-density SCs



And Indium oxide

Review article :

Raychaudhuri and Dutta, Journal of Physics: Cond. Mat. (2021)

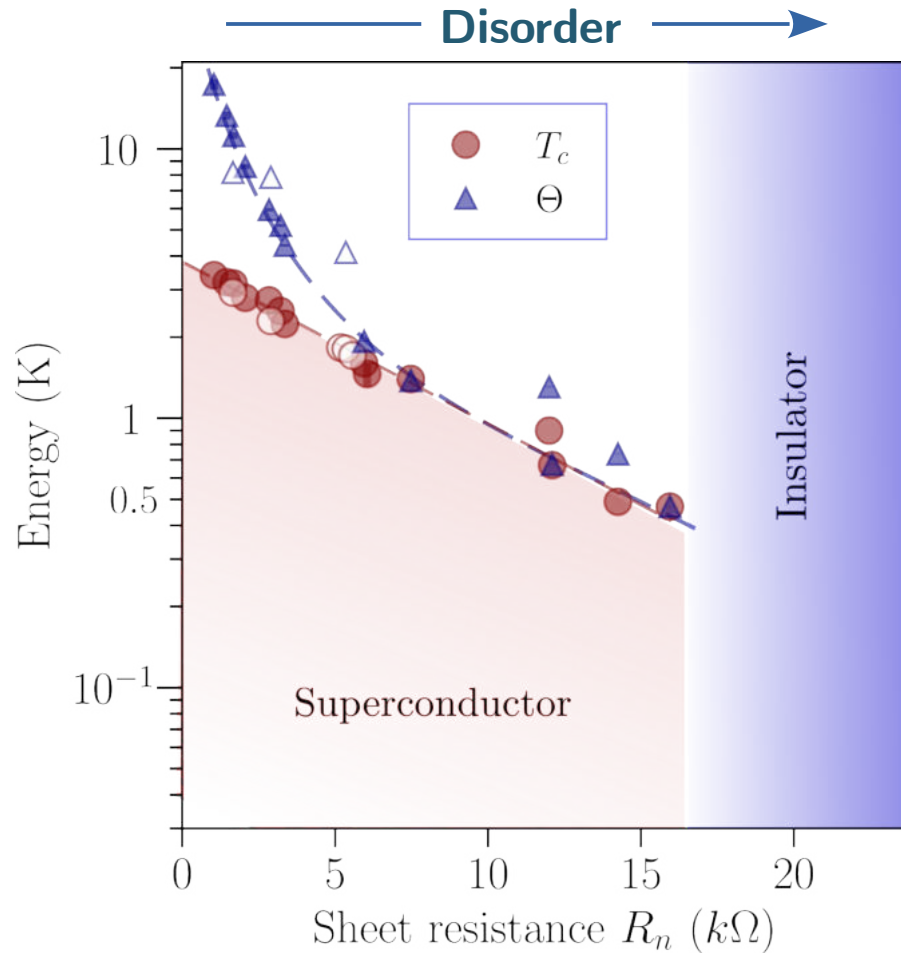


Nature of the $T=0$ phase transition ?

Superconductor-Insulator quantum phase transition driven by disorder



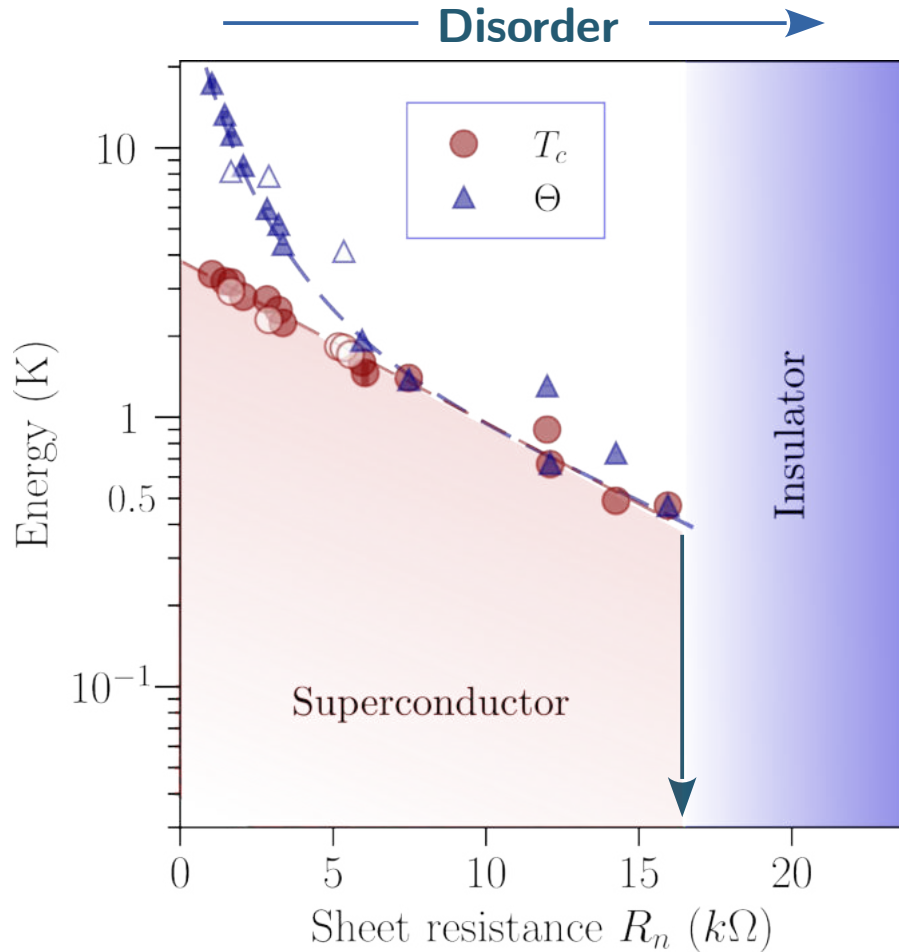
Nature of the $T=0$ phase transition



T_c and Θ versus R in log scale



Nature of the $T=0$ phase transition



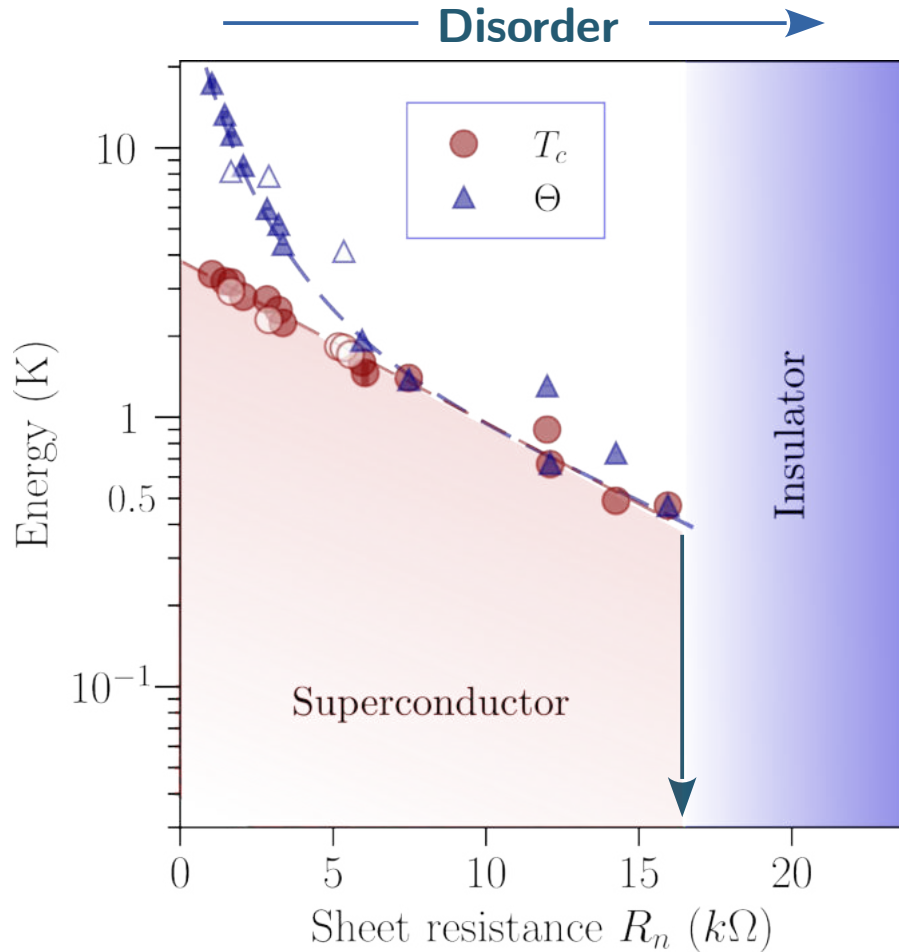
Θ and T_c are finite at SIT

$$T_c \sim \Theta \sim 0.5 \text{ K}$$

Abrupt drop of T_c and Θ at the critical disorder



Nature of the $T=0$ phase transition



Θ and T_c are finite at SIT

$$T_c \sim \Theta \sim 0.5 \text{ K}$$

Abrupt drop of T_c and Θ at the critical disorder

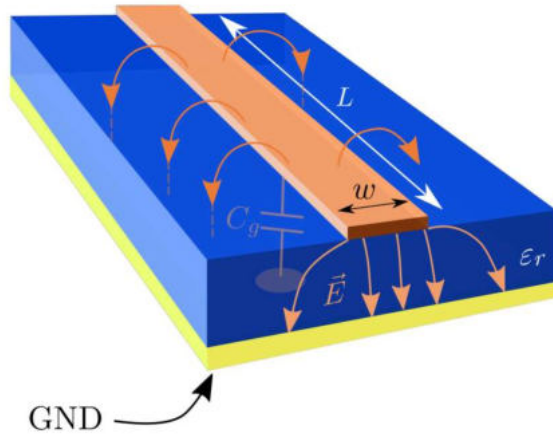
Why this jump ?

First idea : quantum BKT transition in (1+1)D



(1+1)D BKT transition

1D plasmons



Our wires are 1D with respect to plasmon modes

$$w = 1 \mu\text{m}$$

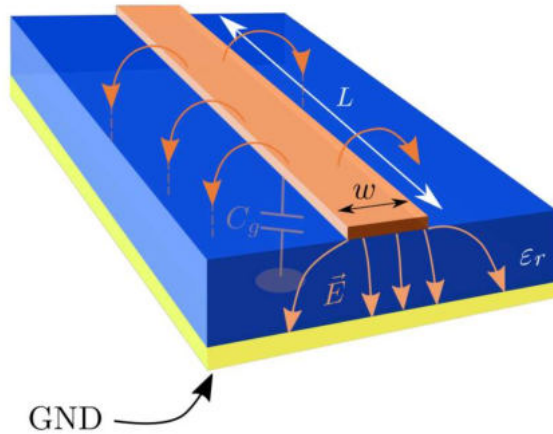
$$d = 40 \text{ nm} \longrightarrow \lambda_L \gg wd$$

$$L = 3.5 \text{ mm} \quad \mathbf{1D \text{ Coulomb potential}}$$



(1+1)D BKT transition

1D plasmons

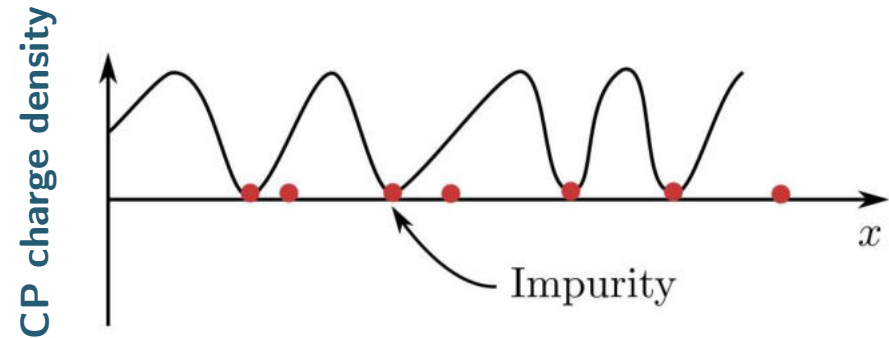


$$w = 1 \mu\text{m}$$

$$d = 40 \text{ nm} \longrightarrow \lambda_L \gg wd$$

$$L = 3.5 \text{ mm} \quad \mathbf{1D \text{ Coulomb potential}}$$

Pinning of plasmons by disorder



Giamarchi and Schulz, PRB (1988)



(1+1)D BKT transition

Wave impedance

$$Z = \sqrt{\frac{L_K^{\square}}{wC'}}$$

Superfluid to Bose glass transition (1+1)D BKT

$$Z_c = \frac{R_Q^S}{3} \quad \text{where} \quad R_Q^S = \frac{h}{(2e)^2}$$

Giamarchi and Schulz, PRB (1988)

Bard et al, PRB (2017)

Houzet and Glazman, PRL (2019)

See also in JJ arrays :

Cedergren et al, PRL (2017)

Kuzmin et al, Nature Physics (2019)

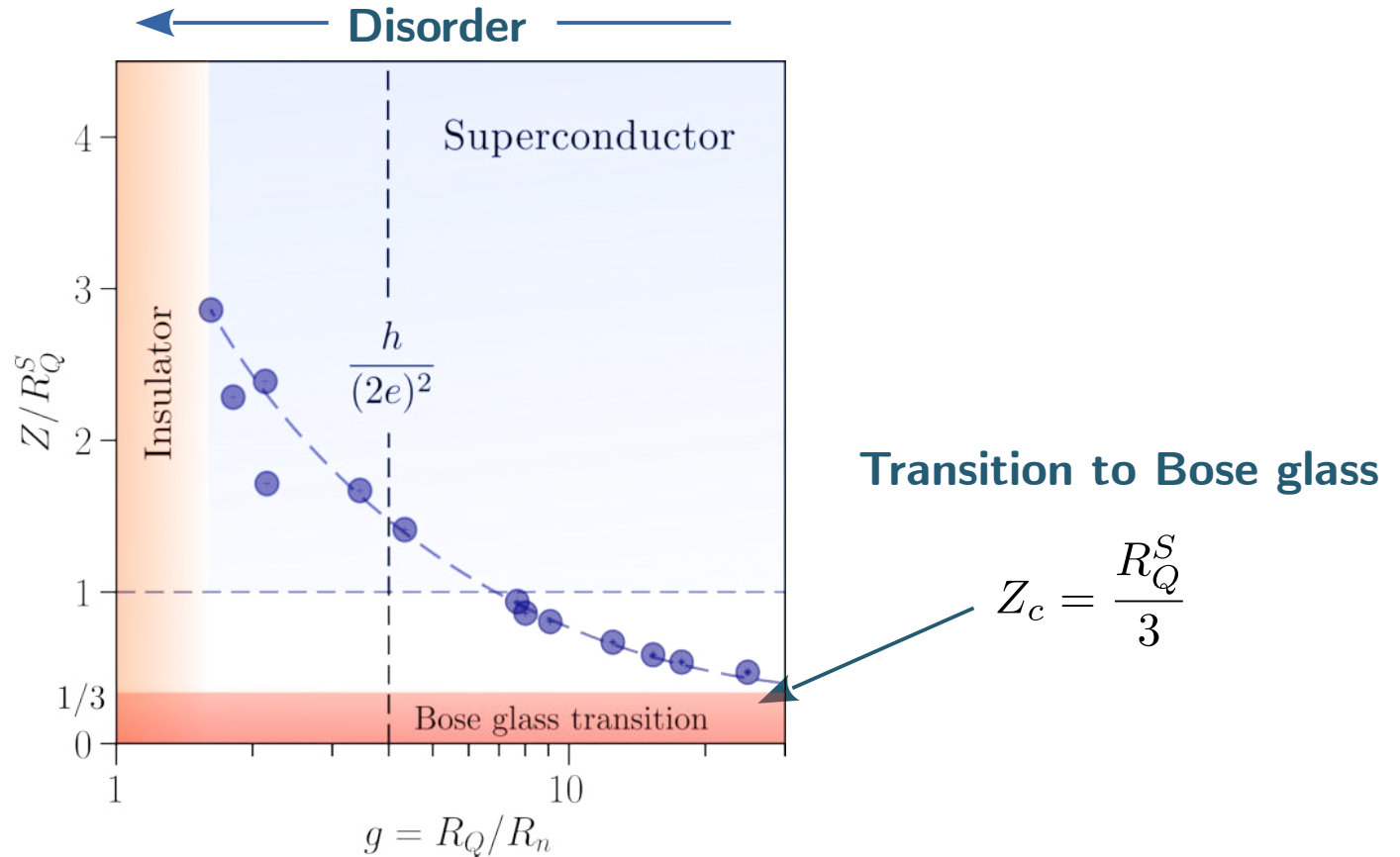
Mukhopadhyay et al, arXiv (2022)



(1+1)D BKT transition

Wave impedance

$$Z = \sqrt{\frac{L_K \square}{wC'}}$$



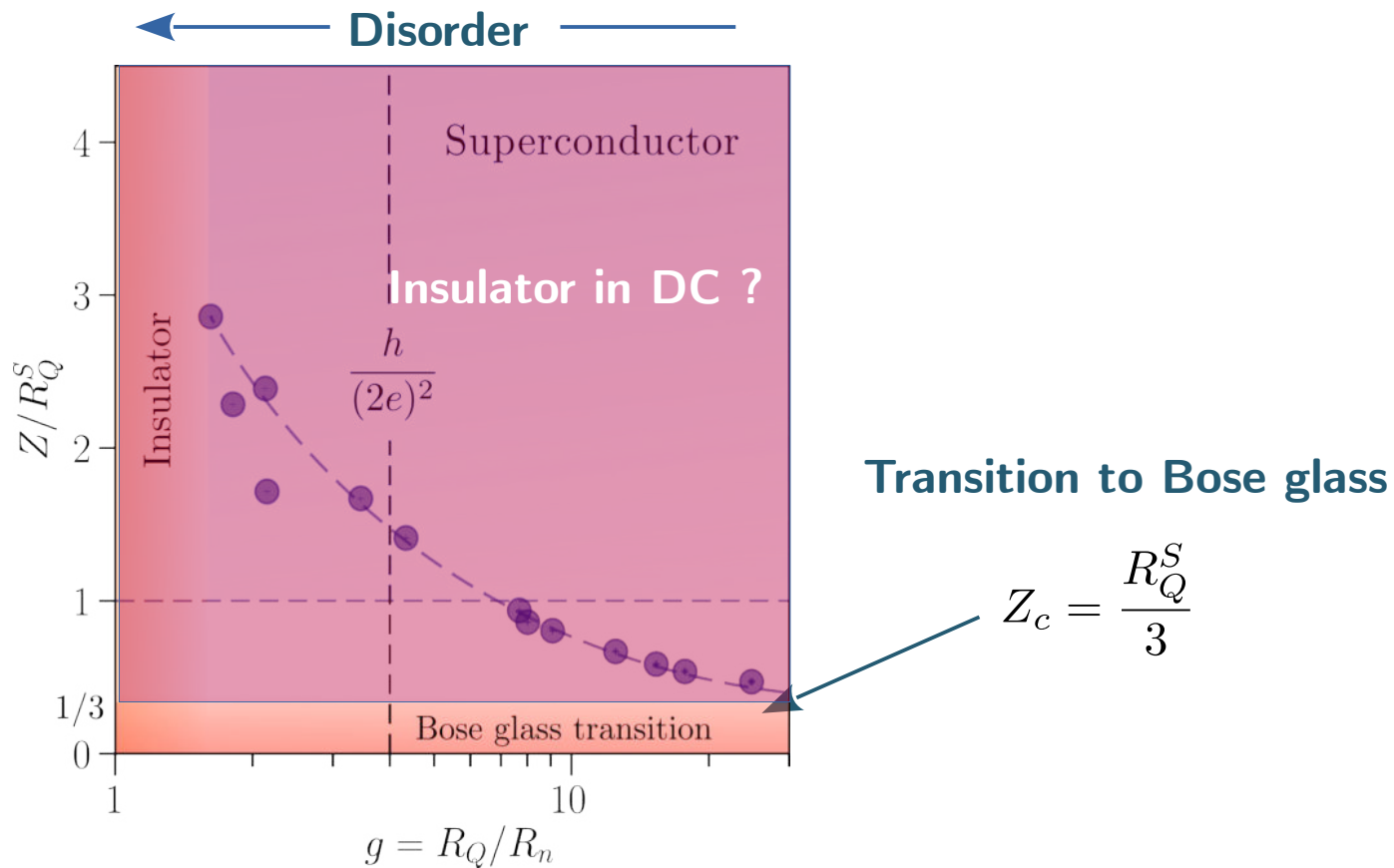
All samples would be insulating in DC !!



(1+1)D BKT transition

Wave impedance

$$Z = \sqrt{\frac{L_K^{\square}}{wC'}}$$



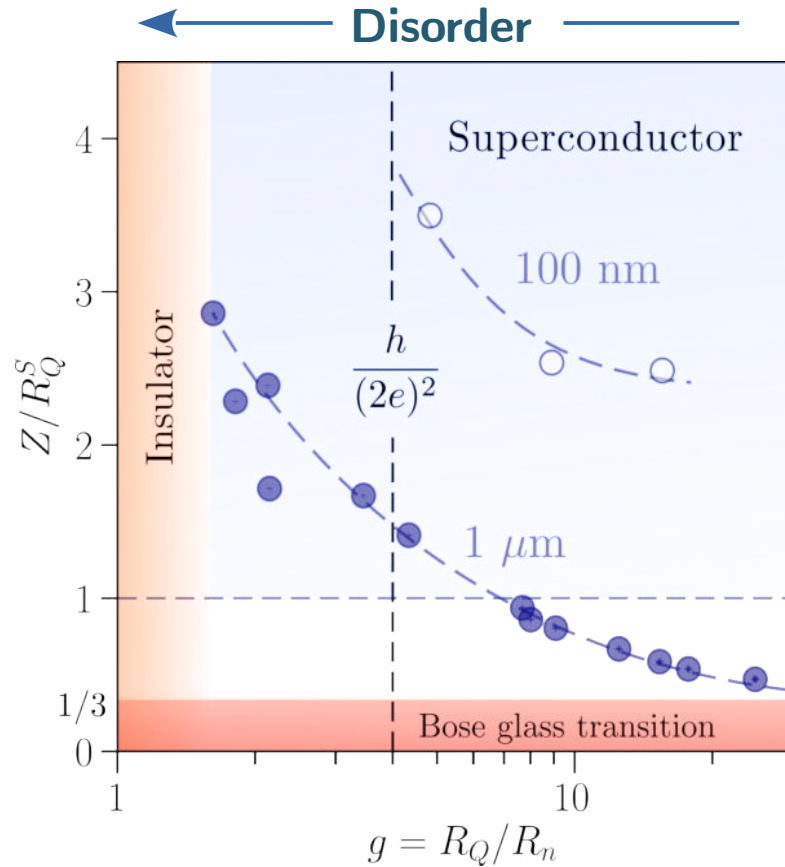
All samples would be insulating in DC !!



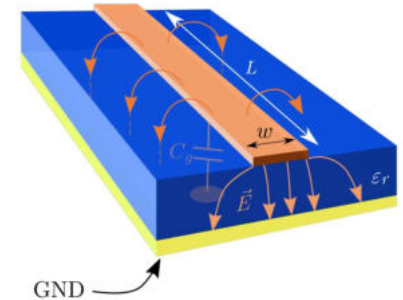
(1+1)D BKT transition

Wave impedance

$$Z = \sqrt{\frac{L_K \square}{wC'}}$$



Nanowires



$$w = 0.1 \mu\text{m}$$

$$d = 40 \text{ nm}$$

$$L = 0.3 \text{ mm}$$

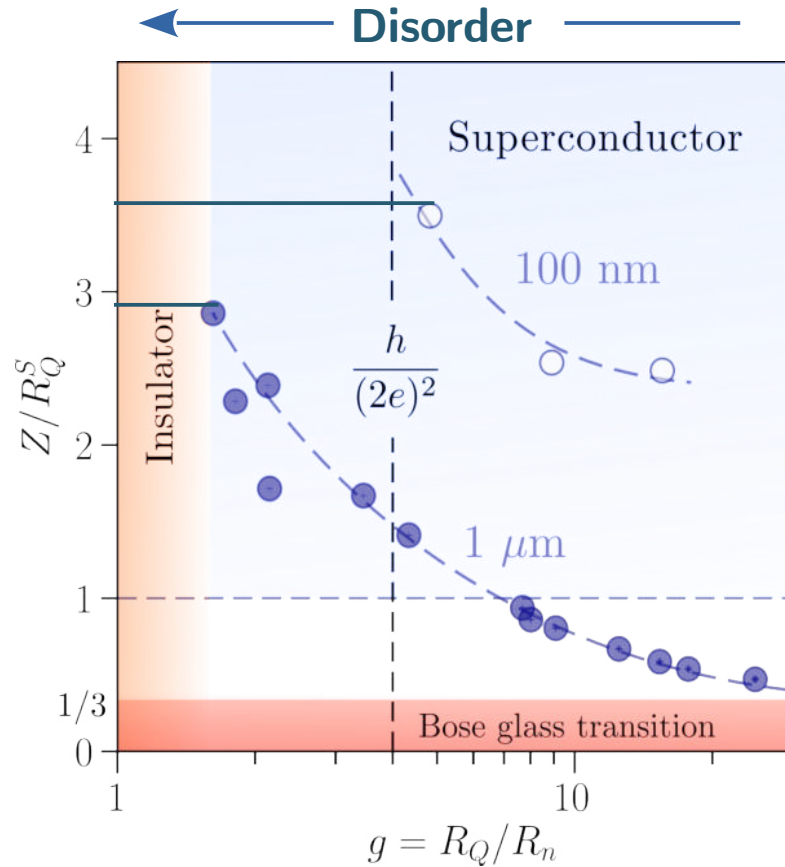
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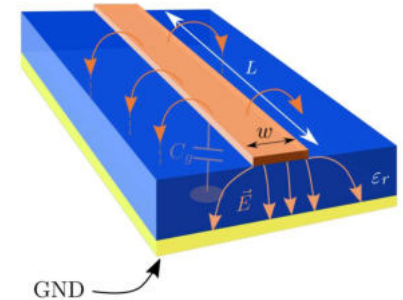
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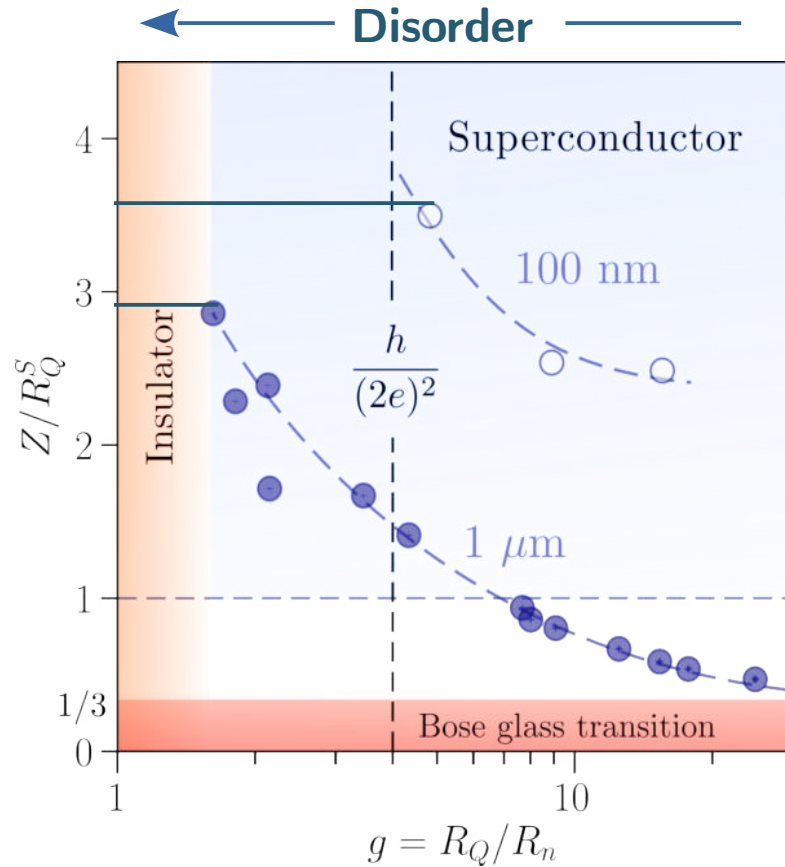
All samples would be insulating in DC !!



(1+1)D BKT transition

Wave impedance

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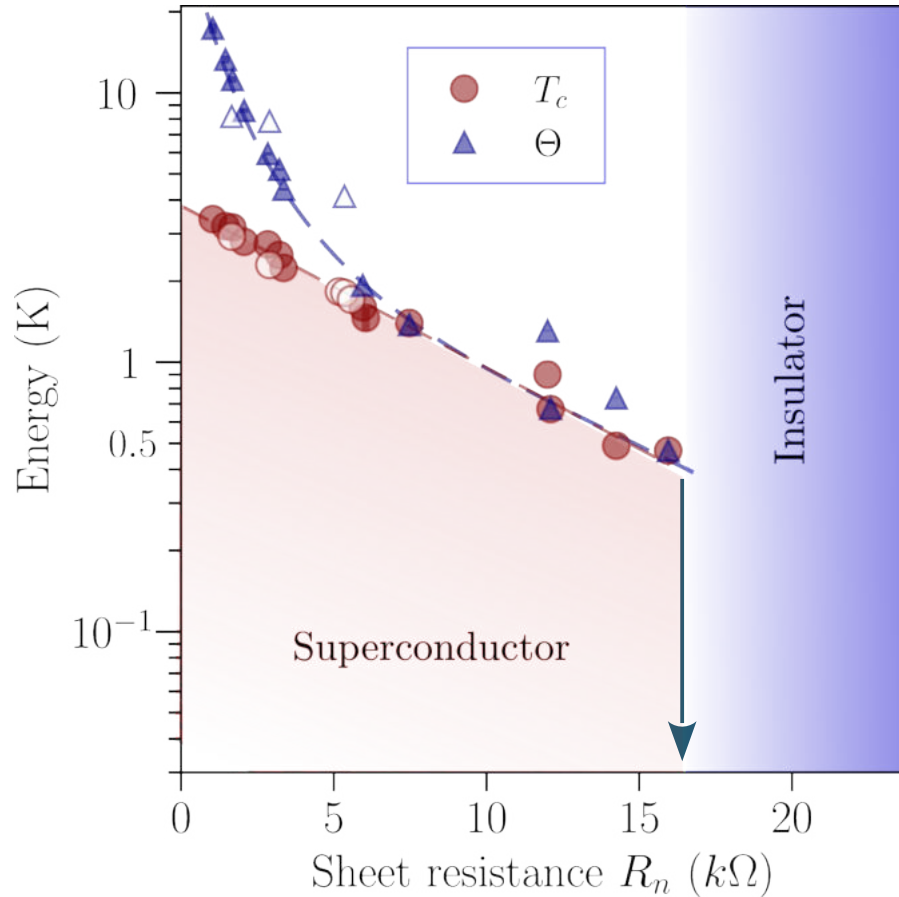
Conclusion

Bose glass transition seems incompatible with indium oxide data

All samples would be insulating in DC !!



Nature of the $T=0$ phase transition



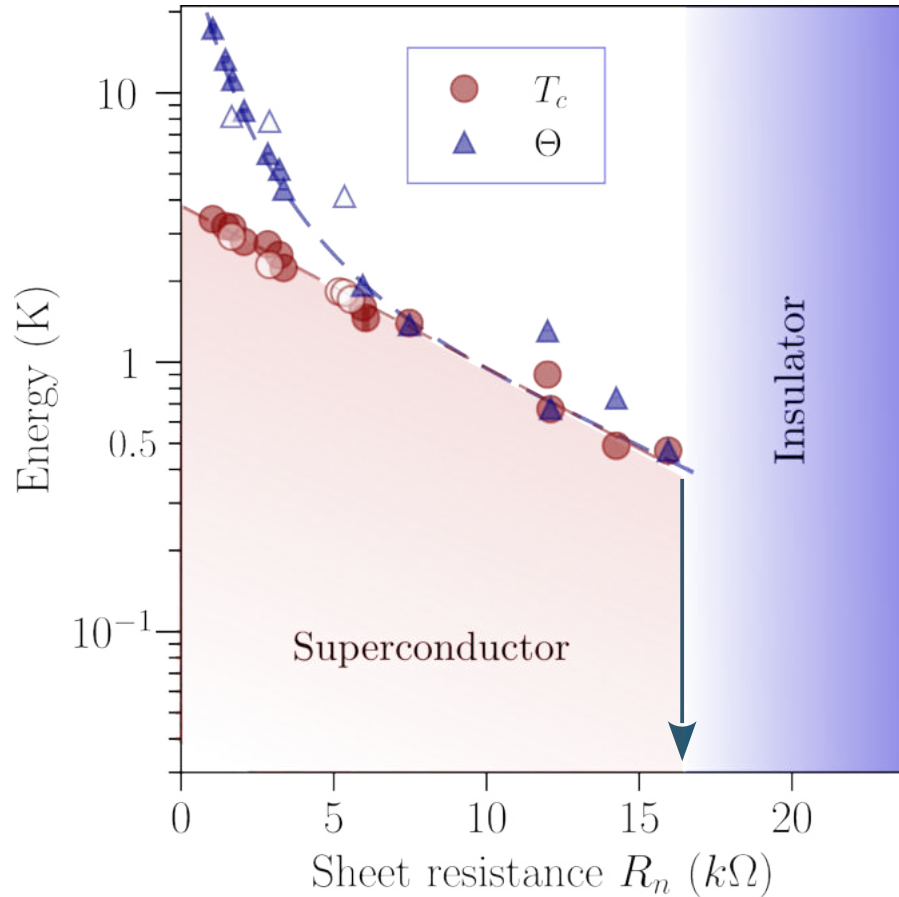
Θ and T_c are finite at SIT

Next scenario :

First-order quantum phase transition ?



Nature of the $T=0$ phase transition



Θ and T_c are finite at SIT

Next scenario :

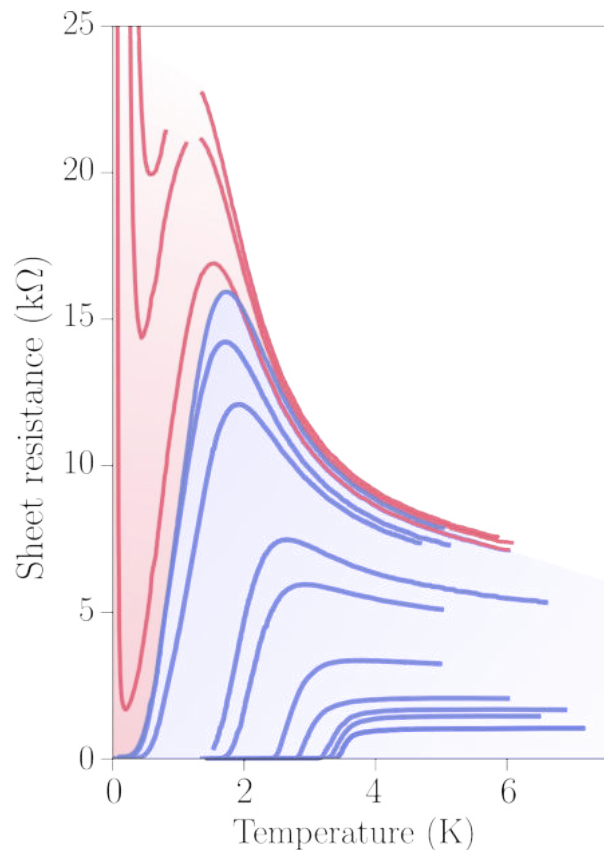
First-order quantum phase transition ?

New theories needed

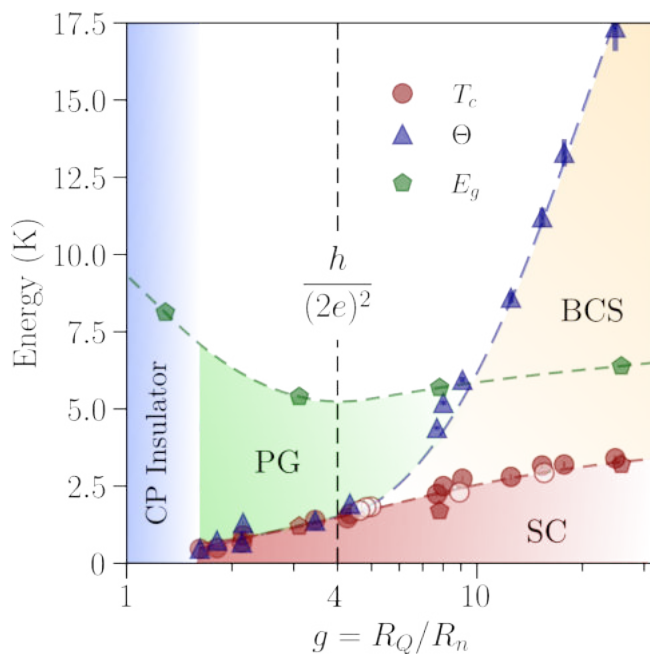


Conclusion

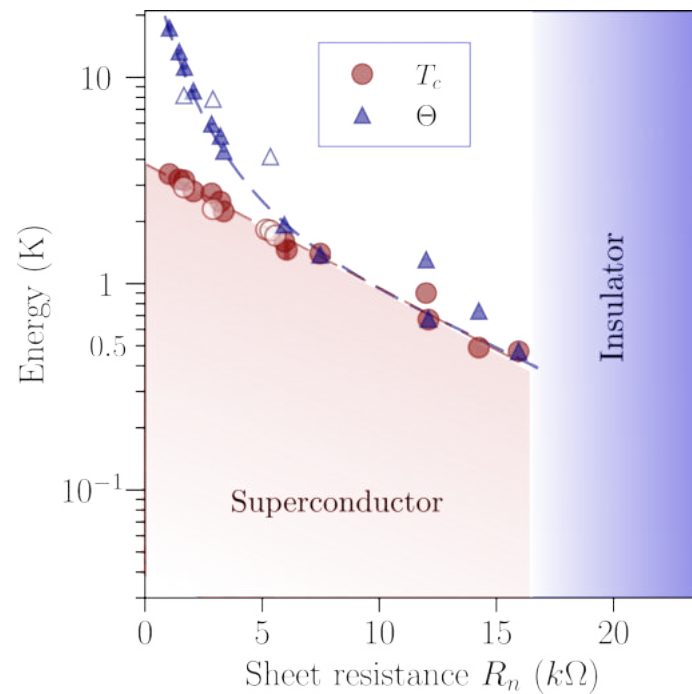
Superconductor-Insulator Transition



DC and cQED study of phase fluctuations

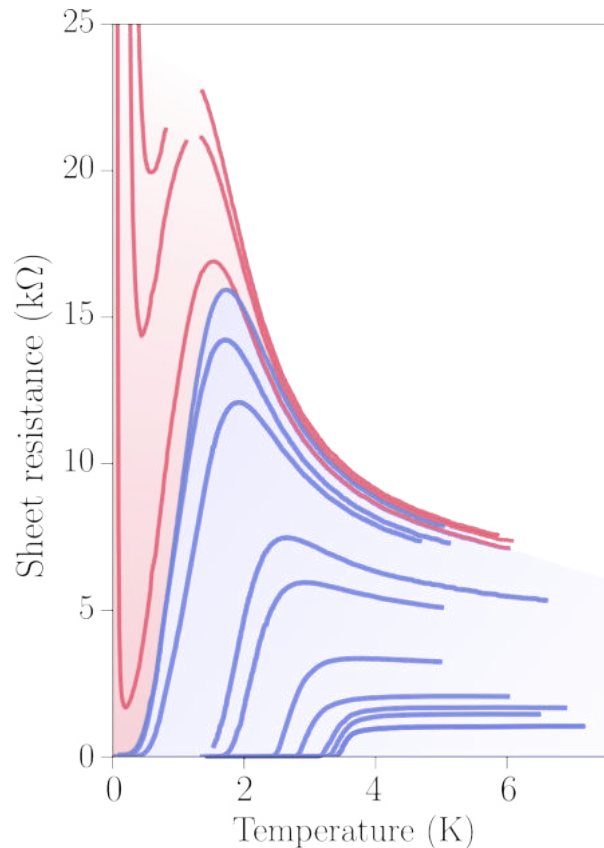


First-order quantum phase transition ?

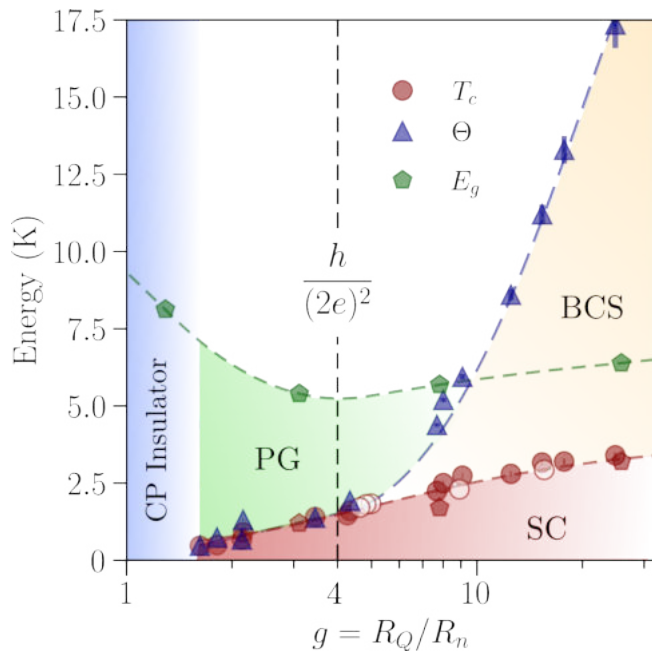


Conclusion

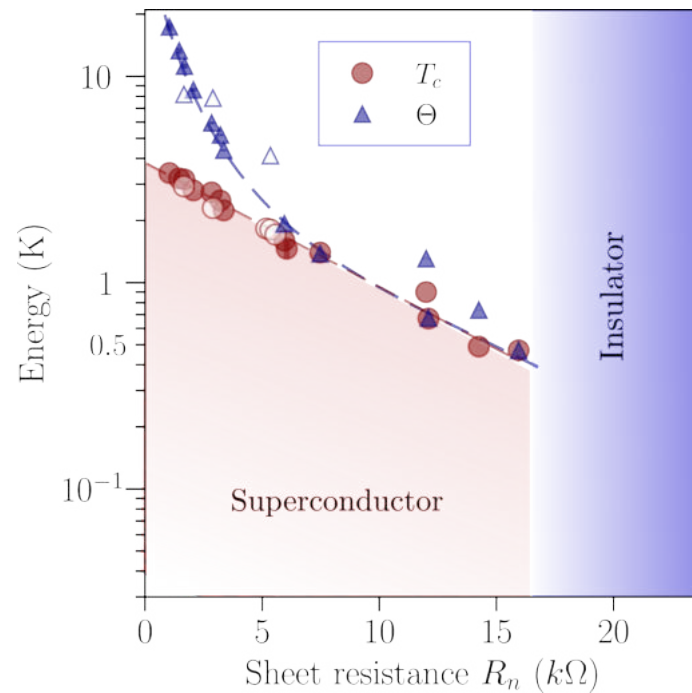
Superconductor-Insulator Transition



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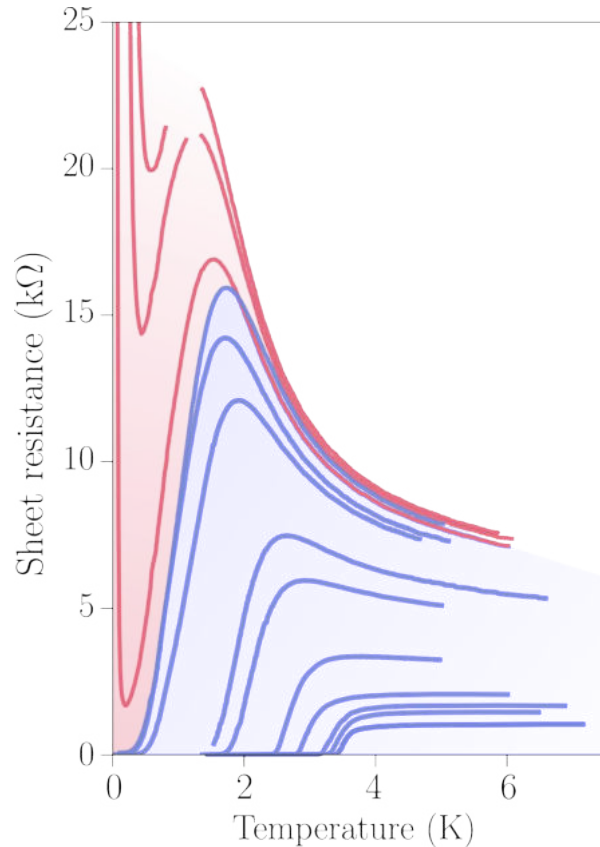


First-order quantum phase transition ?

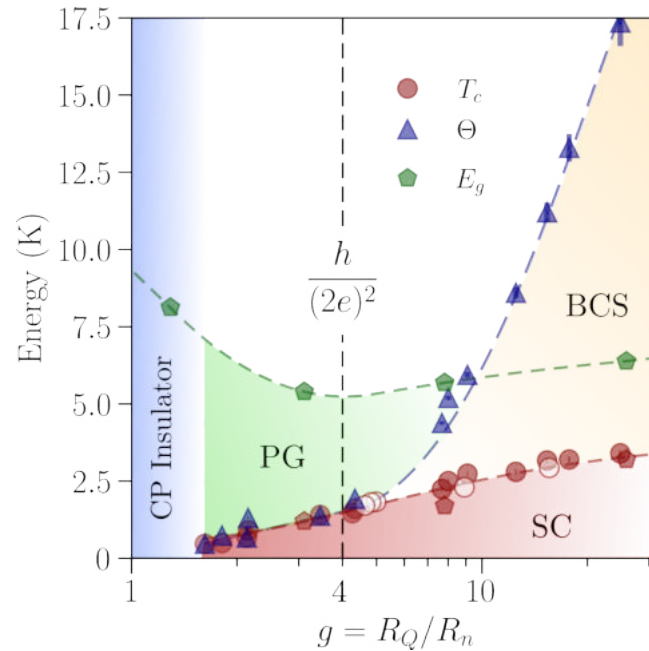


Conclusion

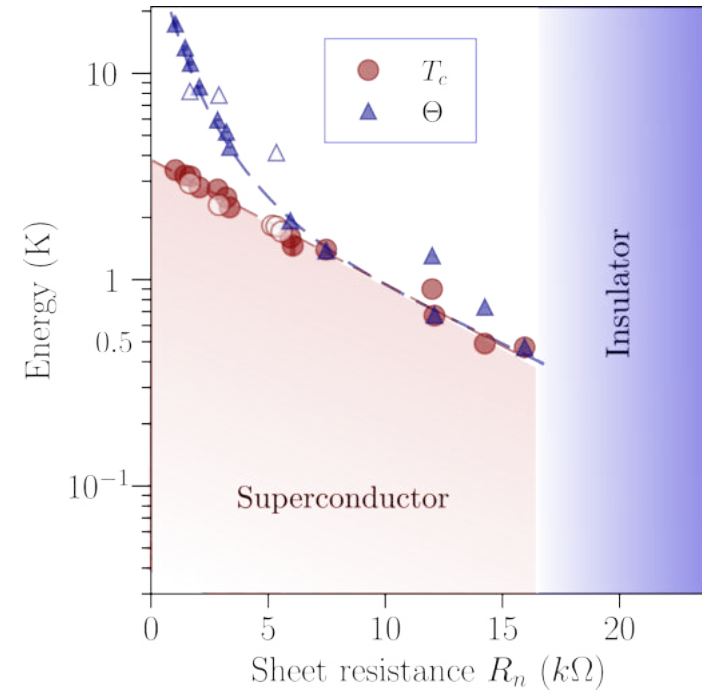
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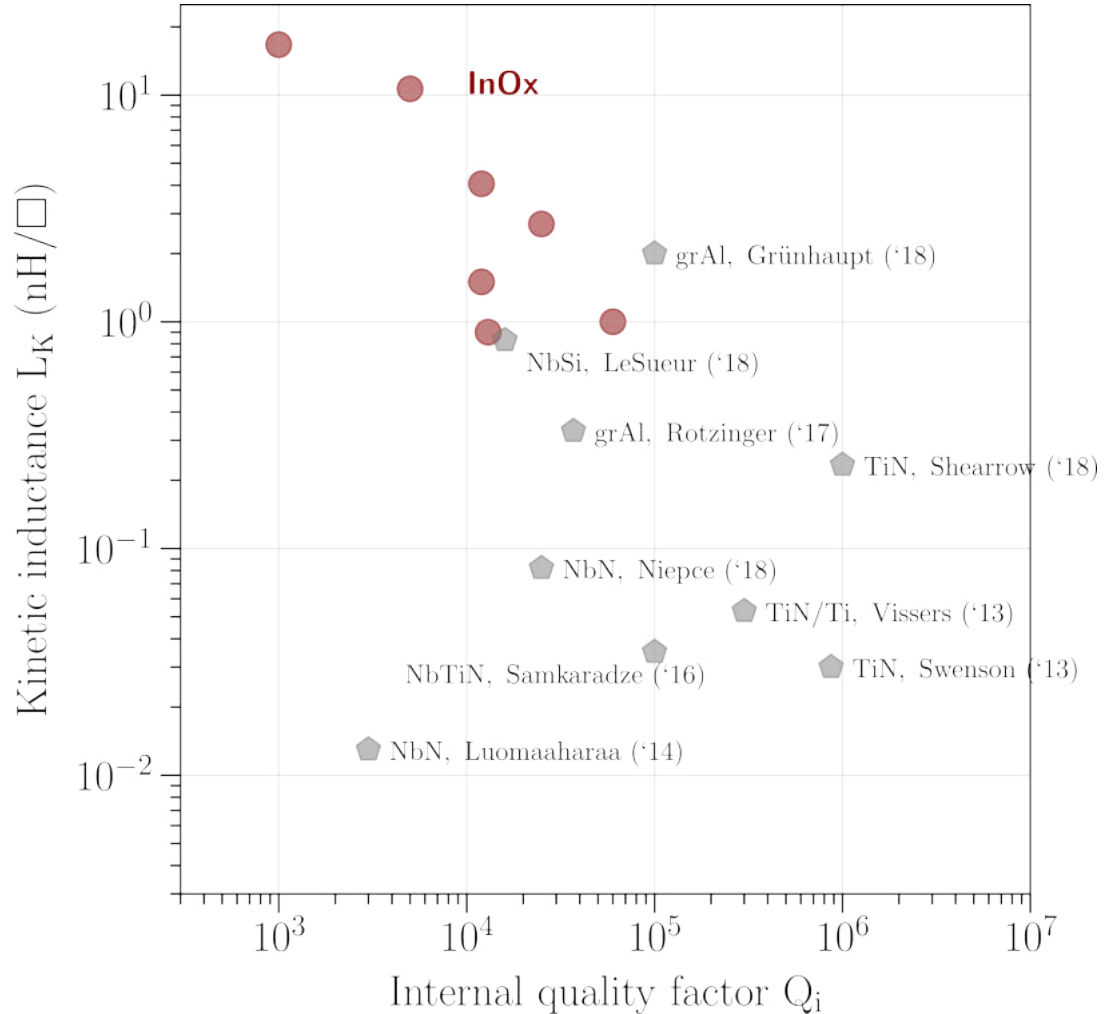
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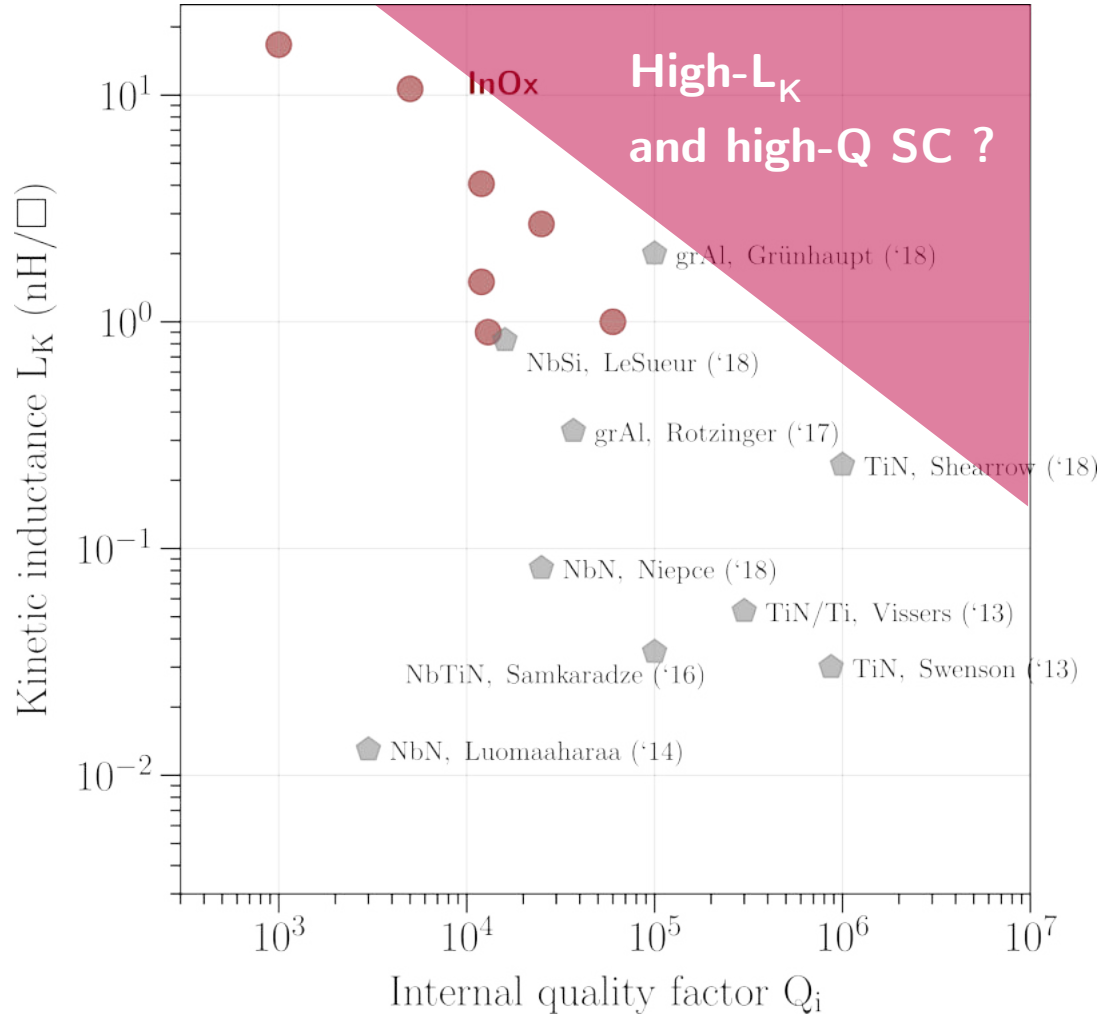
Applications of aInO resonators



Perspectives for cQED : understand losses



Perspectives for cQED : understand losses



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Supervisors



N. Roch



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O. Buisson



T. Grenet

Experimental



S. Léger



Kazi R. Amin



D. Basko



M. Feigel'man



L. Ioffe



A. Khvalyuk

Theory

Thank you !

